

Colour Centers for Quantum Technologies

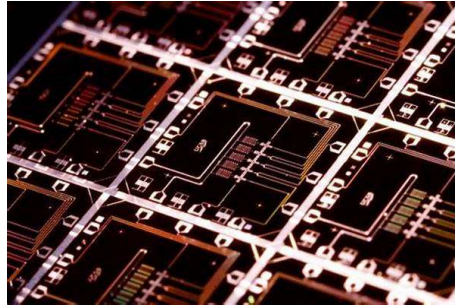
Martin B Plenio

**Institute of Theoretical Physics
&
Center for Quantum-BioSciences
Ulm University**



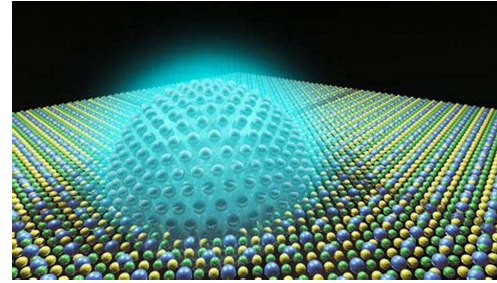
Qubits

Superconductors



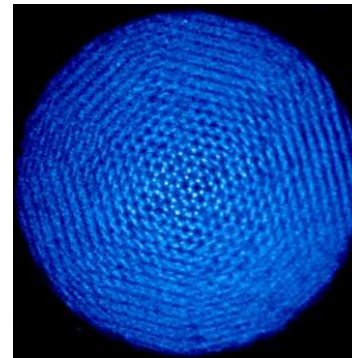
Martinis @ UCSB

Quantum Dots



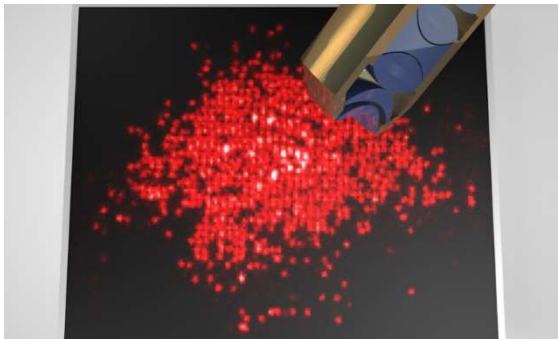
JQI Maryland

2-D Trapped Ion Coulomb Crystal



John Bollinger @ NIST

2-D Neutral Atom Optical Lattice



Immanuel Bloch @ MPQ Garching

Quantum Hardware Shop



Quantum Hardware Shop

A perfect diamond is transparent !



