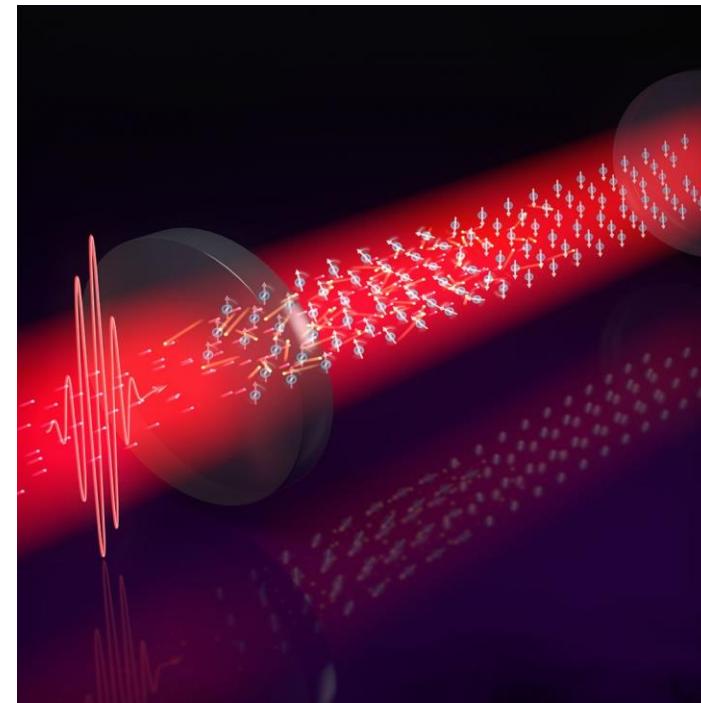
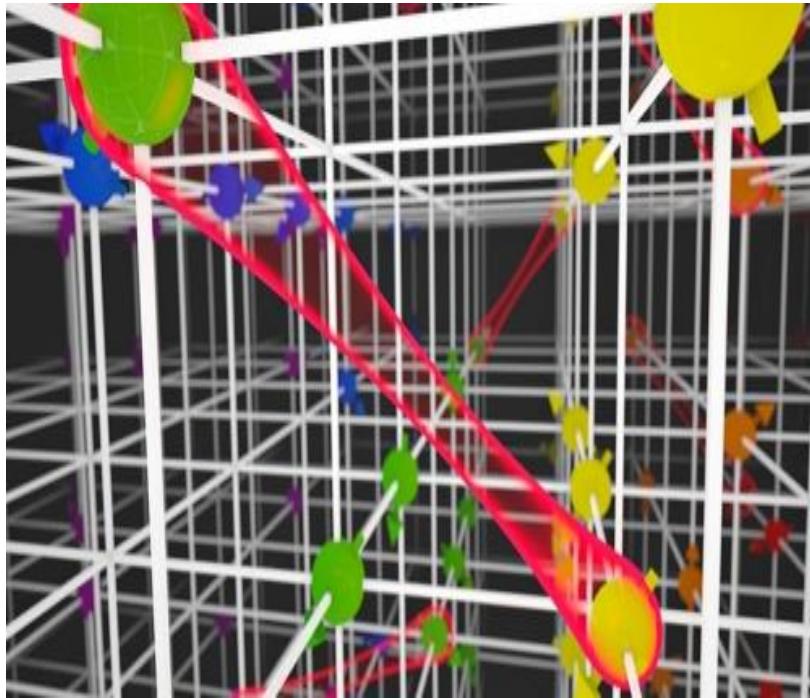
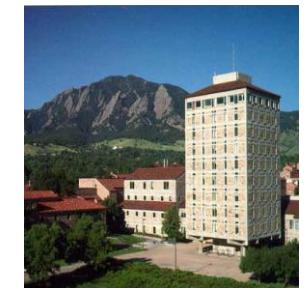


Dynamical Phase Transitions In Cold Atomic Gases

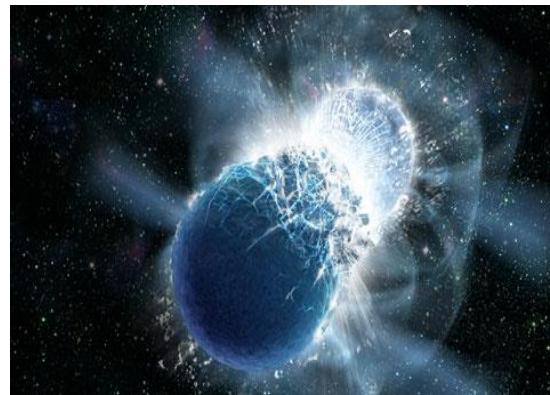
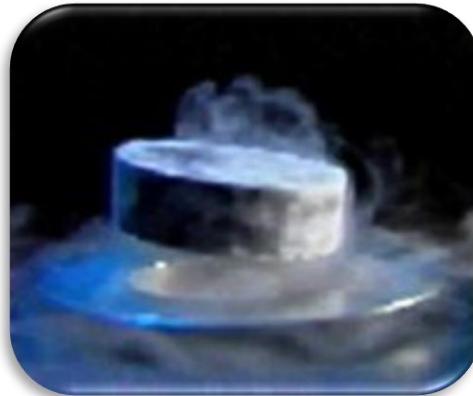


Ana Maria Rey



Quantum Science Seminar, July 30th (2020)

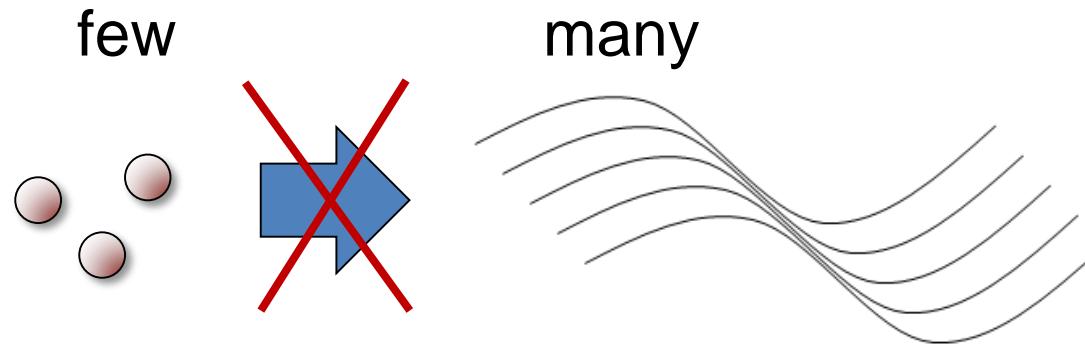
Many body systems are fascinating and useful



And typically Out-of-Equilibrium

... But They Are Extremely Complex

P. W. Anderson: “The behavior of a piece of matter is NOT just a sum of the behavior of its constituent particles” Nobel 1977



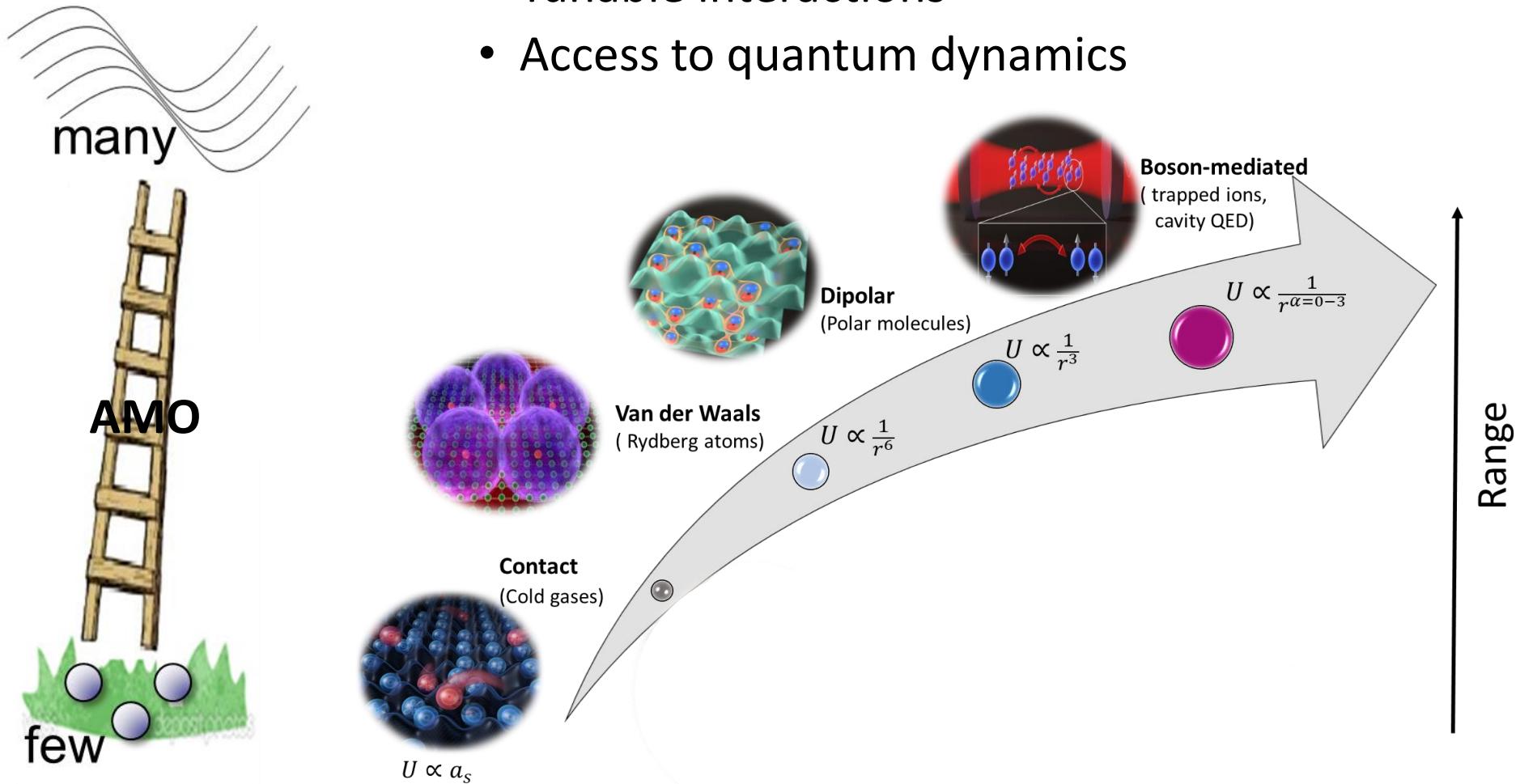
Specially out-of-equilibrium

- Can be strongly correlated and entangled
- Lack a simple description in terms of statistical mechanics
- Feature new types of exotic behaviors prohibited to exist at equilibrium conditions
- Can we understand them?

Scientific Vision

GOAL: Harnessing many-body quantum AMO systems and using them for applications ranging from quantum information to metrology.

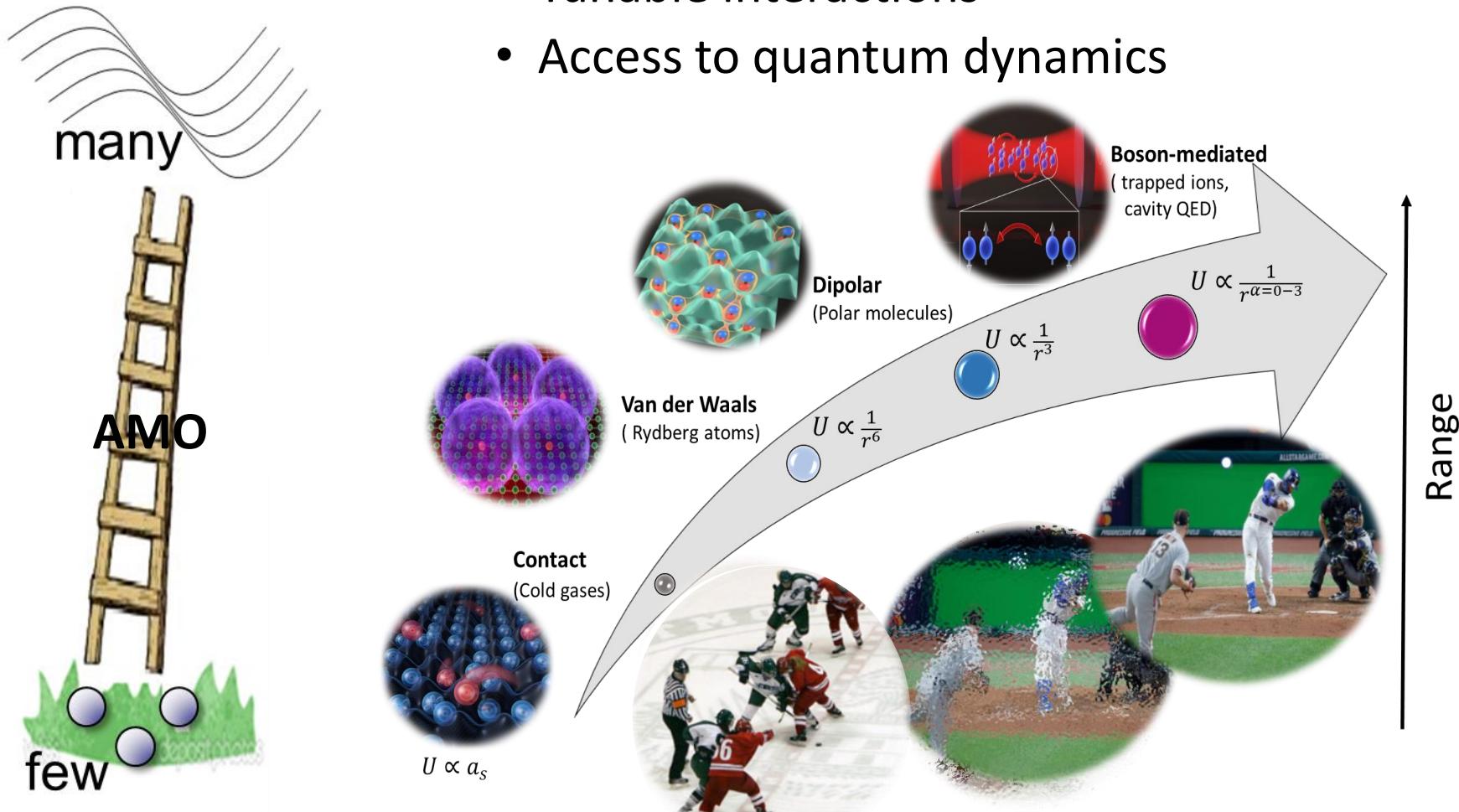
- Well-understood microscopics
- Tunable interactions
- Access to quantum dynamics



Scientific Vision

GOAL: Harnessing many-body quantum AMO systems and using them for applications ranging from quantum information to metrology.

- Well-understood microscopics
- Tunable interactions
- Access to quantum dynamics

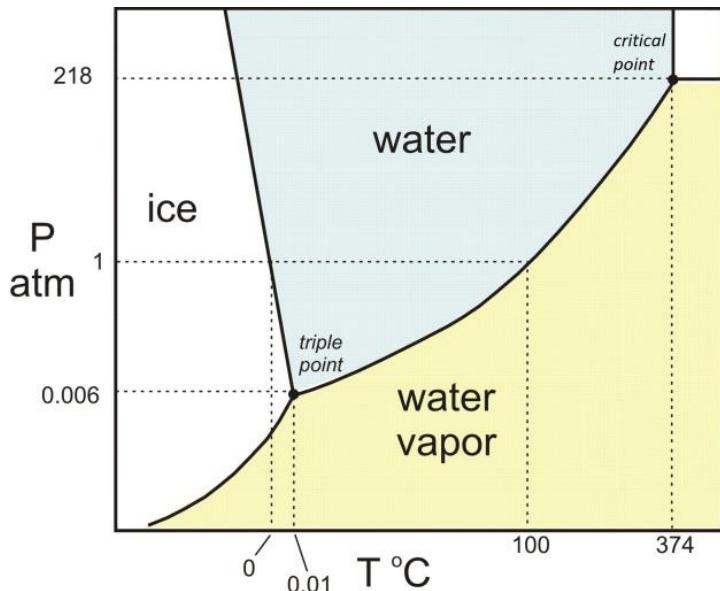


Equilibrium Phase Transitions

Phase Transition: Abrupt (non-analytic) change of behavior as a result of the change of system's parameters, such as temperature (classical), or others control parameter (quantum @ T=0).

Typically describe by an **order parameter**:

Quantity that changes non-analytically at the transition point.



Equilibrium:

- Minimization of Free energy.
- Slow change of system parameters.