Photo taken at Sotheby's London October 2016

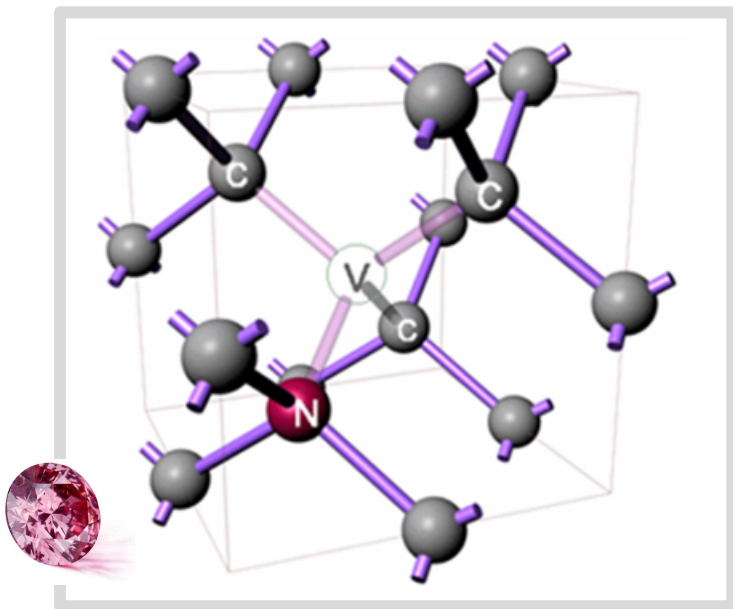


Some diamonds have colour

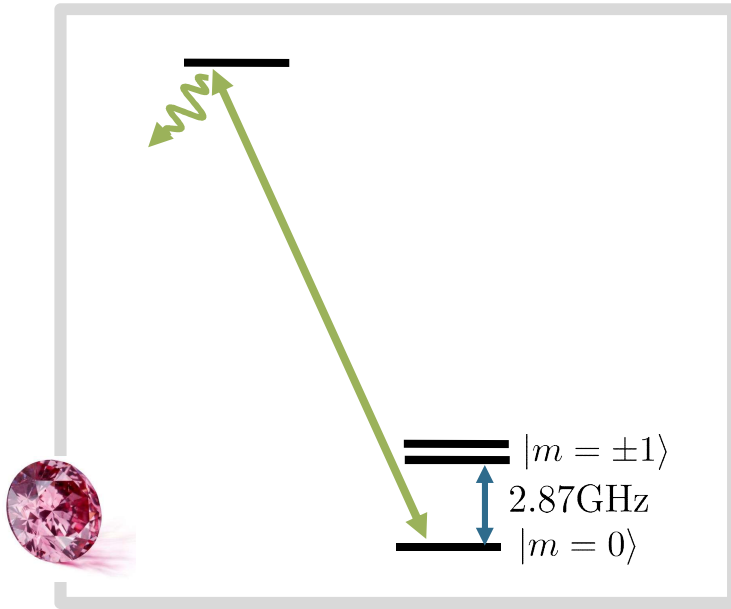
Principles



Principles



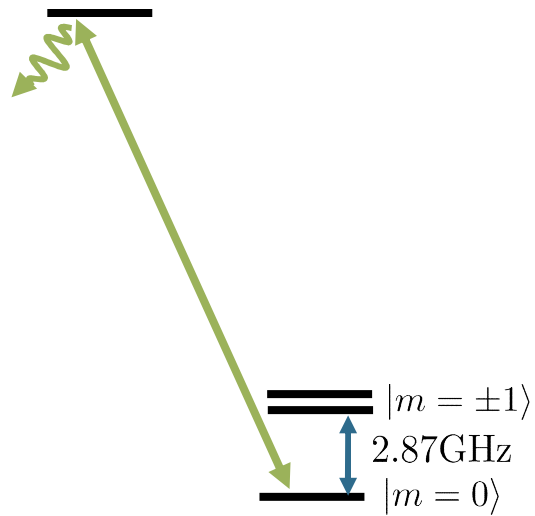
Principles



Optically Detected Magnetic Resonance

- Fast state initialisation
- Optical readout by state dependent fluorescence

Principles



Nuclear Spin

Optically Detected Magnetic Resonance

- Fast state initialisation
- Phase induced by magnetic signal
- Optical readout by state dependent fluorescence

Principles

The Electronic Spin Hamiltonian

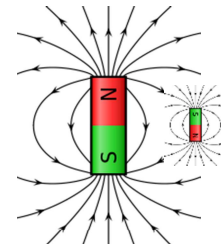
$$\begin{aligned}
 \hat{V}_{gs} = & \boxed{\mu_B g_{gs}^{\parallel} \hat{S}_z B_z + \mu_B g_{gs}^{\perp} (\hat{S}_x B_x + \hat{S}_y B_y)} + \mu_N g_N \vec{I} \cdot \vec{B} + \boxed{D(T) S_z^2} \\
 & + d_{gs}^{\parallel} \boxed{E_z + \delta_z} \left[\hat{S}_z^2 - S(S+1)/3 \right] + d_{gs}^{\perp} \boxed{E_x + \delta_x} (\hat{S}_y^2 - \hat{S}_x^2) + d_{gs}^{\perp} \boxed{E_y + \delta_y} (\hat{S}_x \hat{S}_y + \hat{S}_y \hat{S}_x)
 \end{aligned}$$