Order Parameter: Density

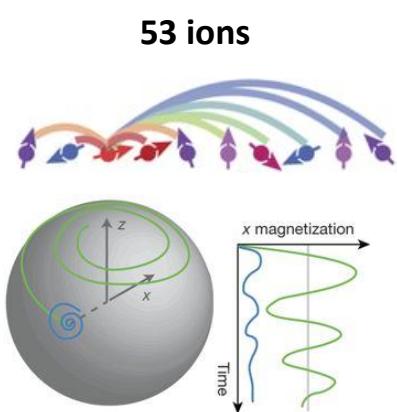
Non-Equilibrium Phase Transitions

Very General: Include open and closed systems:

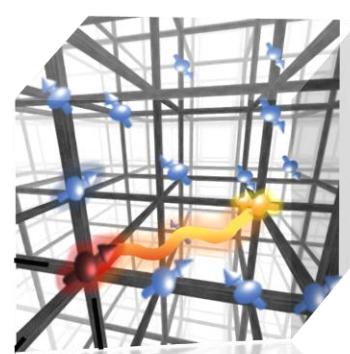
Here: Dynamical Phase Transitions (**Closed systems, Unitary Dynamics**)

A time averaged order parameter distinguishes two distinct dynamical phases and features a non-analytic behavior at the critical point.

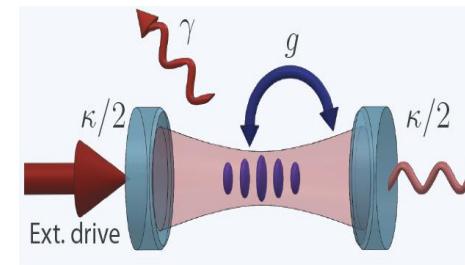
- Dynamical: Not found by minimization of free energy
- New symmetries
- Robust generation of useful entangled states



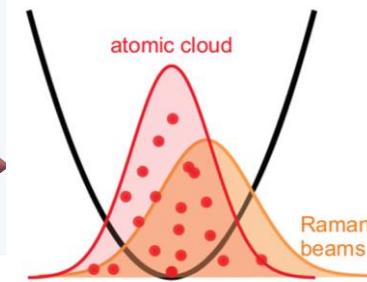
JQI, Nature(2018)



Toronto, Sci. Adv (2019)



JILA, Nature (2020)



Hannover, Arxiv(2020)

Other Definitions: Innsbruck, PRL(2017) & Hamburg, Nat. Phys (2018)

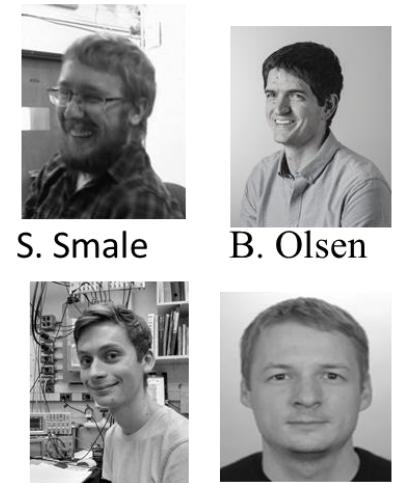
M. Heyl, EPLA (2019)

Theory

M. Mamaev



The Toronto team:



The JILA Sr teams:



James
Thompson



M. Norcia



J. Cline



J. Silva



D. Young



Jun Ye



Jan Arlt



Carsten
Klempt

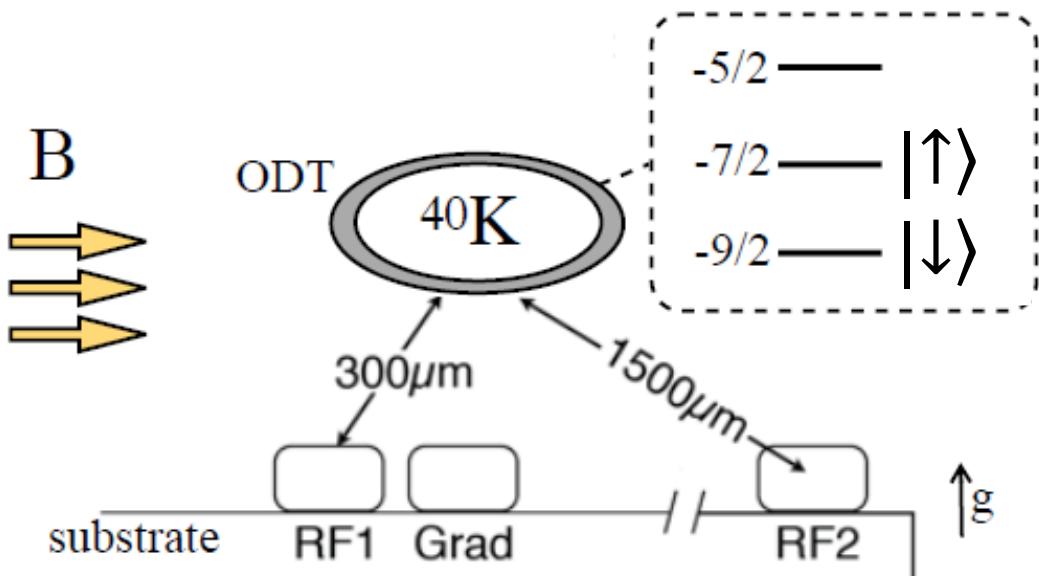


Toronto Experiment

S. Smale *et al* Science Advances 5, eaax1568 (2019)

3D Trapped Quantum degenerate ^{40}K , $T/T_F \sim 0.3\text{-}0.5$, $N \sim 3 \times 10^4$

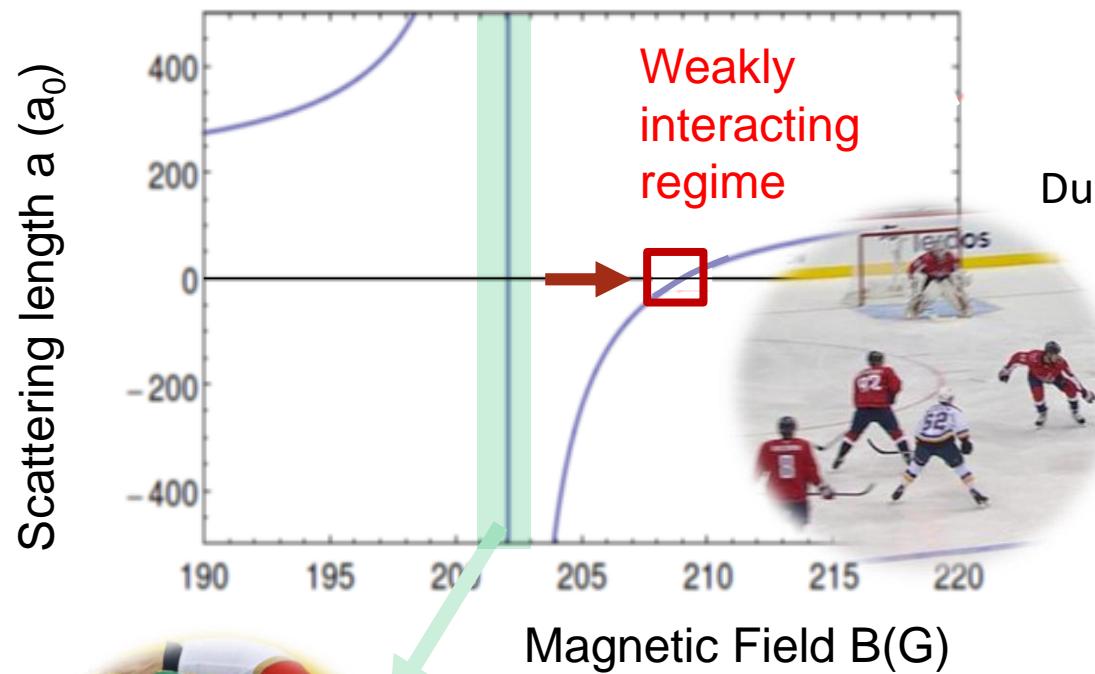
Use lowest two hyperfine states



Proximal wires give strong RF (for spin flips, gradient control)

Control of Interactions via Feshbach Resonance

- Strength of Contact of Interactions: set by a single parameter, scattering length
- In some atoms can be controllably varied via magnetic fields

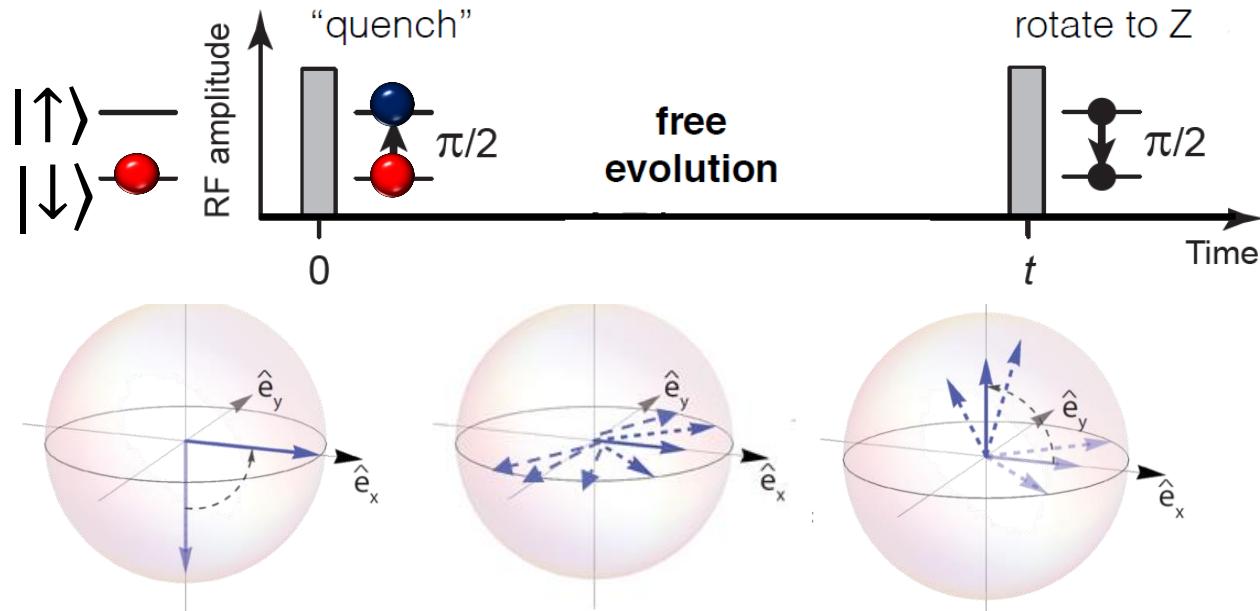


Strongly Interacting Regime:
Hydrodynamics Behavior
Connection to High T_c , Quark-Gluon plasma...

Observables

Stern-Gerlach

Total magnetization of ensemble



Directly observed:

total transverse magnetisation

$$c = \sqrt{\langle \hat{S}^x(t) \rangle^2 + \langle \hat{S}^y(t) \rangle^2}$$

$$\hat{S}^{x,y,z} = \sum_{i=1}^N s_i^{x,y,z}$$

but initial:

$$\langle \hat{S}^z(0) \rangle = 0$$

& constant

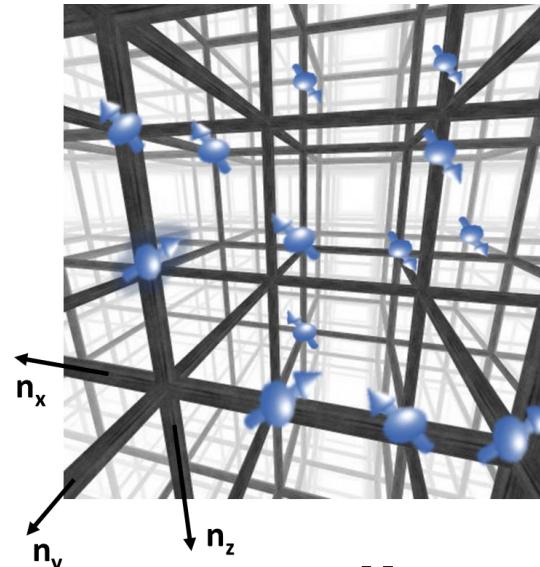
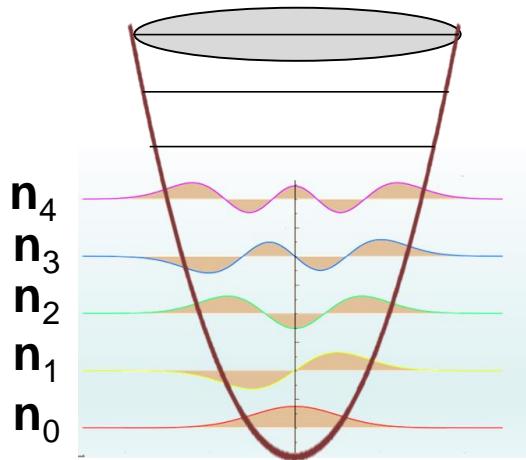
so can interpret it as:

$$s = \sqrt{\langle \vec{\hat{S}}(t) \cdot \vec{\hat{S}}(t) \rangle}$$

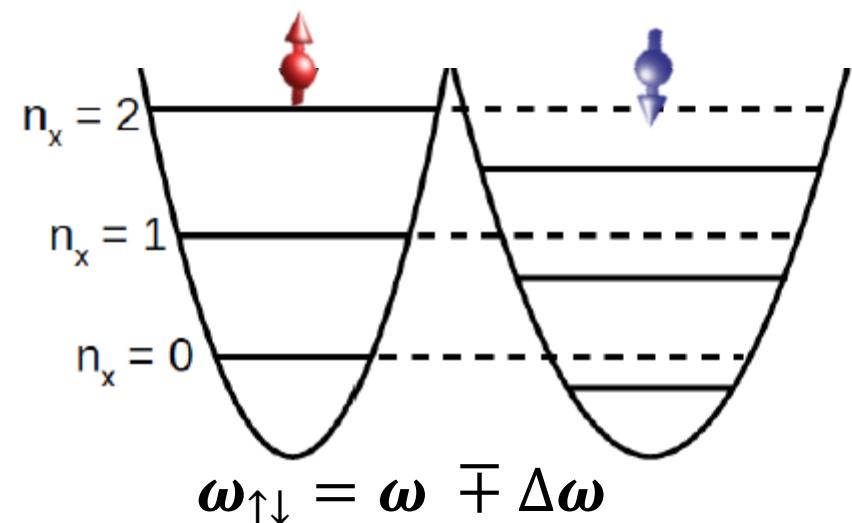
Total magnetization

Non-Interacting Atoms

Non-interacting 3D harmonic oscillator modes



Spin-dependent energy shifts



$$\hat{H}_0 = E + \sum_{i=1}^N h_i s_i^z$$

$$h_i = 2\Delta\omega \cdot \mathbf{n}_i$$

Control in the lab:

1. Curvature in (real) B
2. Vector light shift

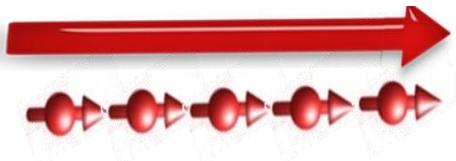
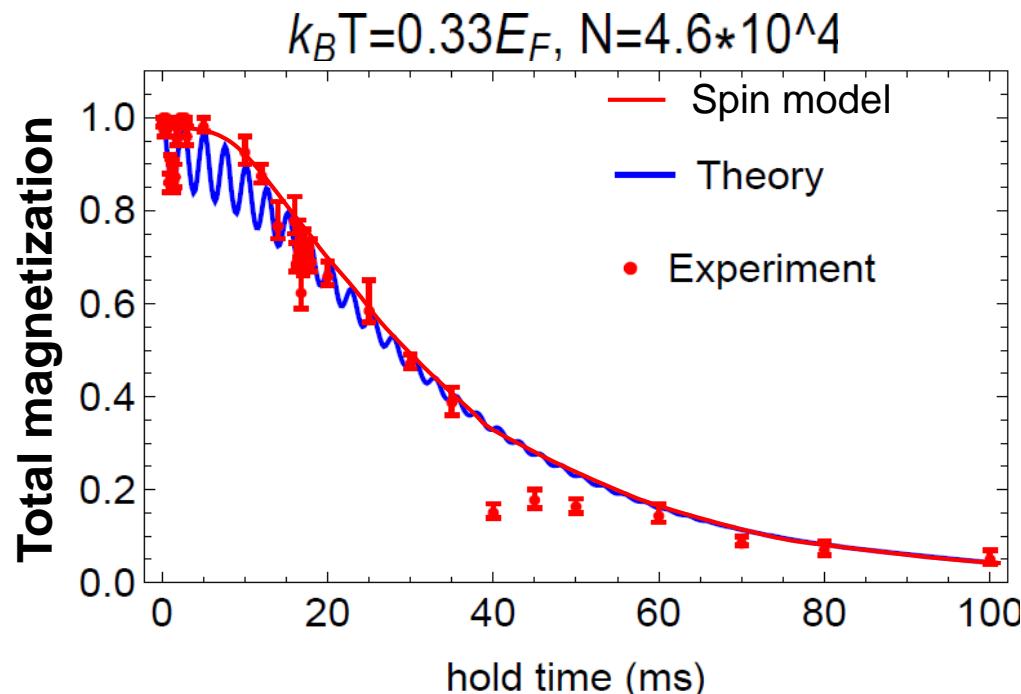
Non-Interacting Atoms