Magnetic Field
 Temperature
 Strain
 Electric Field

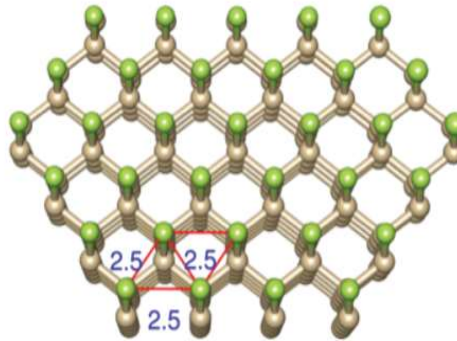
Roadmap

Diamond Quantum Devices for Simulation and Imaging

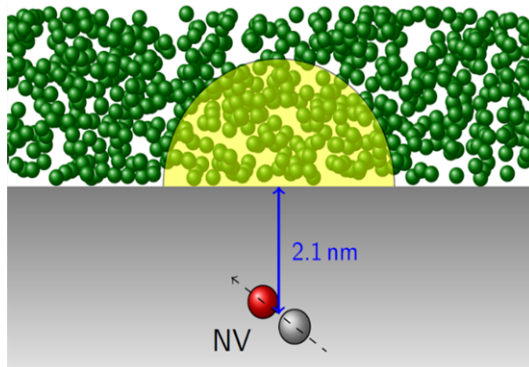
Electrons and Nuclei



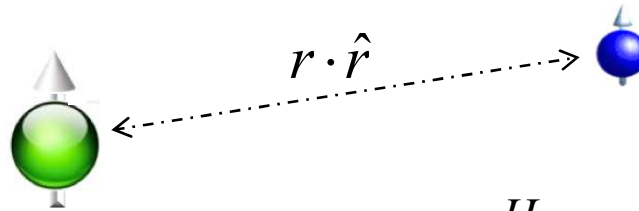
Quantum Simulation



Nanoscale NMR



Coupling Electron Spins to Nuclei

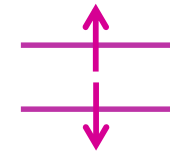


$$H_{NV-S} = gS_z \left[3r_x r_z I_N^x + 3r_y r_z I_N^y + (3r_z^2 - 1) I_N^z \right]$$

$m_s = +1/2$

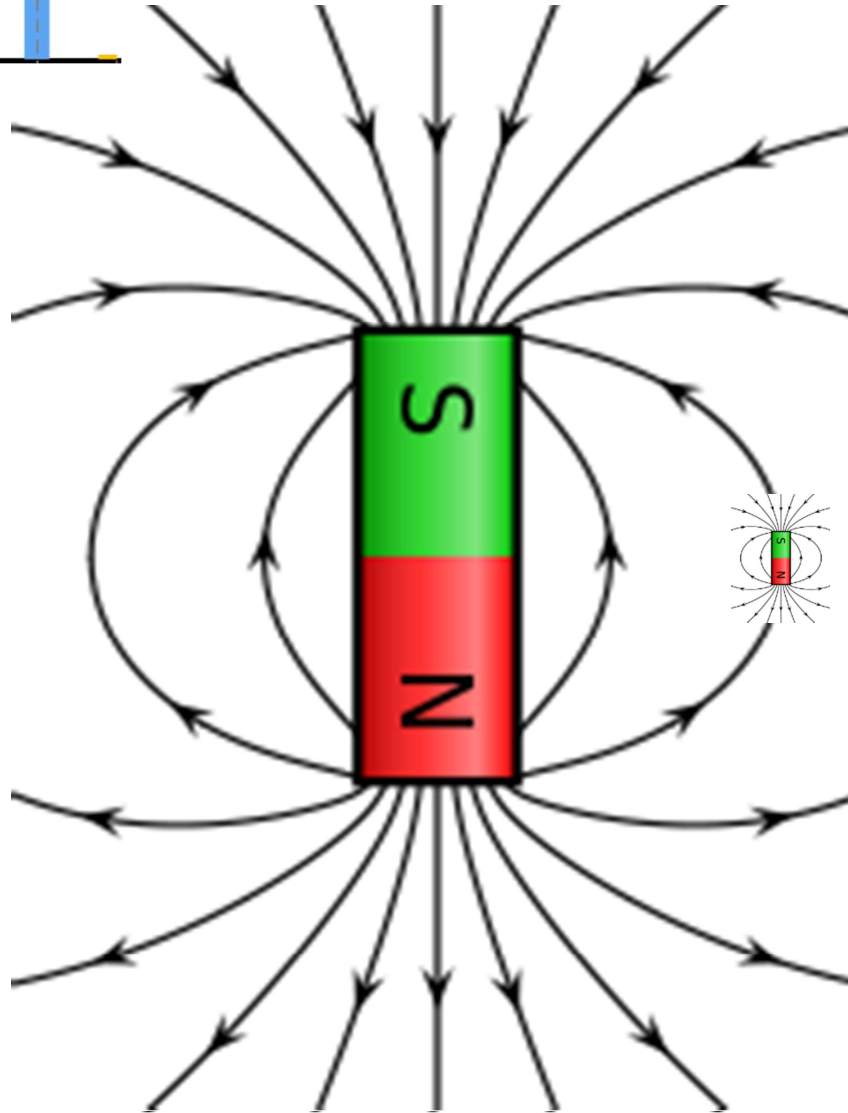
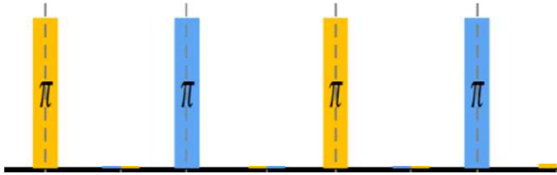
$$H_S = \gamma_E \vec{B} \cdot \vec{S}$$

$$H_S = \gamma_N \vec{B} \cdot \vec{I}_N$$

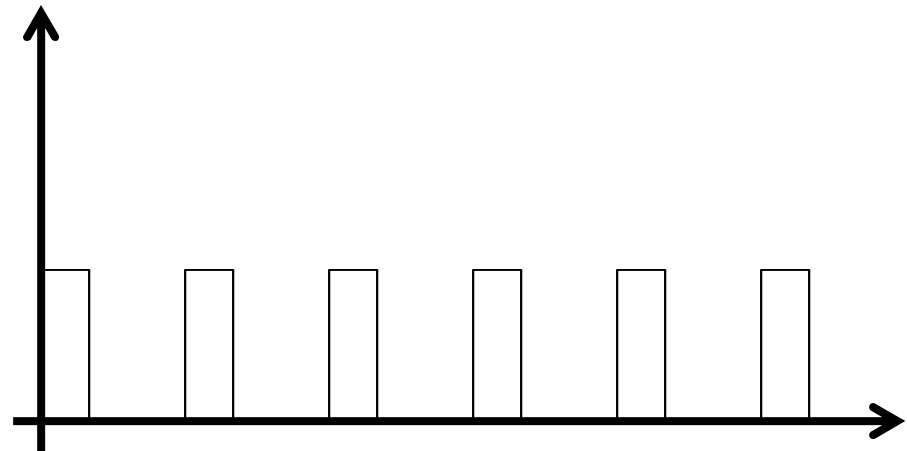
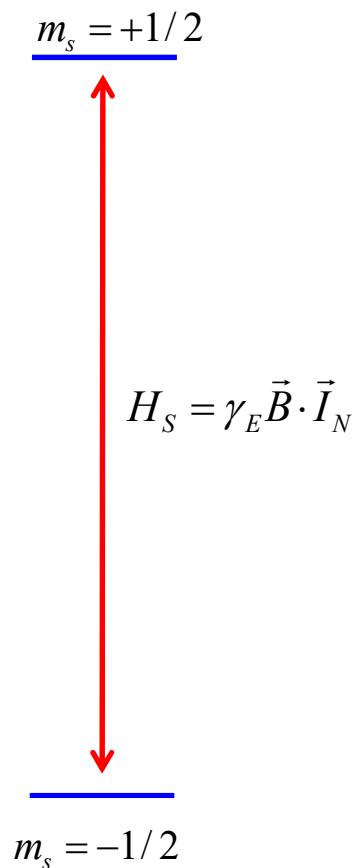
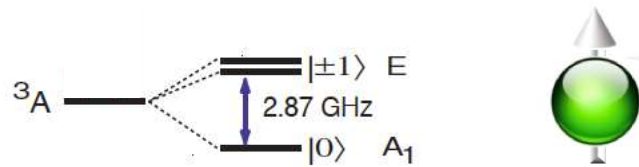