Dephasing: loss of phase coherence

$$\hat{H}_0 = \sum_i h_i s_i^z$$

$$h_i = 2\Delta\omega \cdot \mathbf{n}_i$$

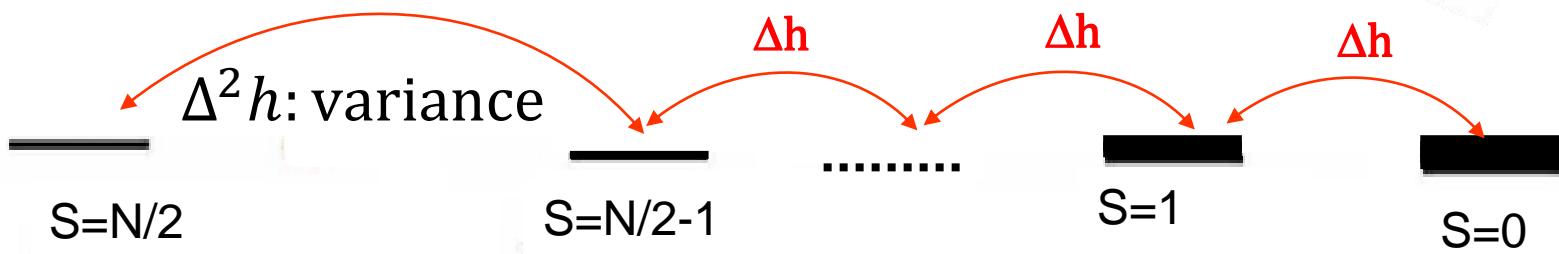
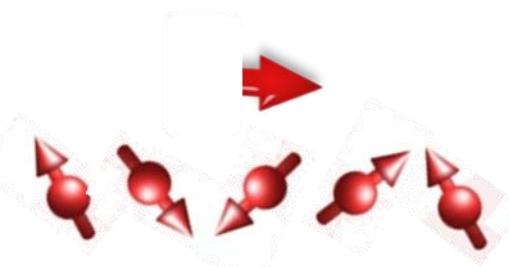
$$\hat{S}^{x,y,z} = \sum_{i=1}^N s_i^{x,y,z}$$



Δh

H_0 does not conserve S

$$(\hat{\vec{S}} \cdot \hat{\vec{S}}) |S, M\rangle = S(S+1) |S, M\rangle$$

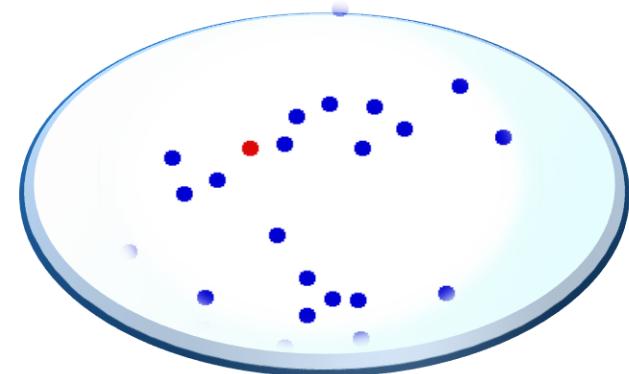


Weakly Interacting gas

Idea: Model the atoms as quantum magnets- frozen in energy space

Position

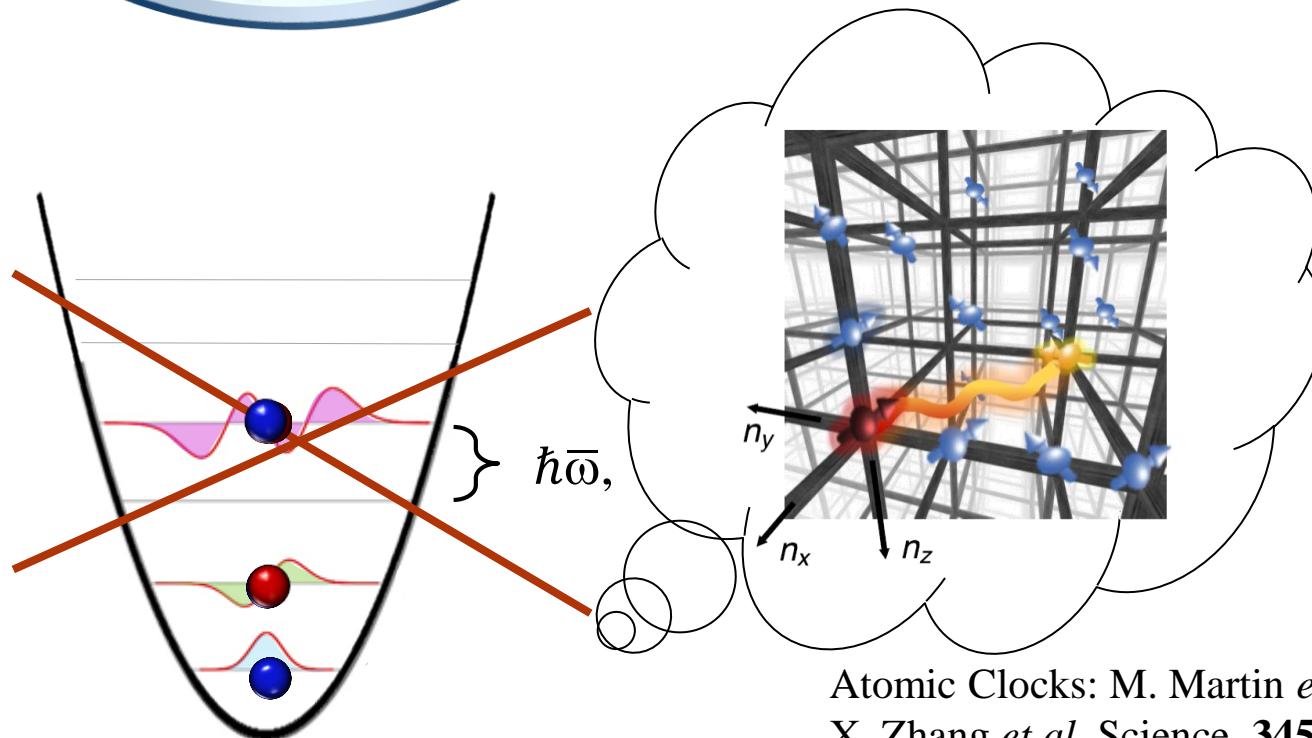
Hard to model



Weak interactions simplify physics

Frozen motional levels

Delocalized modes: Long range interactions



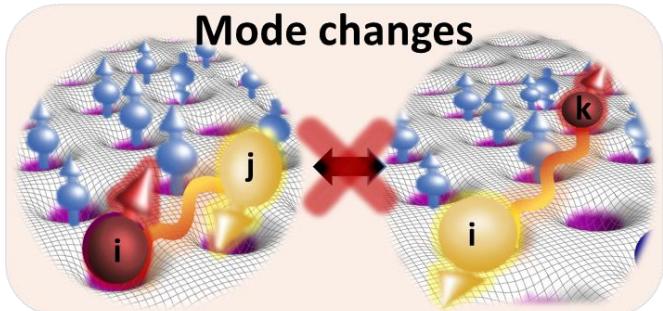
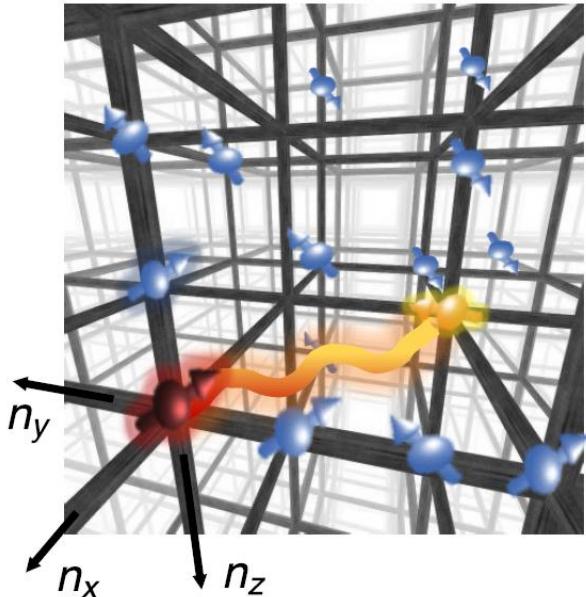
**Energy lattice:
Spin model**

Atomic Clocks: M. Martin *et al*, Science **341**, 632 (2013)
X. Zhang *et al*, Science **345**, 1467 (2014)

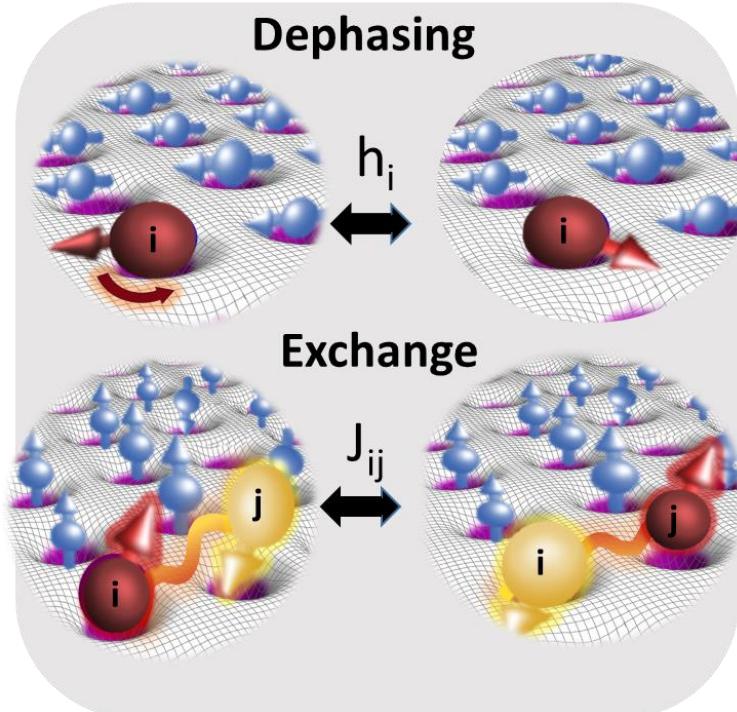
Weakly Interacting gas

Spin model approximation: Frozen motional levels

Spin lattice model



$$\hat{H} = - \sum_{i>j} J_{ij}(a) \vec{\hat{S}}_i \cdot \vec{\hat{S}}_j + \sum_i h_i \hat{S}_i^z$$



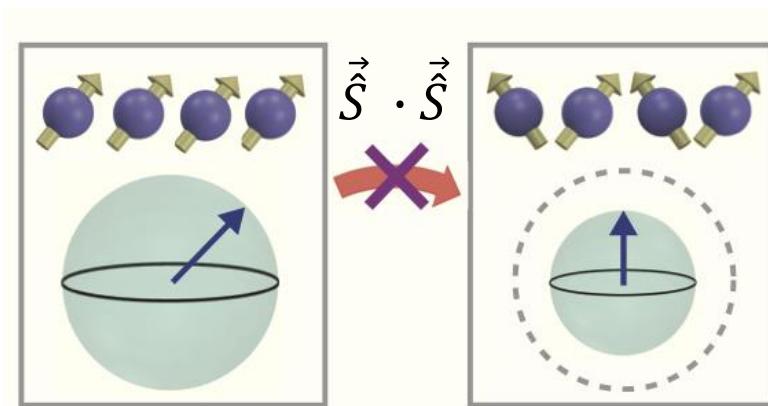
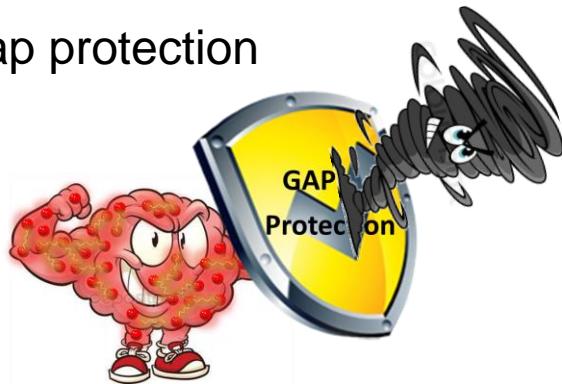
a : scattering length

$$J_{ij} \propto a \int d^3\mathbf{r} (\phi_{\uparrow n_i}^2(\mathbf{r}) \phi_{\downarrow n_j}^2(\mathbf{r}))$$

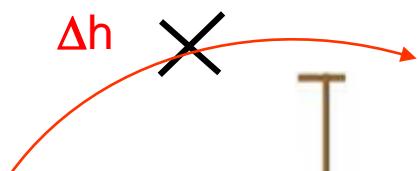
Weakly Interacting gas

$$\hat{H} = - \sum_{i>j} J_{ij} \vec{\hat{S}}_i \cdot \vec{\hat{S}}_j + \hat{H}_0$$

Gap protection



Stabilizes alignment



Exchange energy change from

$$S = N/2 \rightarrow S = N/2 - 1$$

Collective gap

PHYSICAL REVIEW A 77, 052305 (2008)

s Many-body protected entanglement generation in interacting spin systems

A. M. Rey,¹ L. Jiang,² M. Fleischhauer,³ E. Demler,² and M. D. Lukin^{1,2}

Mean-Field Picture

$$\hat{H}_{MF} = \sum_i \hat{\vec{S}}_i \cdot \vec{B}_i^{\text{ef}}(t)$$

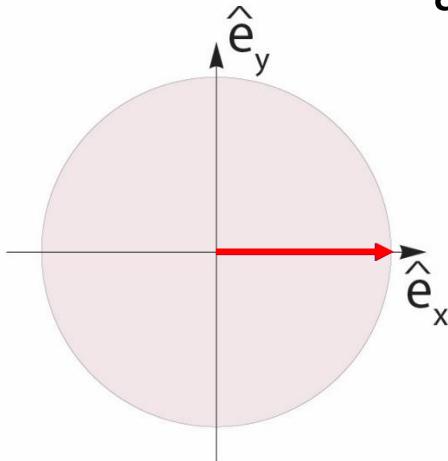
$$\vec{B}_i^{\text{ef}} = h_i \hat{z} - 2 \sum_j^N J_{ij} \left\langle \hat{\vec{S}}_j(t) \right\rangle$$

Semi-classical picture:

Identical spin-rotation effect (ISRE)

C. Lhuillier, F. Laloe, *J. Phys.-Paris* **43**, 225 (1982).

A time dependent effective magnetic field generated by other atoms which favors alignment



Non Interacting

Large enough
Interactions

Self-rephasing with increasing interaction

Rb atoms magnetically trapped on a chip: C. Deutsch *et al* PRL (2010).

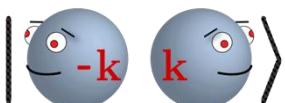
C. Solaro *et al* PRL (2016)

Simulating a BCS Superconductor

$$H \sim \sum_k \epsilon_k \hat{s}_k^z + \frac{J}{2} \sum_{kq} \hat{s}_k^+ \hat{s}_q^- = \sum_k \epsilon_k \hat{s}_k^z + J \hat{S}^+ \cdot \hat{S}^-$$



$$\langle s_{\mathbf{k}}^z \rangle = +\frac{1}{2}$$



$$\langle s_{\mathbf{k}}^z \rangle = -\frac{1}{2}$$



$$\Delta \equiv \frac{J}{2} \langle \hat{S}^- \rangle \quad \text{Order parameter or gap function}$$

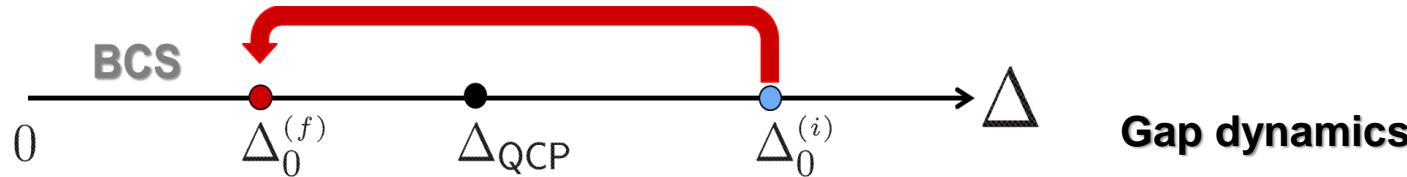
$$|\langle \hat{S}^- \rangle| = \sqrt{\langle \hat{S}^x(t) \rangle^2 + \langle \hat{S}^y(t) \rangle^2}$$

- Integrable (Richardson-Gaudin model)

Method: Self-consistent non-equilibrium mean field theory

- Exact solution to nonlinear classical spin dynamics via integrability,
- Lax construction: Frequency spectrum ruling dynamics V. Gurarie, M. Foster

Quenches in superconductors



Collective Rabi Oscillations and Solitons in a Time-Dependent BCS Pairing ProblemR. A. Barankov,¹ L. S. Levitov,¹ and B. Z. Spivak²¹*Department of Physics, Massachusetts Institute of Technology, 77 Massachusetts Ave, Cambridge, Massachusetts 02139, USA*²*Department of Physics, University of Washington, Seattle, Washington 98195, USA***REPORTS**PRL 96ending
NE 2006**SUPERCONDUCTIVITY****Quantum Light-induced collective pseudospin precession resonating with Higgs mode in a superconductor**¹Ce

4

⁴*1 Ryusuke Matsunaga,^{1,*} Naoto Tsuji,¹ Hiroyuki Fujita,¹ Arata Sugioka,¹ Kazumasa Makise,² Yoshinori Uzawa,^{3,†} Hirotaka Terai,² Zhen Wang,^{2,‡} Hideo Aoki,^{1,4} Ryo Shimano^{1,5*}*

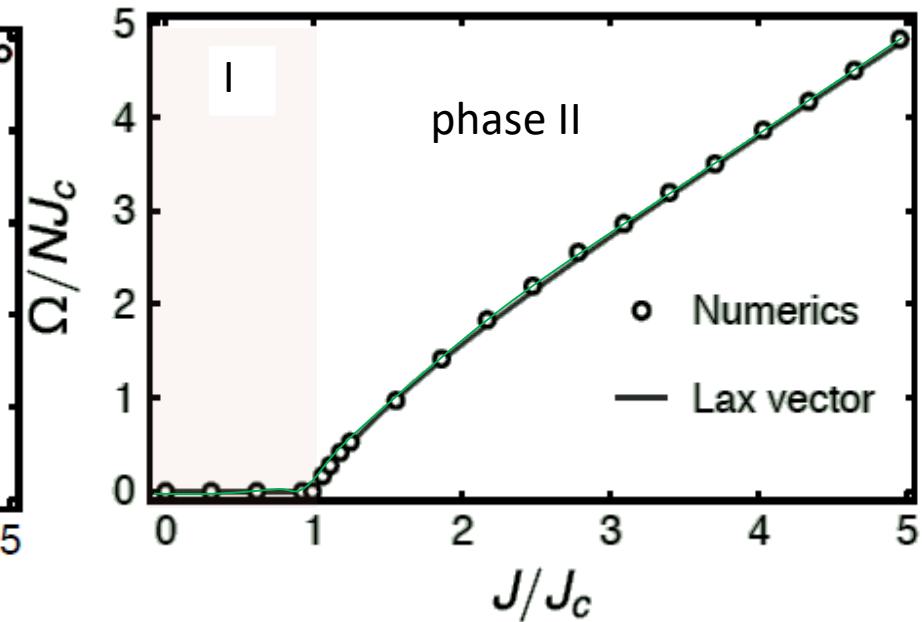
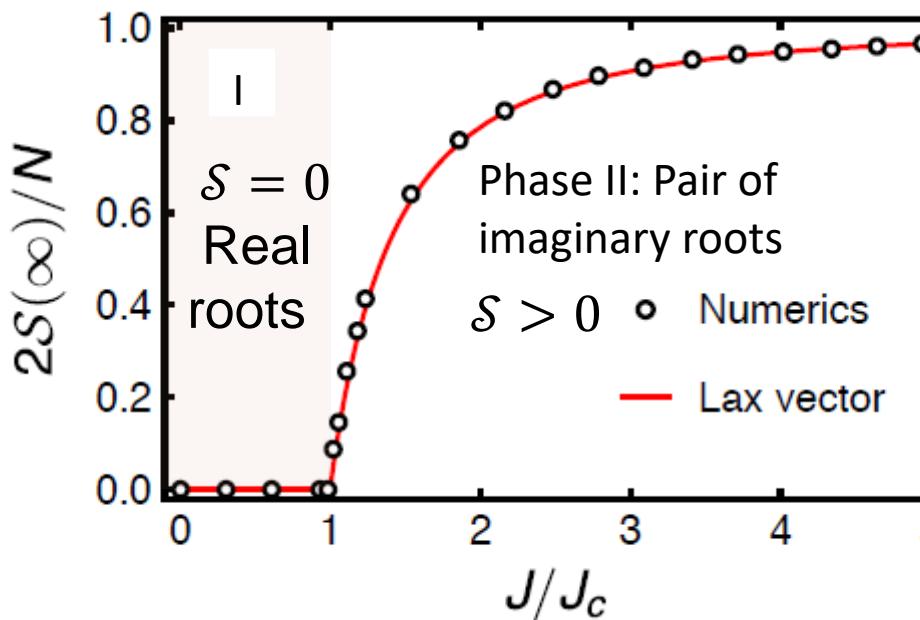
- Hard in real materials.
- Need of ultra-fast pulses
- Small quenches

Dynamical Phase Transition (All-To-All)

$$\hat{H} \approx -\bar{J} \vec{\hat{S}} \cdot \vec{\hat{S}} + \sum_i h_i s_i^z \quad \bar{J} \propto a/\sqrt{N}$$

Gap Frequency: Ω

$$\Omega = 2JS(\infty)$$



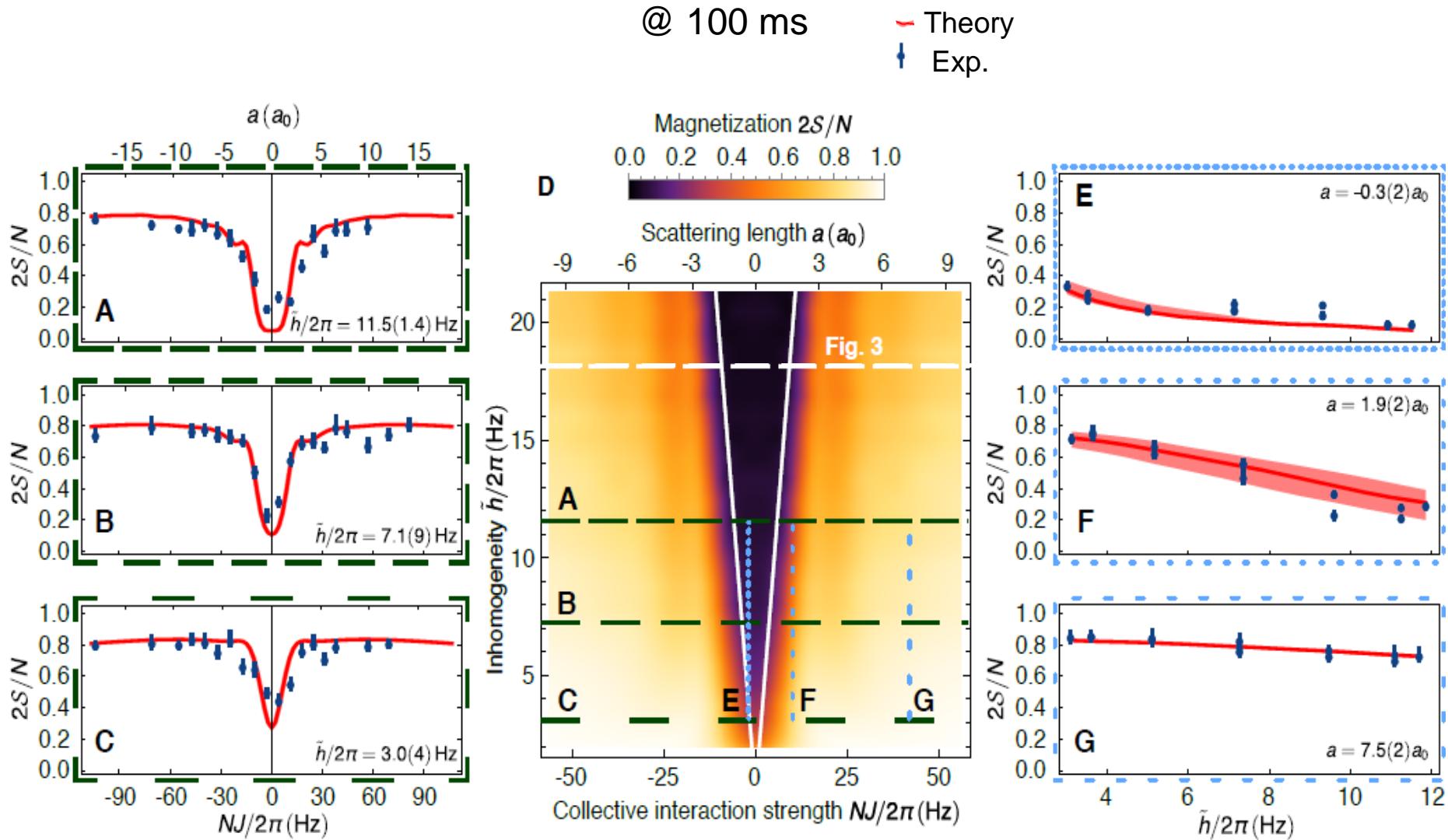
Finite steady state magnetization $J > J_c$

$$S(\infty) = \frac{N}{2} \frac{\pi J_c}{2J} \cot\left(\frac{\pi J_c}{2J}\right)$$

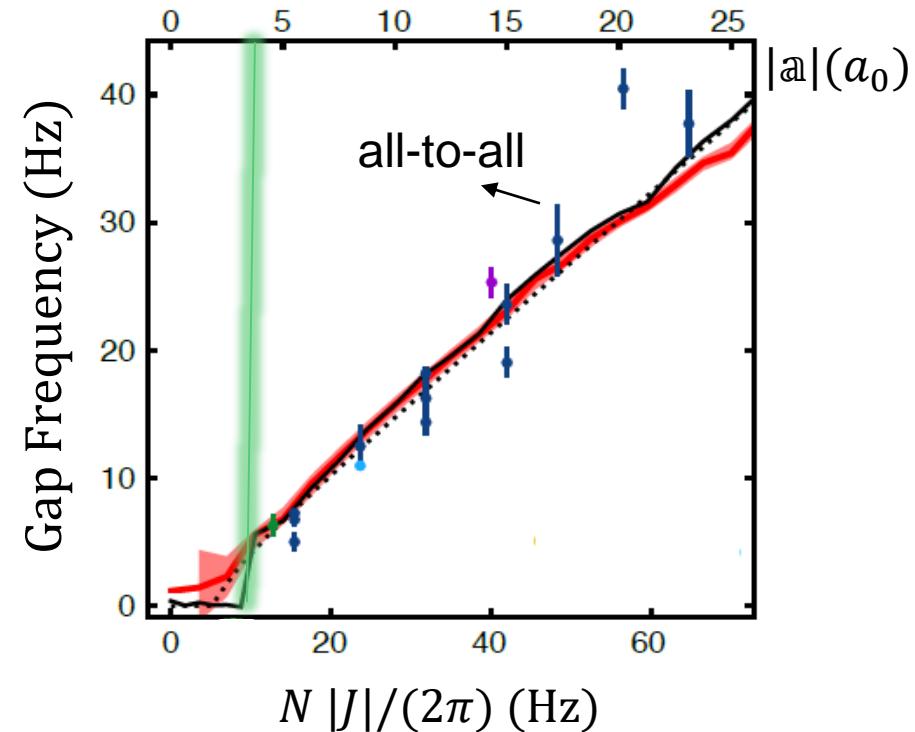
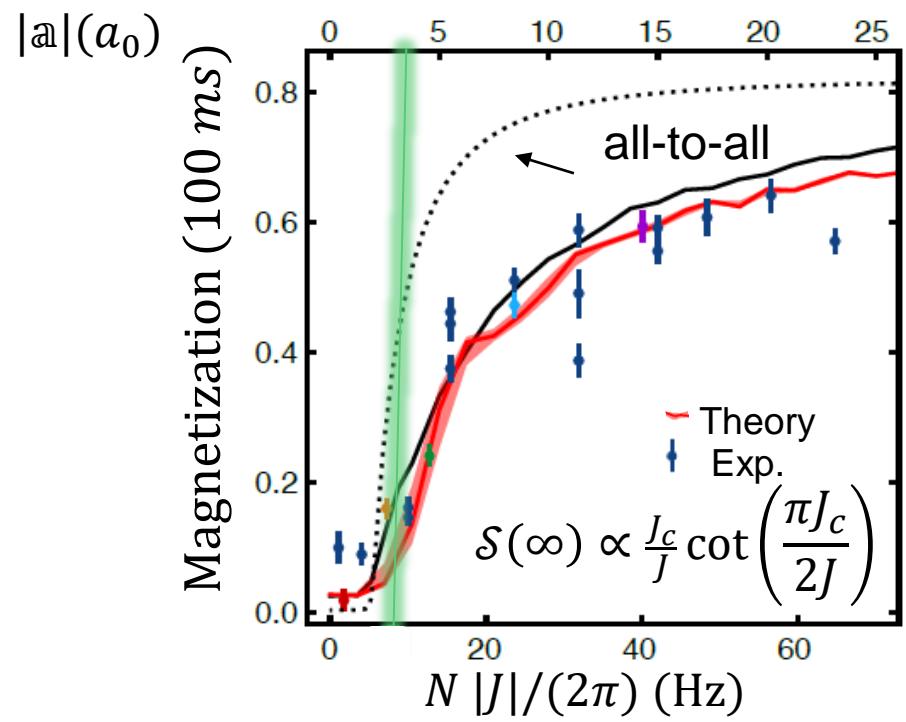
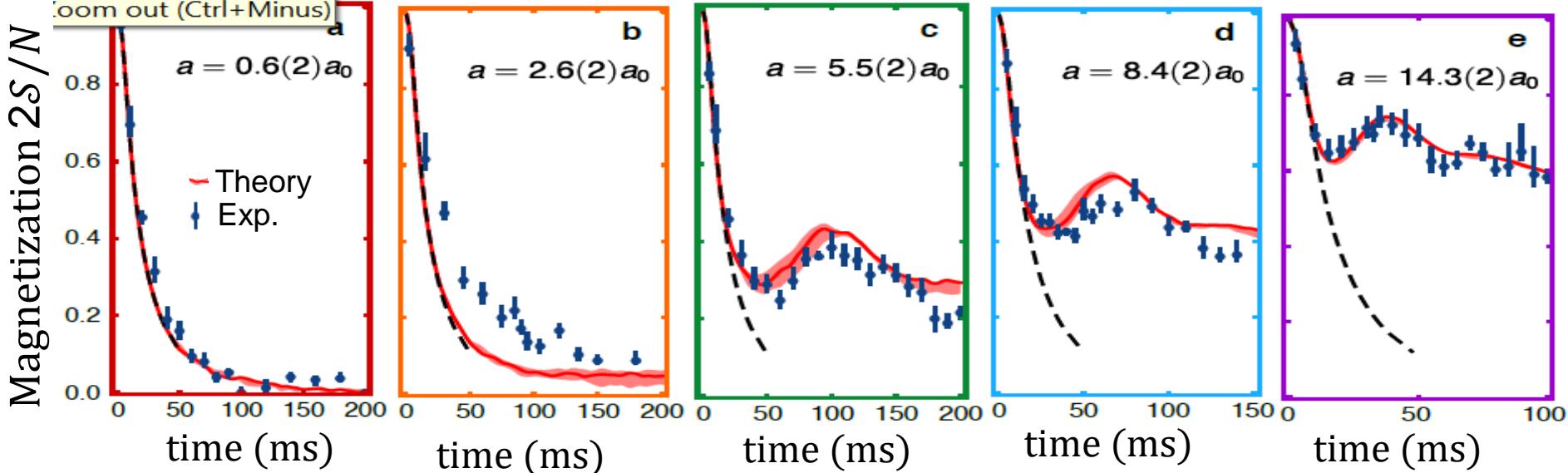
$$NJ_c = \frac{2\sqrt{3}(\Delta h)}{\pi}$$