$m_s = -1/2$

Coupling Electron Spins to Nuclei



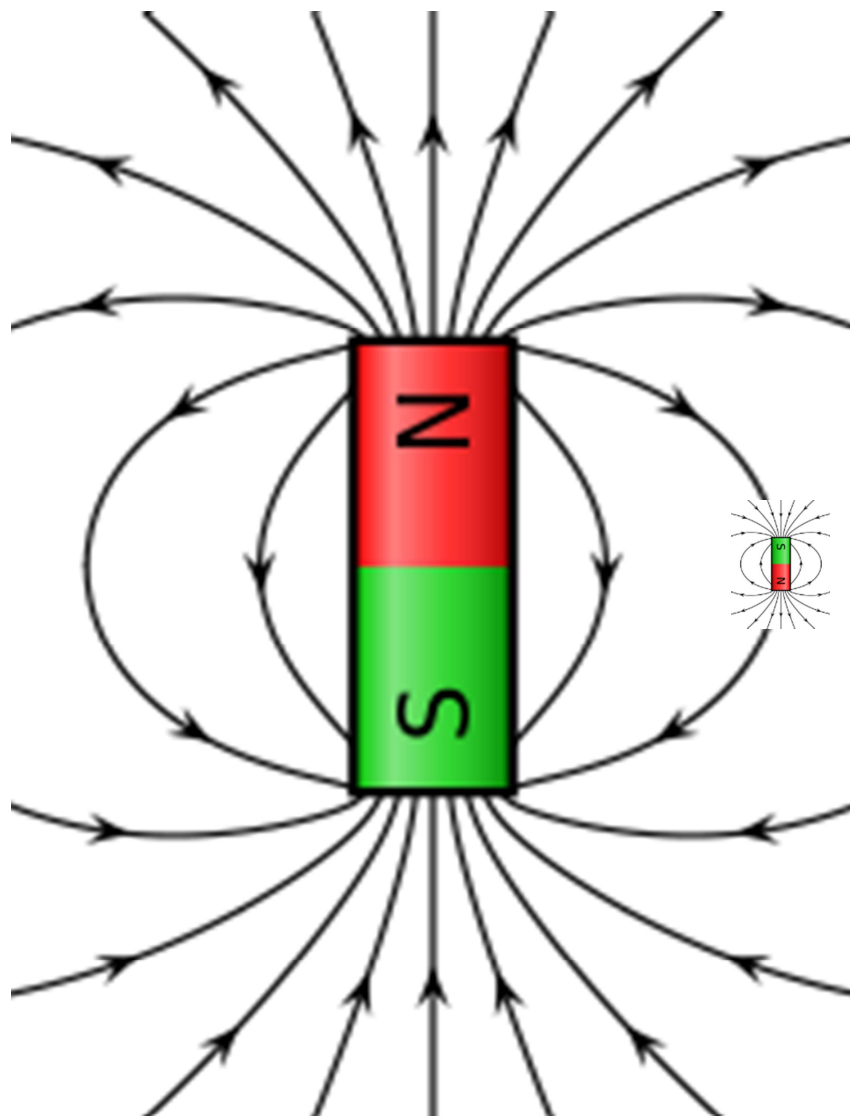
Coupling Electron Spins to Nuclei



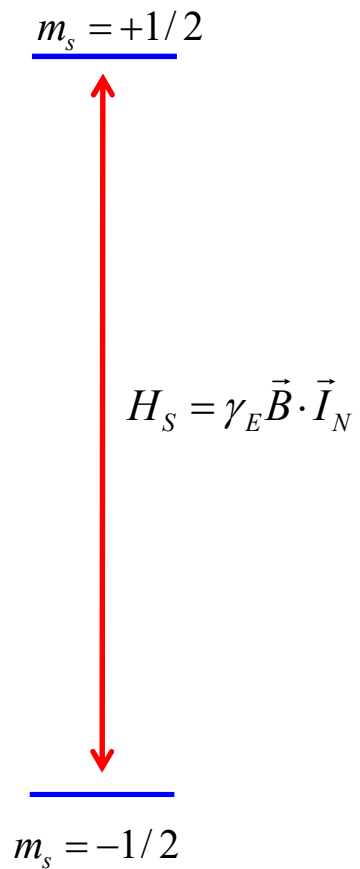
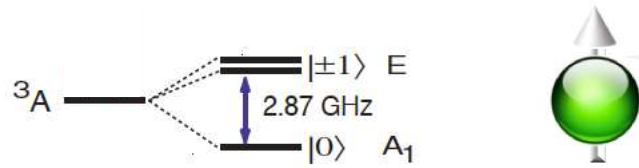
Pulsed decoupling – Induce short π -pulses to flip the electron spin periodically

Coupling Electron Spins to Nuclei

(Spin locking)_y

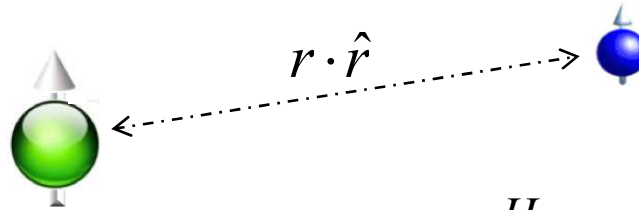


Coupling Electron Spins to Nuclei



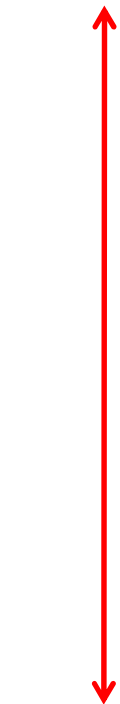
Continuous driving to rotate the electron spin

Coupling Electron Spins to Nuclei