For 1D Exact

Dynamical Phase Transition - Observation

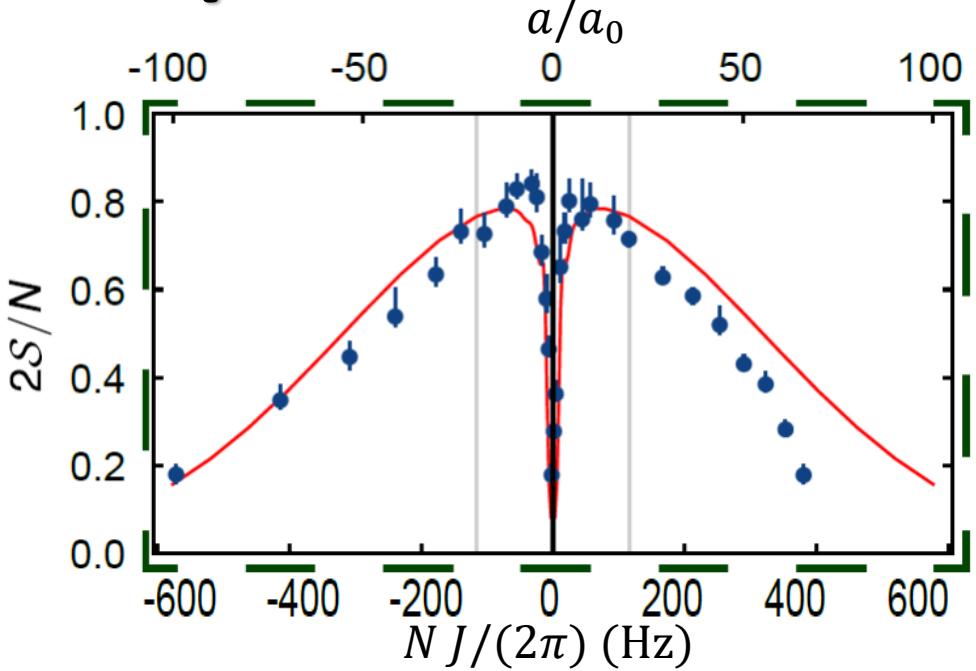


Dynamical Phase Transition - Observation



Validity of the spin model

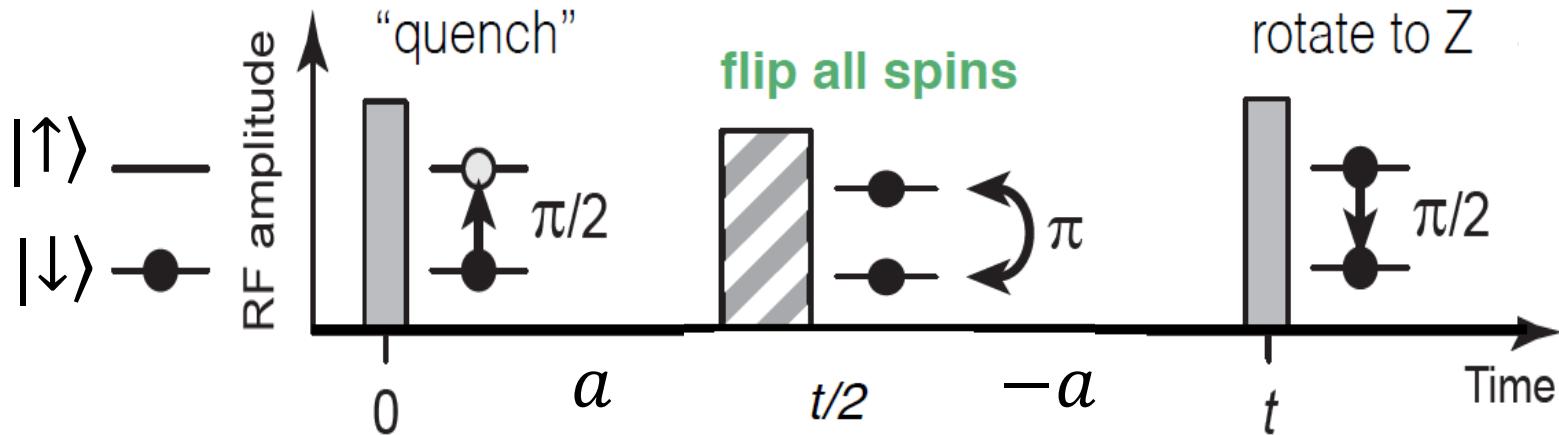
$$\mathcal{S}(t) \rightarrow \mathcal{S}(t)e^{-\Gamma(a)t}$$
$$\Gamma(a) = \Gamma_0 + \gamma \left(\frac{a}{a_0} \right)^2$$



Validity of the spin model

Idea: Use many body echo

If we can time reverse the spin model then we should not see dynamics



$$\hat{H} = - \sum_{i>j} J_{ij} \hat{\vec{s}}_i \cdot \hat{\vec{s}}_j + \sum_i h_i \hat{s}_i^z$$

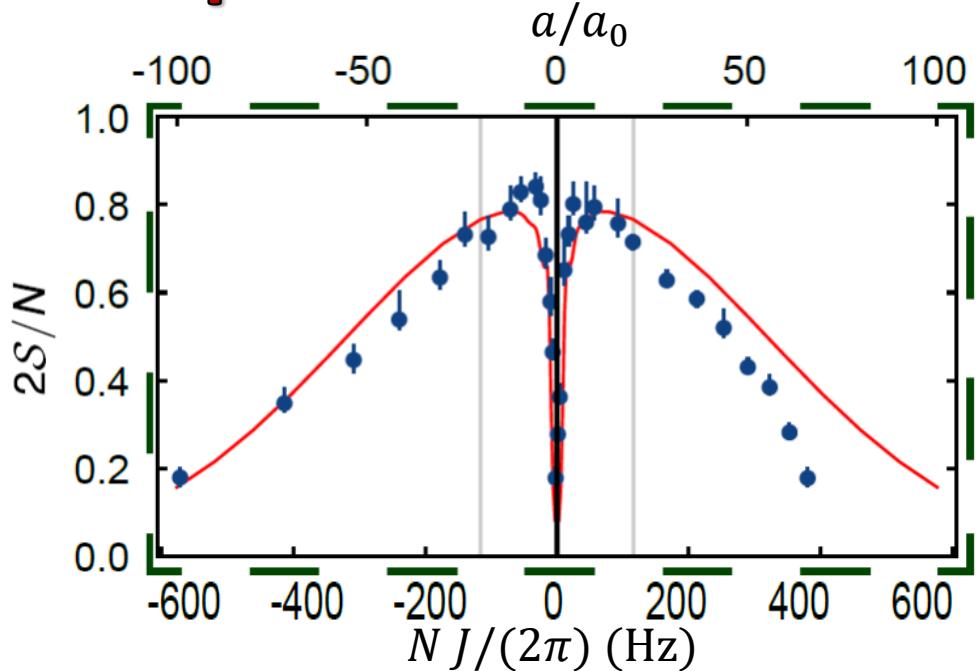
$$\hat{H}\psi \rightarrow -\hat{H}\psi$$

..as if $t \rightarrow -t$

Validity of the spin model

No time reversal

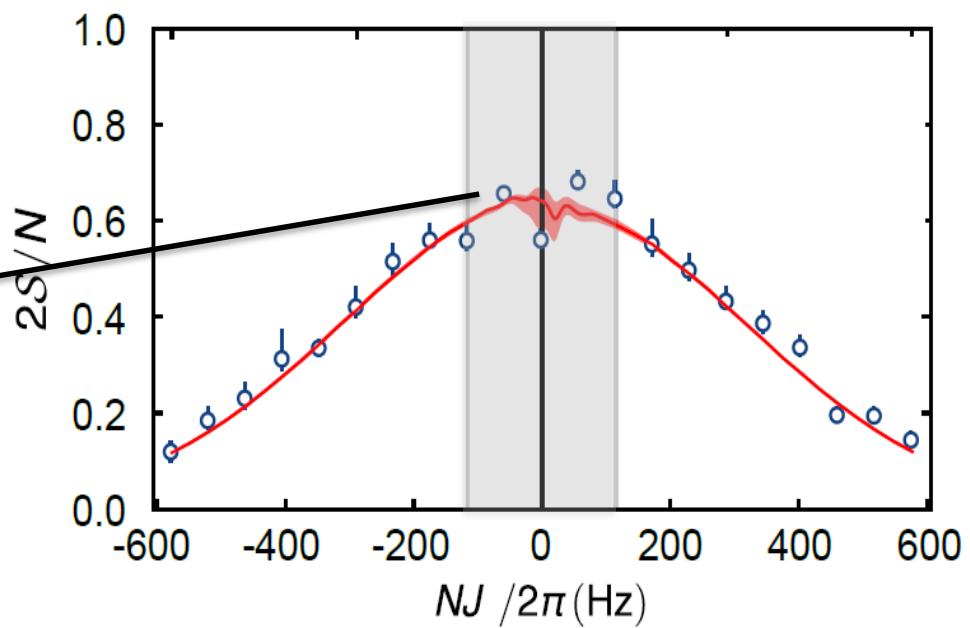
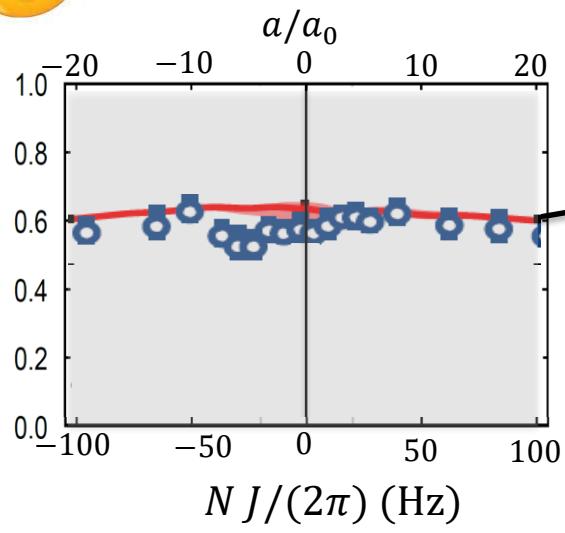
$$\begin{aligned}\mathcal{S}(t) &\rightarrow \mathcal{S}(t)e^{-\Gamma(a)t} \\ \Gamma(a) &= \Gamma_0 + \gamma \left(\frac{a}{a_0} \right)^2\end{aligned}$$



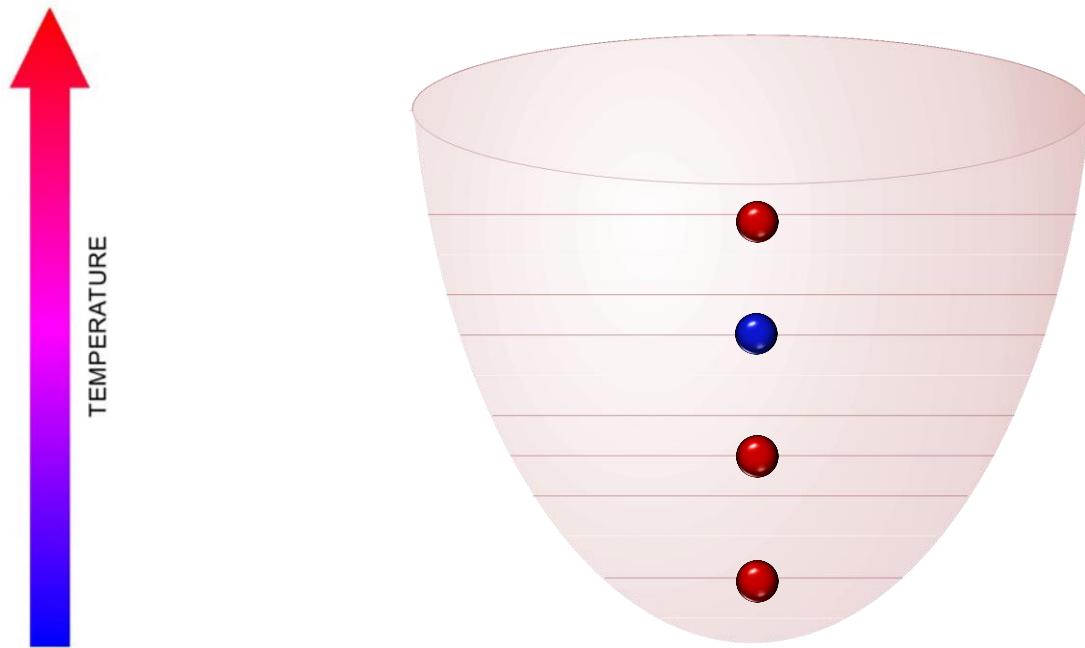
Time reversal



$$\Gamma(a) = \tilde{\Gamma}_0 + \gamma \left(\frac{a}{a_0} \right)^2$$



Thermal Bosons and Fermions Alike



Doubly occupied modes energetically suppressed $T \gg T_c$

Thermal bosons can also be described by a spin model in the collisionless regime: trapping frequency \gg interaction

Bosonic Spin Model

A. Chu, J. Will, J. Arlt, C. Klempt, and A. M. Rey, arXiv:2004.01282

- ^{87}Rb atomic gases $|\downarrow\rangle \equiv |F = 1, m_F = 0\rangle$ $|\uparrow\rangle \equiv |F = 2, m_F = 0\rangle$

$$H_{\text{int}} = \sum_{ij} J_{ij} \mathbf{S}_i \cdot \mathbf{S}_j + \sum_{ij} \chi_{ij} S_i^z S_j^z + \sum_i B_i S_i^z$$

$$J_{ij} = \frac{4\pi\hbar^2}{m} V_{ij}^{\text{ex}} a_{\uparrow\downarrow} \quad a_{\sigma\sigma'} : \text{scattering lengths}$$

$$\chi_{ij} = \frac{4\pi\hbar^2}{m} \left(V_{ij}^{\uparrow\uparrow} a_{\uparrow\uparrow} + V_{ij}^{\downarrow\downarrow} a_{\downarrow\downarrow} - V_{ij}^{\uparrow\downarrow} a_{\uparrow\downarrow} - V_{ij}^{\text{ex}} a_{\uparrow\downarrow} \right)$$

$$B_i = \frac{4\pi\hbar^2}{m} \sum_j \left(V_{ij}^{\uparrow\uparrow} a_{\uparrow\uparrow} - V_{ij}^{\downarrow\downarrow} a_{\downarrow\downarrow} \right) + h_i$$

$$V_{ij}^{\text{ex}} = \int d^3\mathbf{R} \phi_i^{\uparrow\uparrow}(\mathbf{R}) \phi_i^{\downarrow\downarrow}(\mathbf{R}) \phi_j^{\uparrow\uparrow}(\mathbf{R}) \phi_j^{\downarrow\downarrow}(\mathbf{R}) \quad V_{ij}^{\sigma\sigma'} = \int d^3\mathbf{R} [\phi_i^\sigma(\mathbf{R})]^2 [\phi_j^{\sigma'}(\mathbf{R})]^2$$

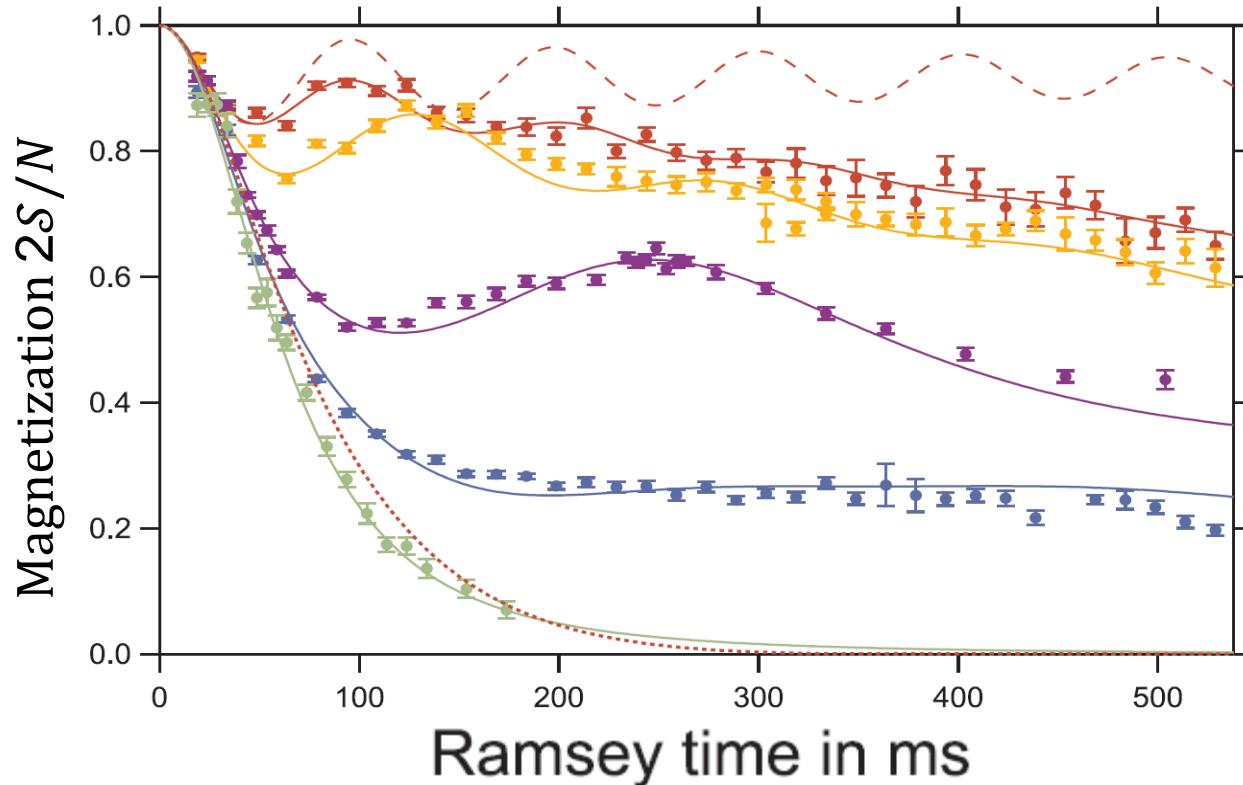
^{87}Rb Experiment: Similar DPT

$$|\downarrow\downarrow\rangle \equiv |F = 1, m_F = 0\rangle \quad |\uparrow\uparrow\rangle \equiv |F = 2, m_F = 0\rangle$$

$$\phi_i^{\uparrow}(\mathbf{R}) = \phi_i^{\downarrow}(\mathbf{R})$$

$$H_{\text{int}} = \sum_{ij} J_{ij} \mathbf{S}_i \cdot \mathbf{S}_j + \sum_{ij} \chi_{ij} S_i^z S_j^z + \sum_i B_i S_i^z$$

$$\chi_{ij} = \frac{4\pi\hbar^2}{m} (V_{ij}^{\uparrow\uparrow} a_{\uparrow\uparrow} + V_{ij}^{\downarrow\downarrow} a_{\downarrow\downarrow} - V_{ij}^{\uparrow\downarrow} a_{\uparrow\downarrow} - V_{ij}^{\text{ex}} a_{\uparrow\downarrow}) = \frac{4\pi\hbar^2}{m} V_{ij} (a_{\uparrow\uparrow} + a_{\downarrow\downarrow} - 2a_{\uparrow\downarrow})$$



Increasing density



P. Rosenbusch group

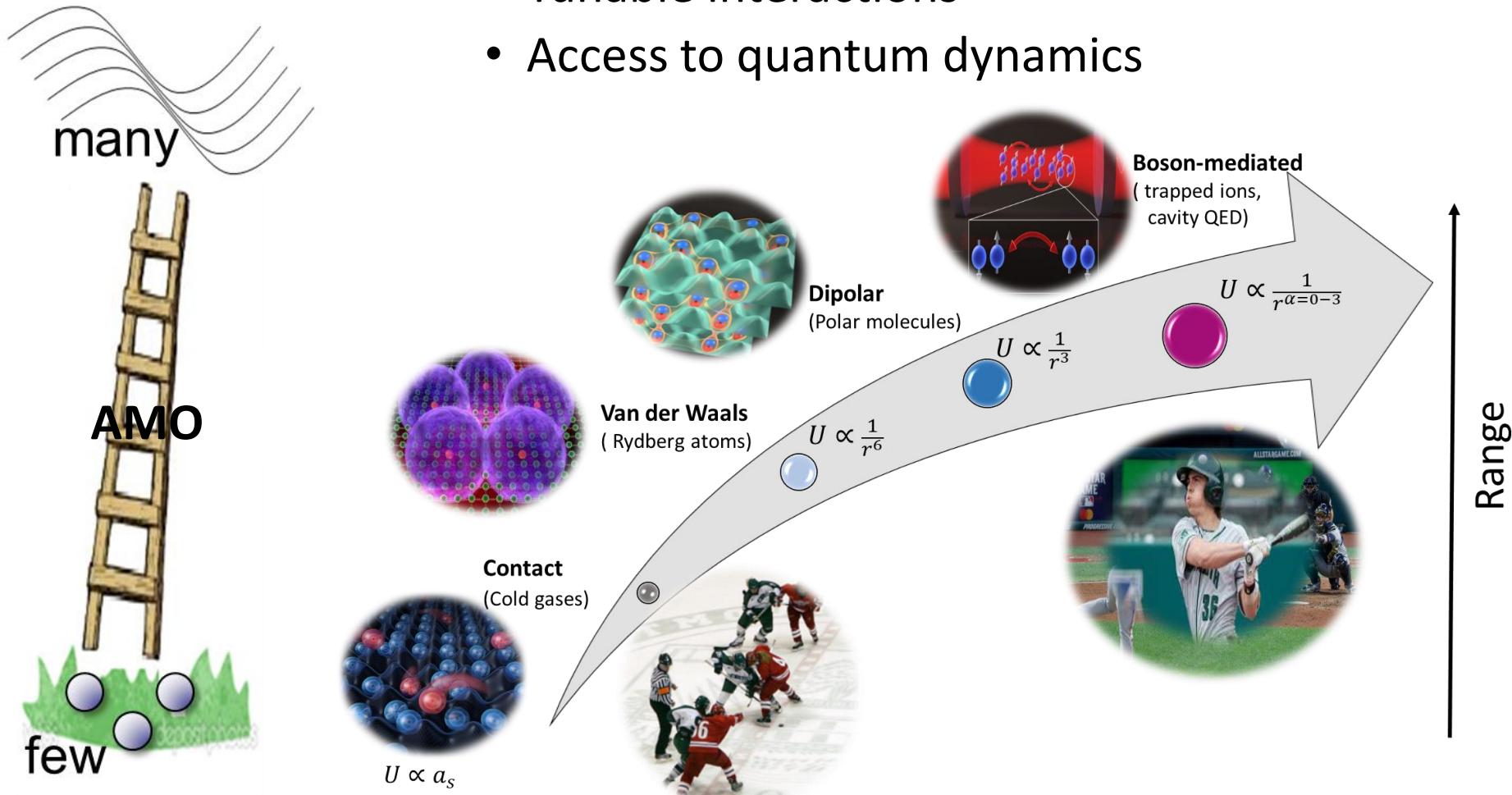
PRL 105, 020401 (2010)

PRL 106, 240801 (2011)

Scientific Vision

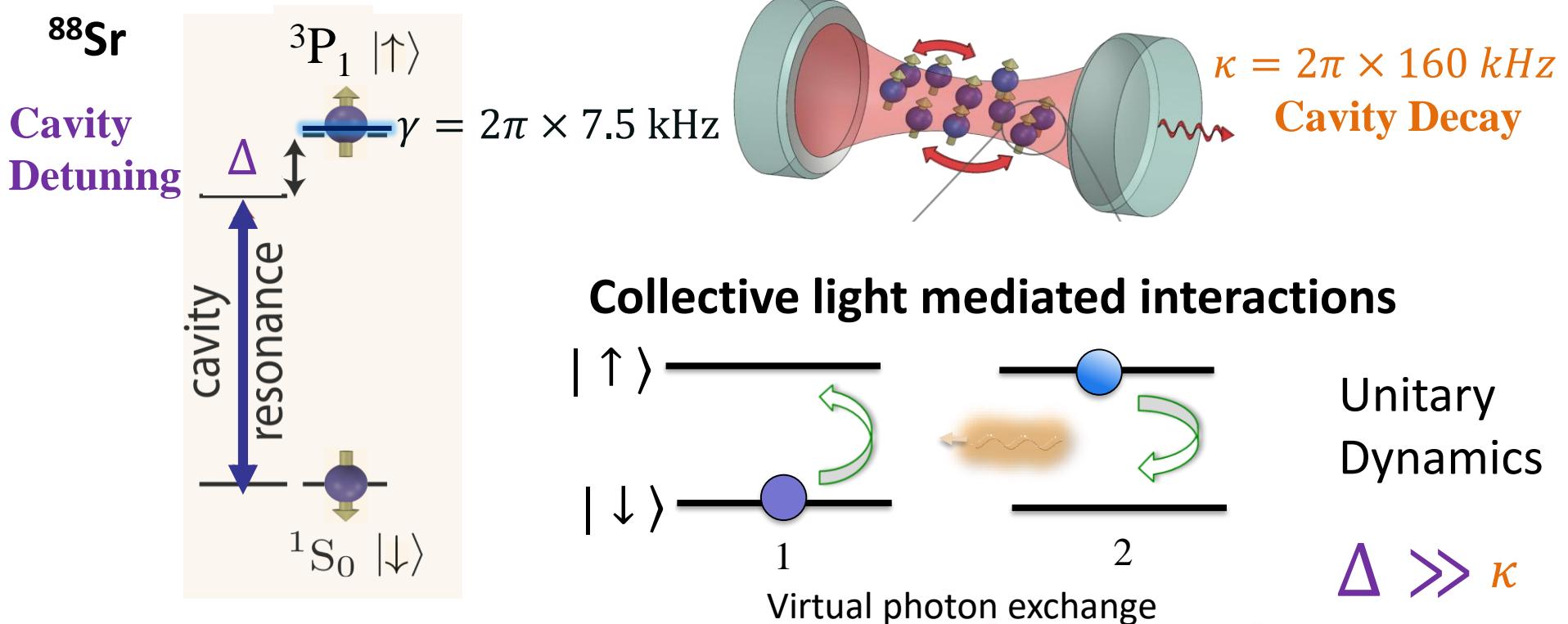
GOAL: Harnessing many-body quantum systems and using them for applications ranging from quantum information to metrology.

- Well-understood microscopics
- Tunable interactions
- Access to quantum dynamics



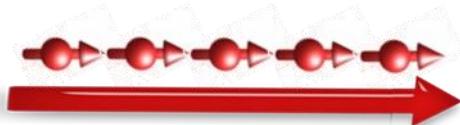
Sr : New regime in Cavity QED

J. A. Muniz *et al*, A. M. Rey and J.K. Thompson Nature 580, 602 (2020)



$$\hat{J}^{x,y,z} = \frac{1}{2} \sum_i \hat{\sigma}_i^{x,y,z}$$

Collective spin



$$\hat{H} = \chi \hat{J}^+ \hat{J}^-$$

$$\chi \propto \frac{g^2}{\Delta}$$

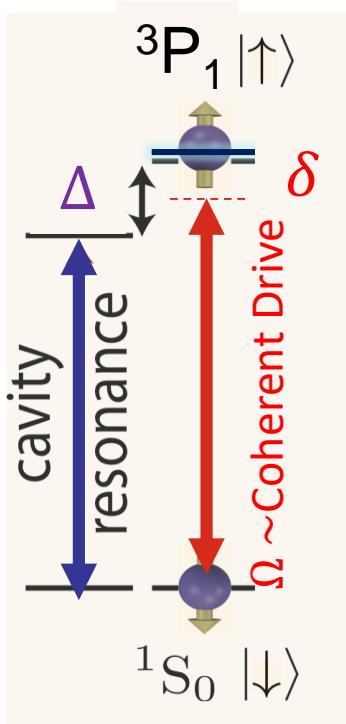
~~$$\mathcal{L}_{\text{spin}} = \sqrt{\Gamma} \hat{J}^-$$~~

$$\frac{\Gamma}{\chi} \propto \frac{\kappa}{\Delta}$$

Dynamical Phase Transition (DPT)

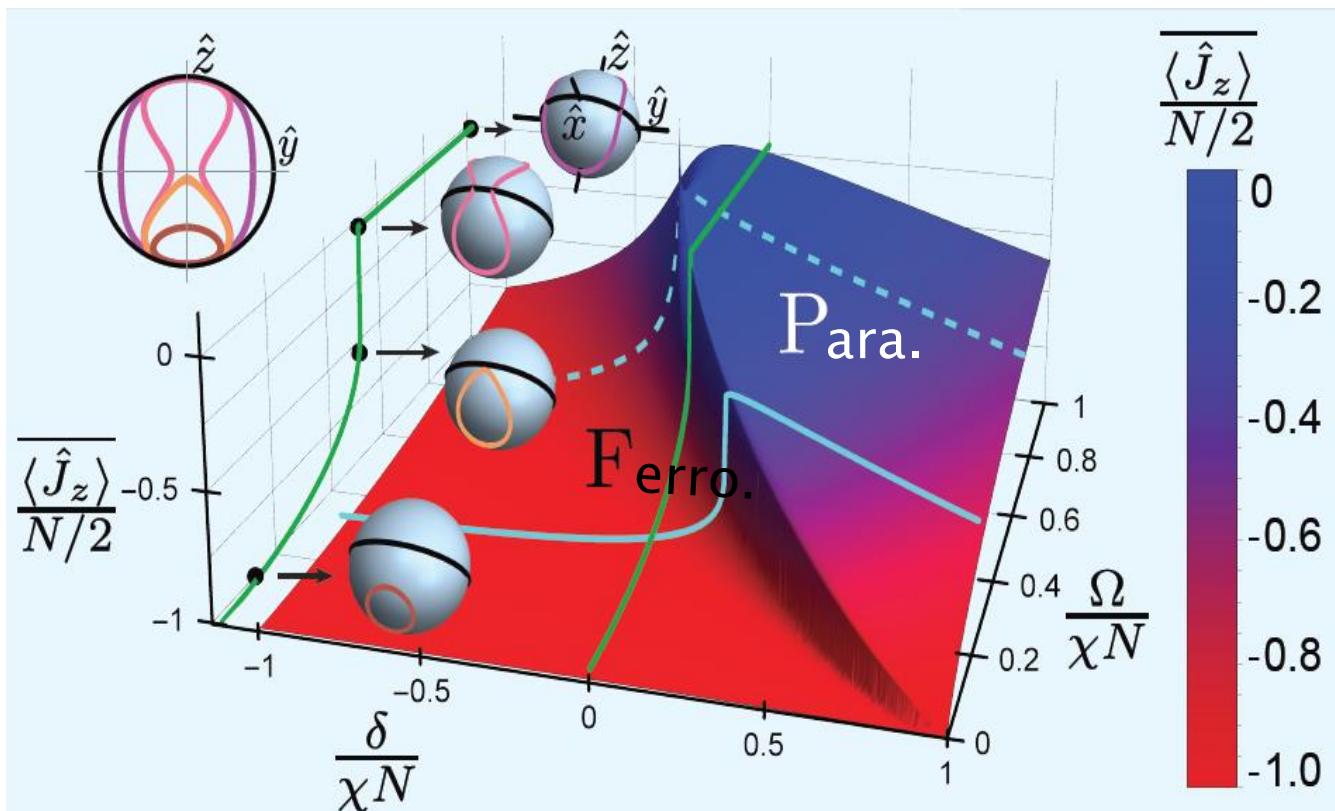
J.A. Muniz, ..., A.M. Rey, J.K. Thompson, Nature 580, 602 (2020)

$$\hat{H} = -\chi \hat{J}^+ \hat{J}^- + \Omega \hat{J}_x + \delta \hat{J}_z$$



Lipkin-Meshkov-Glick model

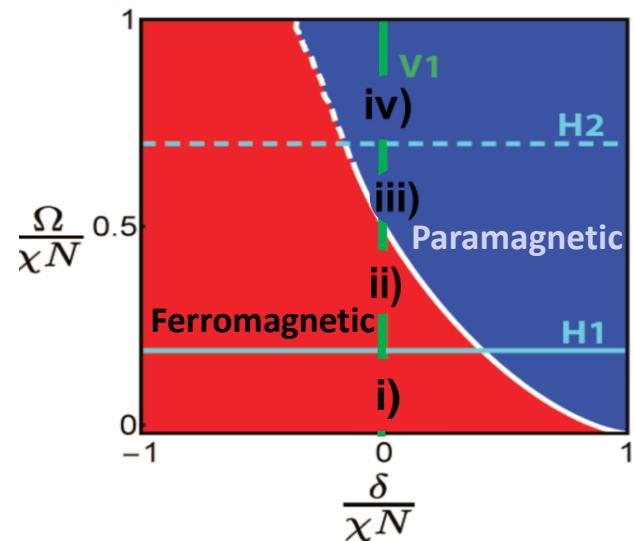
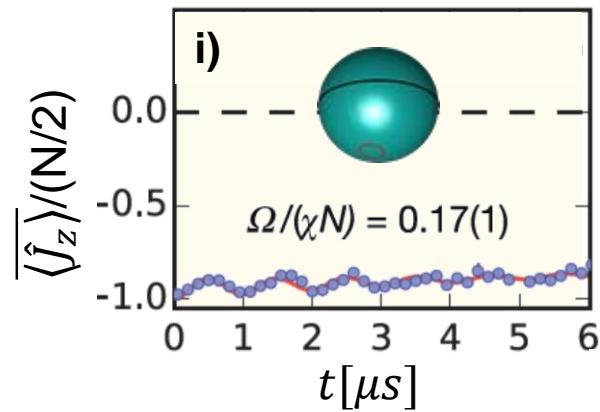
Order Parameter: Time averaged magnetization $\langle \hat{J}_z \rangle$



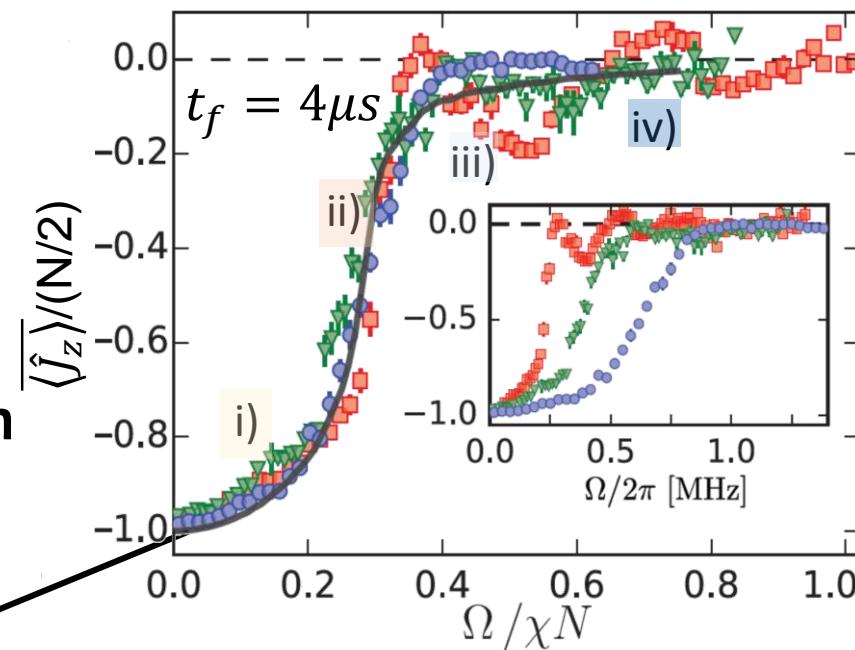
Experimental Observation of DPT: $\delta=0$

Order Parameter: time averaged magnetization $\langle \hat{J}_z \rangle$

Experiment Theory



$$N = (935; 620; 320) \times 10^3$$



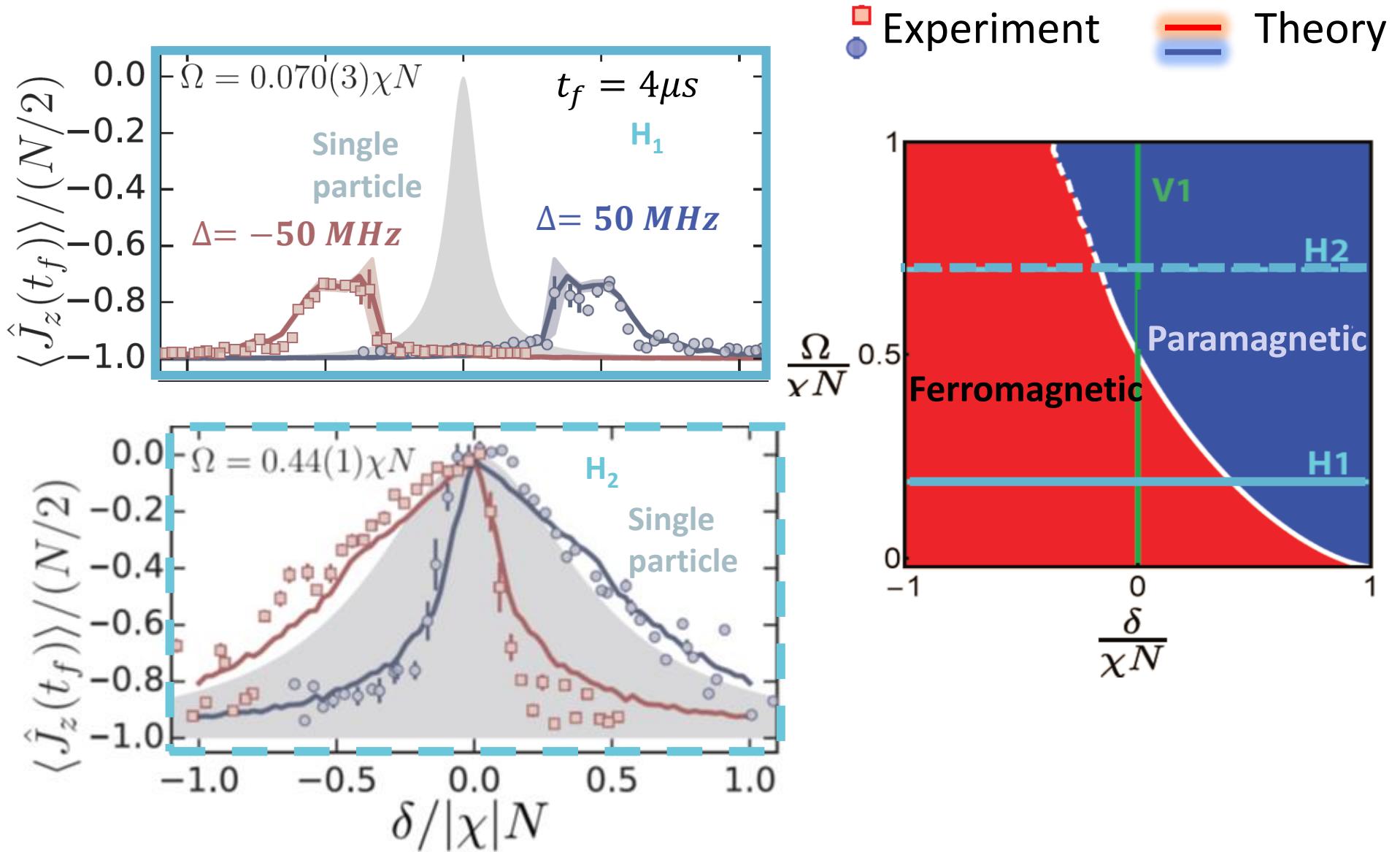
Theoretical calculation

Theory reproduces experiment when accounting for inhomogeneities

N scaling

Experimental Observation of NEPT: $\delta \neq 0$

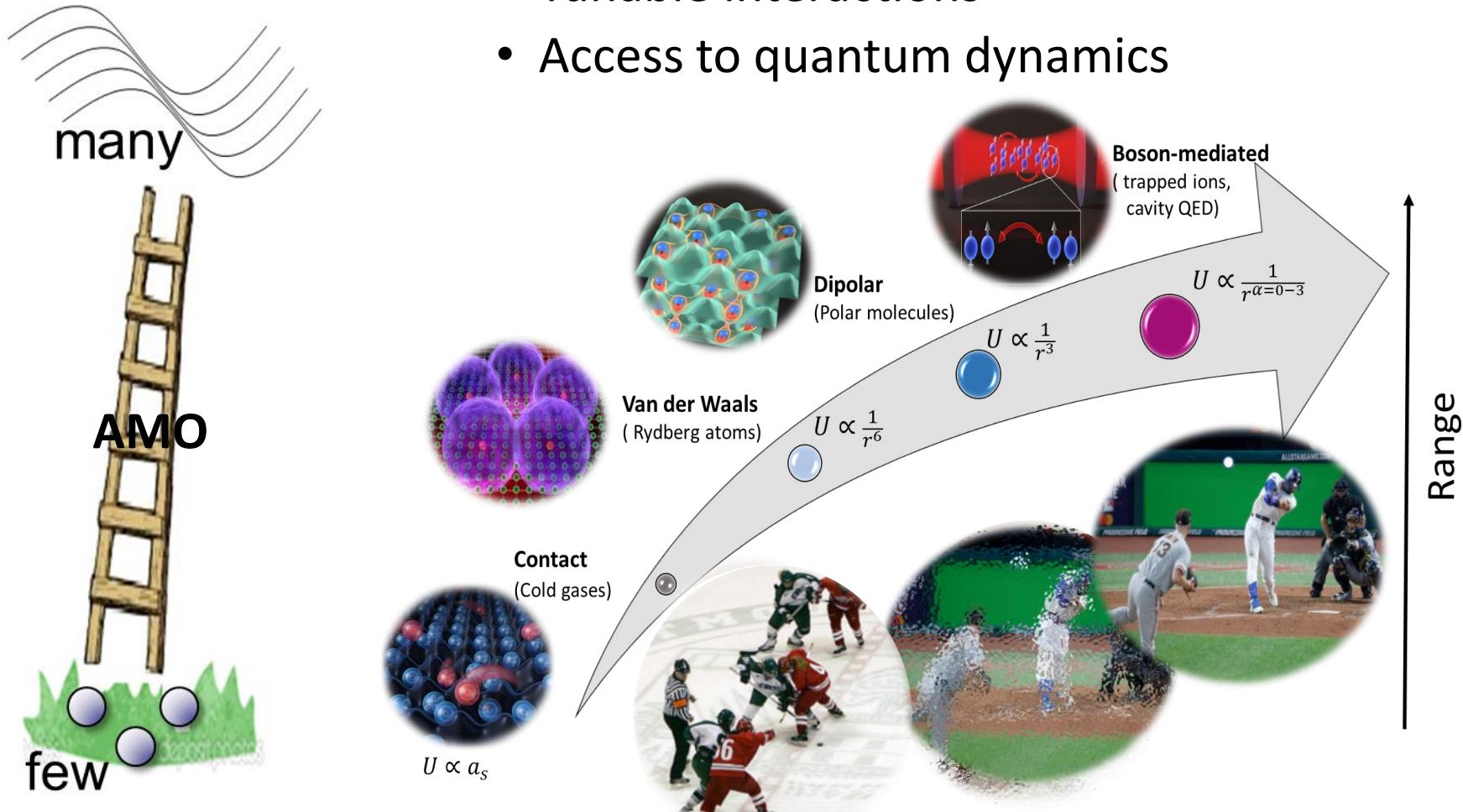
□ Competition of interactions and longitudinal field



Scientific Vision

GOAL: Harnessing many-body quantum AMO systems and using them for applications ranging from quantum information to metrology.

- Well-understood microscopics
- Tunable interactions
- Access to quantum dynamics



Bosonic Spin Model

A. Chu, J. Will, J. Arlt, C. Klempt, and A. M. Rey, arXiv:2004.01282

- ^{87}Rb atomic gases $|\downarrow\rangle \equiv |F = 1, m_F = 0\rangle$ $|\uparrow\rangle \equiv |F = 2, m_F = 0\rangle$

$$H_{\text{int}} = \sum_{ij} J_{ij} \mathbf{S}_i \cdot \mathbf{S}_j + \sum_{ij} \chi_{ij} S_i^z S_j^z + \sum_i B_i S_i^z$$

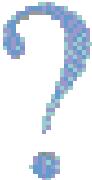
$$\chi_{ij} = \frac{4\pi\hbar^2}{m} (V_{ij}^{\uparrow\uparrow} a_{\uparrow\uparrow} + V_{ij}^{\downarrow\downarrow} a_{\downarrow\downarrow} - V_{ij}^{\uparrow\downarrow} a_{\uparrow\downarrow} - V_{ij}^{\text{ex}} a_{\uparrow\downarrow}) = \frac{4\pi\hbar^2}{m} V_{ij} (a_{\uparrow\uparrow} + a_{\downarrow\downarrow} - 2a_{\uparrow\downarrow})$$

$$J_{ij} = \frac{4\pi\hbar^2}{m} V_{ij}^{\text{ex}} a_{\uparrow\downarrow} \quad \phi_i^{\uparrow}(\mathbf{R}) = \phi_i^{\downarrow}(\mathbf{R})$$

$$V_{ij}^{\text{ex}} = \int d^3\mathbf{R} \phi_i^{\uparrow}(\mathbf{R}) \phi_i^{\downarrow}(\mathbf{R}) \phi_j^{\uparrow}(\mathbf{R}) \phi_j^{\downarrow}(\mathbf{R}) \quad V_{ij}^{\sigma\sigma'} = \int d^3\mathbf{R} [\phi_i^{\sigma}(\mathbf{R})]^2 [\phi_j^{\sigma'}(\mathbf{R})]^2$$

Can we make χ_{ij} non-zero

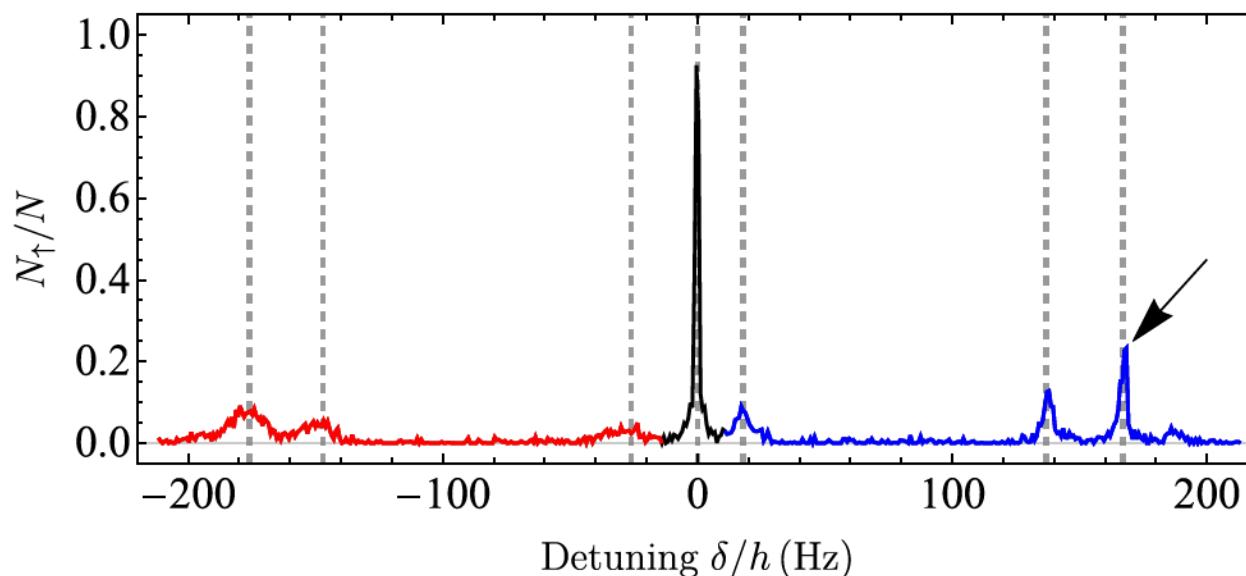
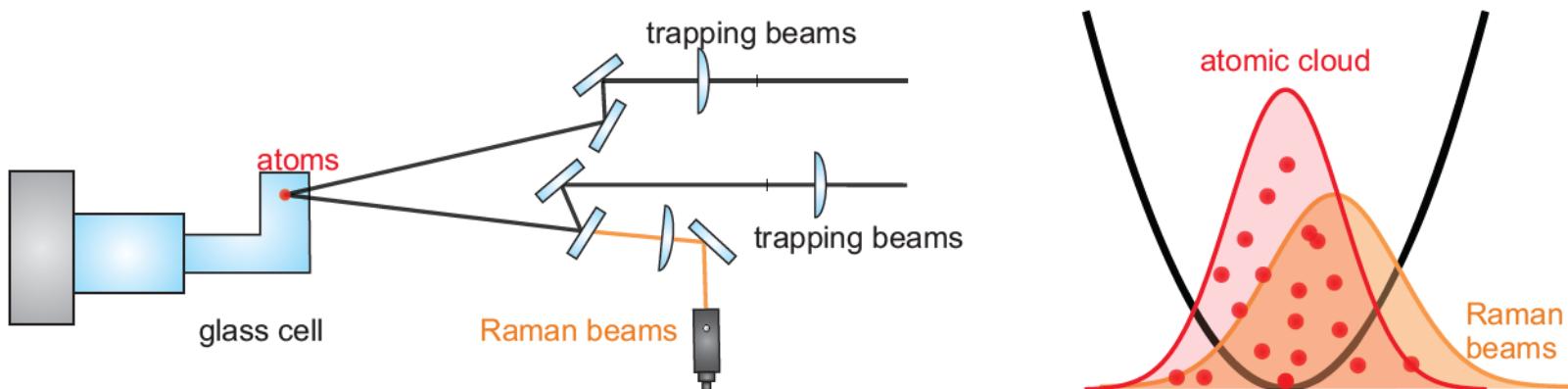
$$\phi_i^{\uparrow}(\mathbf{R}) \neq \phi_i^{\downarrow}(\mathbf{R})$$



^{87}Rb Experimental Set-up

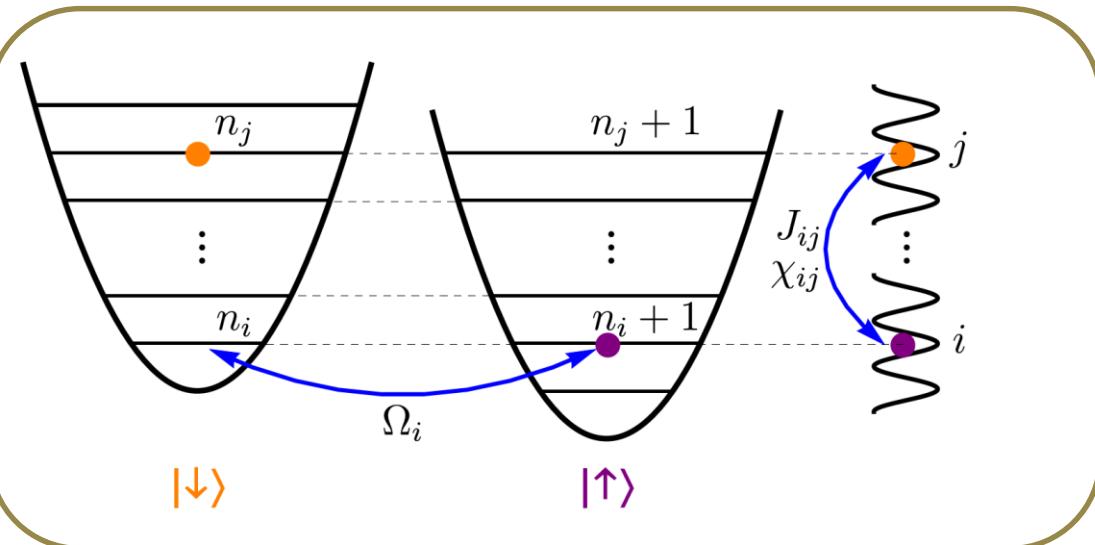
A. Chu, J. Will, J. Arlt, C. Klempt, and A. M. Rey, arXiv:2004.01282

- ^{87}Rb atomic gases $|\downarrow\rangle \equiv |F = 1, m_F = 0\rangle$ $|\uparrow\rangle \equiv |F = 2, m_F = 0\rangle$
Main Idea: Use a sideband



⁸⁷Rb Experimental Set-up

A. Chu, J. Will, J. Arlt, C. Klempt, and A. M. Rey, arXiv:2004.01282



- Blue sideband transition

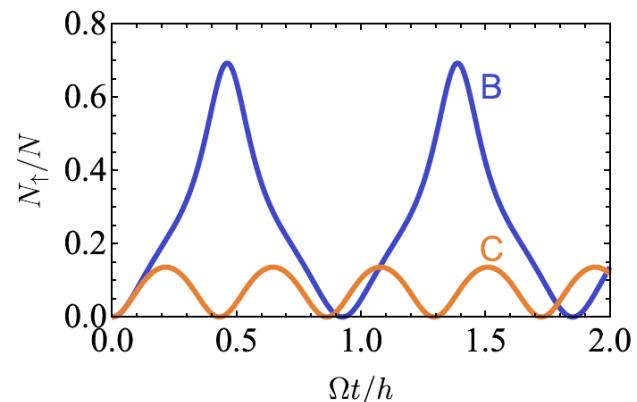
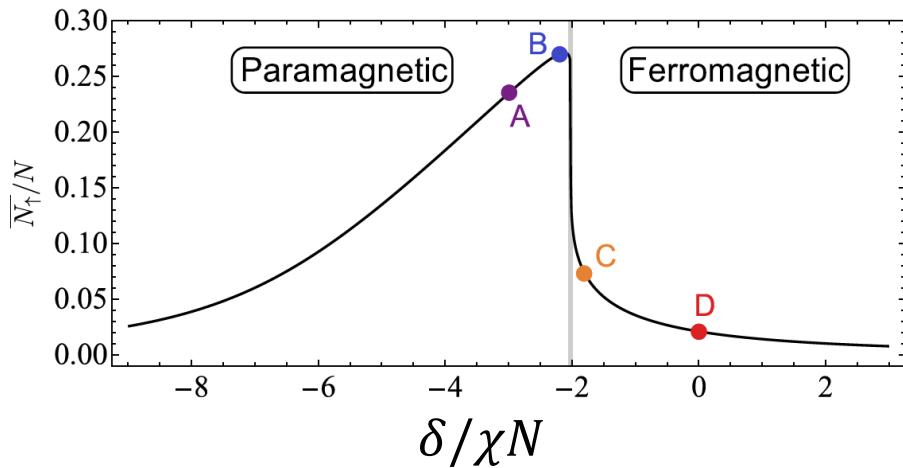
$$|\uparrow_i\rangle = |\uparrow; n_i^X, n_i^Y, n_i^Z + 1\rangle$$

$$|\downarrow_i\rangle = |\downarrow; n_i^X, n_i^Y, n_i^Z\rangle$$



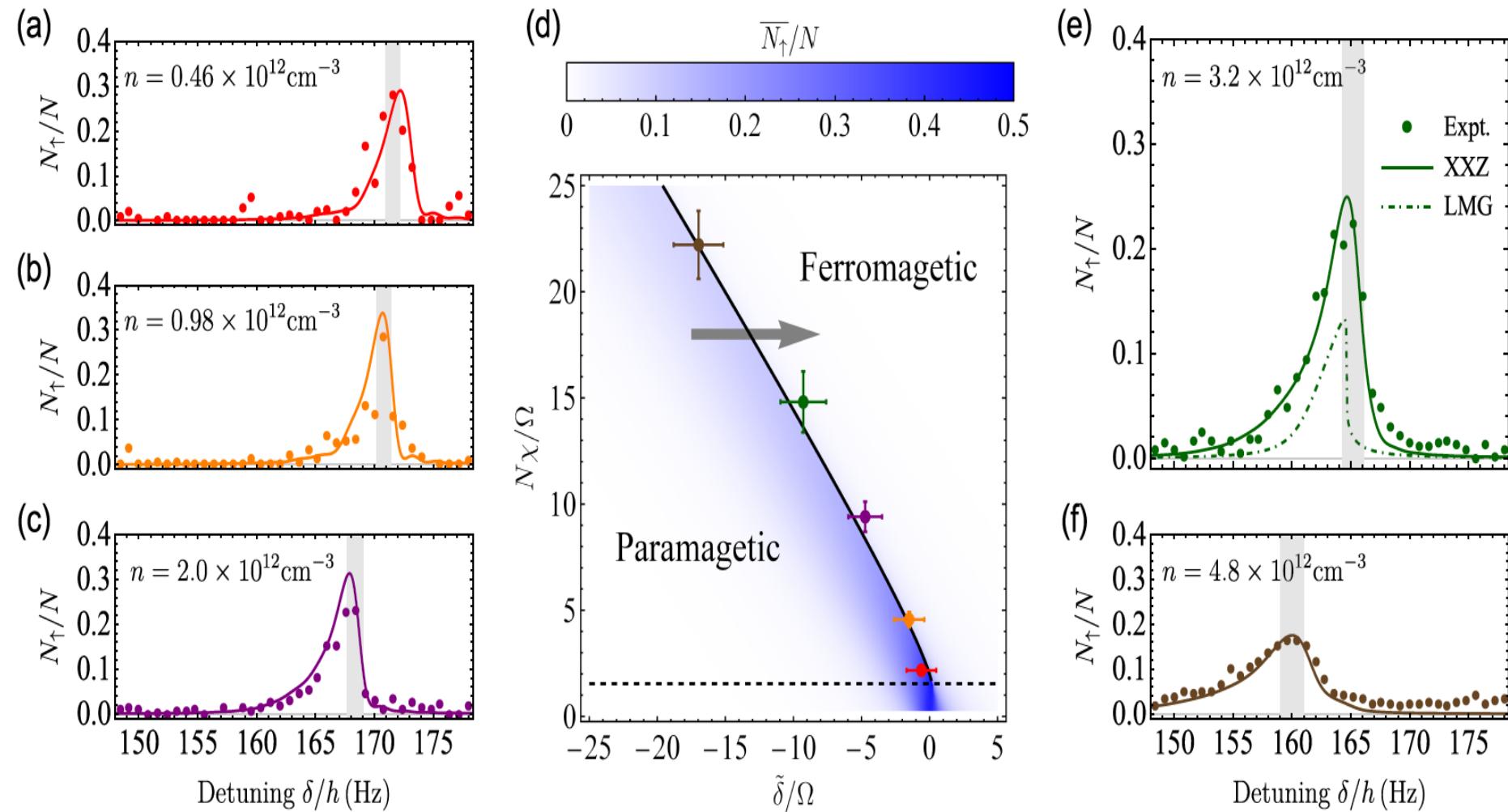
Lipkin-Meshkov-Glick model: Like in the cavity → Coherent Raman drive

$$\hat{H} = -\vec{J}\vec{S} \cdot \vec{S} + \chi(\hat{S}^z)^2 + \Omega \hat{S}_x + \delta S_z$$

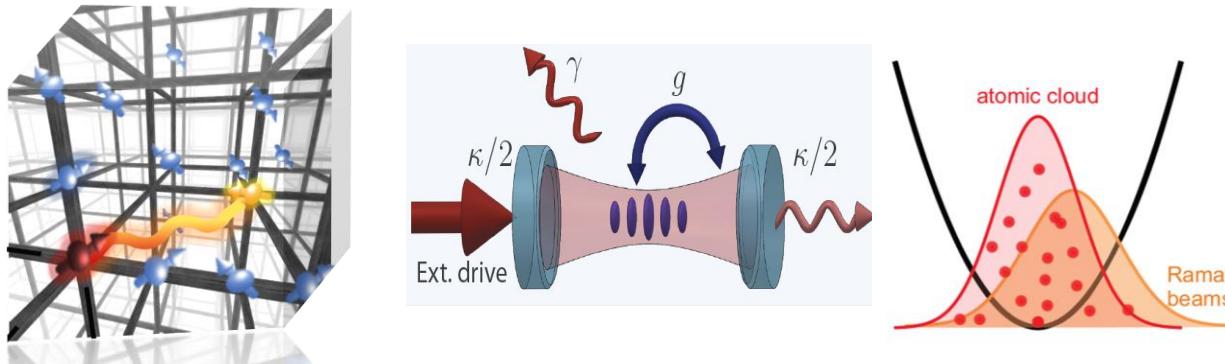


^{87}Rb Experimental DPT

A. Chu, J. Will, J. Arlt, C. Klempt, and A. M. Rey, arXiv:2004.01282



Dynamical Phase Transitions



Toronto, Sci. Adv (2019) JILA, Nature (2020)

- Dynamical: Not found by minimization of free energy
- New symmetries
- Robust generation of useful entangled states

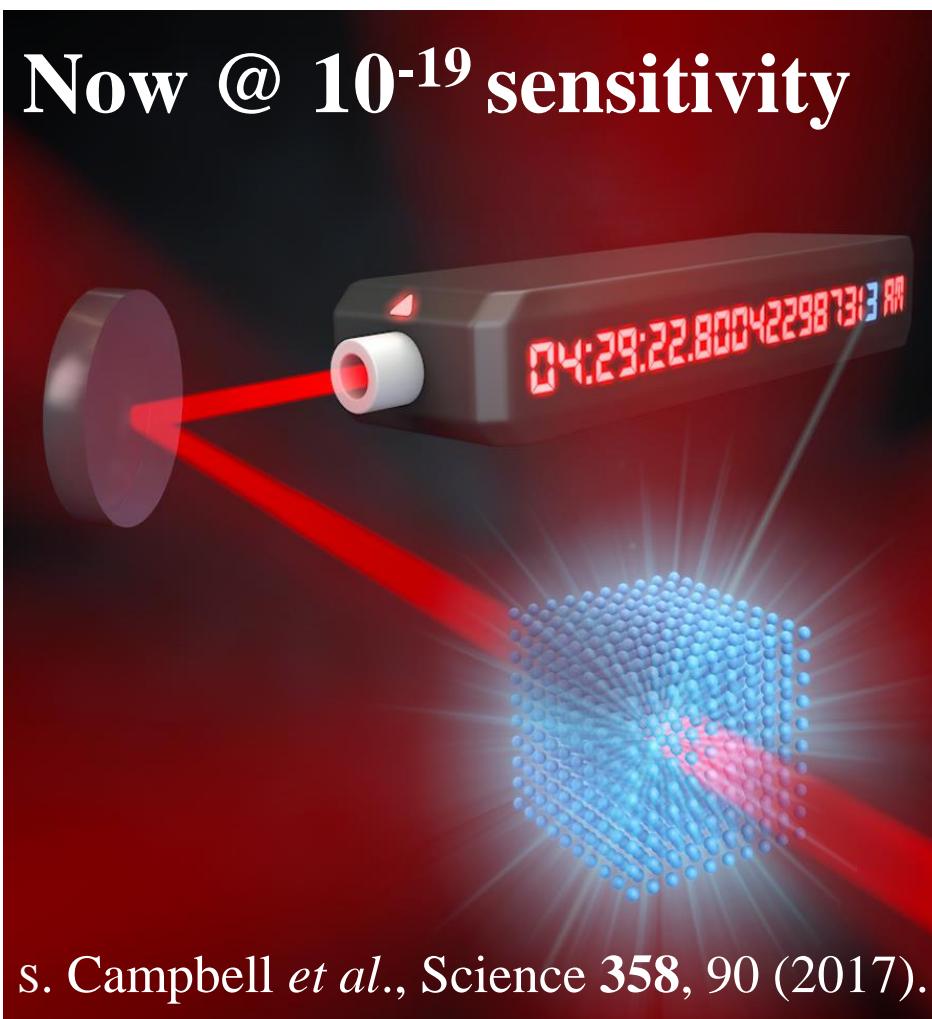


So far everything has admitted a mean field description

Time evolution restricted to relatively short times

New generation of atomic clocks: 3D ultra-cold fermionic lattice clock

Scaling up the Sr quantum clock: 3D lattice



- High accuracy at highest density
- All degrees of freedom at the quantum level

$N \sim 10^4$ atoms below 80 nK,
 $T/T_F \sim 0.1$

- Now 12s quantum coherence (Record for quantum coherence in 3D lattices).

Quantum Physics with Ultra-Cold Atoms

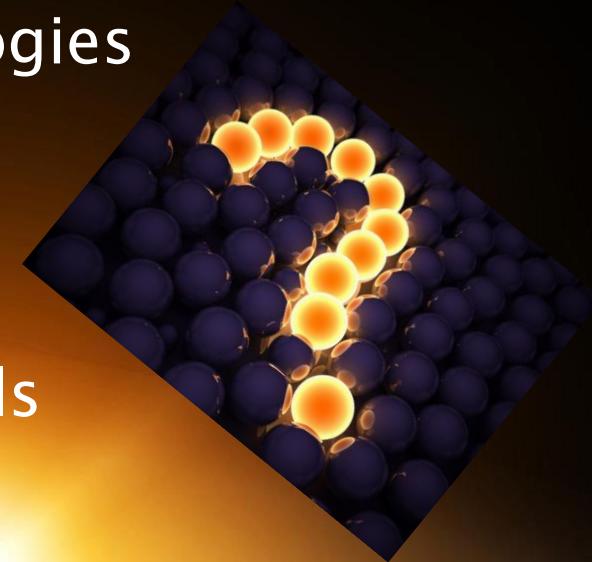
Only the beginning: Bright vista ahead

Quantum computers

Quantum
simulators

Quantum
technologies

Synthetic materials



Thank YOU!