$$H_{NV-S} = gS_z \left[3r_x r_z I_N^x + 3r_y r_z I_N^y + (3r_z^2 - 1) I_N^z \right]$$

$$m_s = +1/2$$



$$m_s = -1/2$$

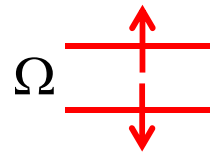
$$H_S = \gamma_E \vec{B} \cdot \vec{S}$$

Continuous
Resonant Drive

Laser

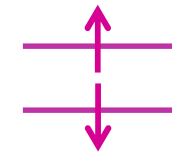
$$H_{NV} = \Omega \sigma_x$$

$$|+\rangle = |-1/2\rangle + |+1/2\rangle$$

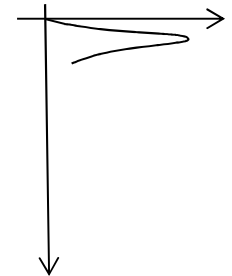


$$|-\rangle = |-1/2\rangle - |+1/2\rangle$$

$$H_S = \gamma_N \vec{B} \cdot \vec{I}_N$$

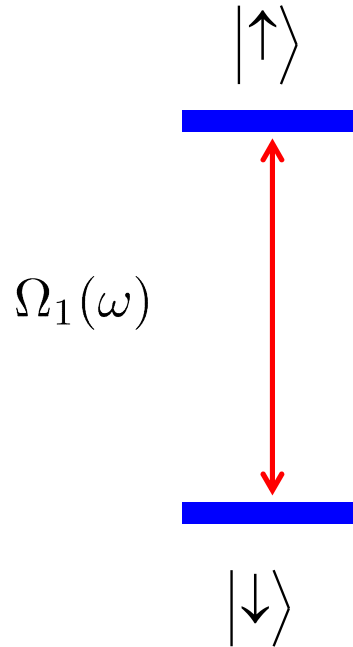


Environment
spectral density



Concatenated Continuous Dynamical Decoupling

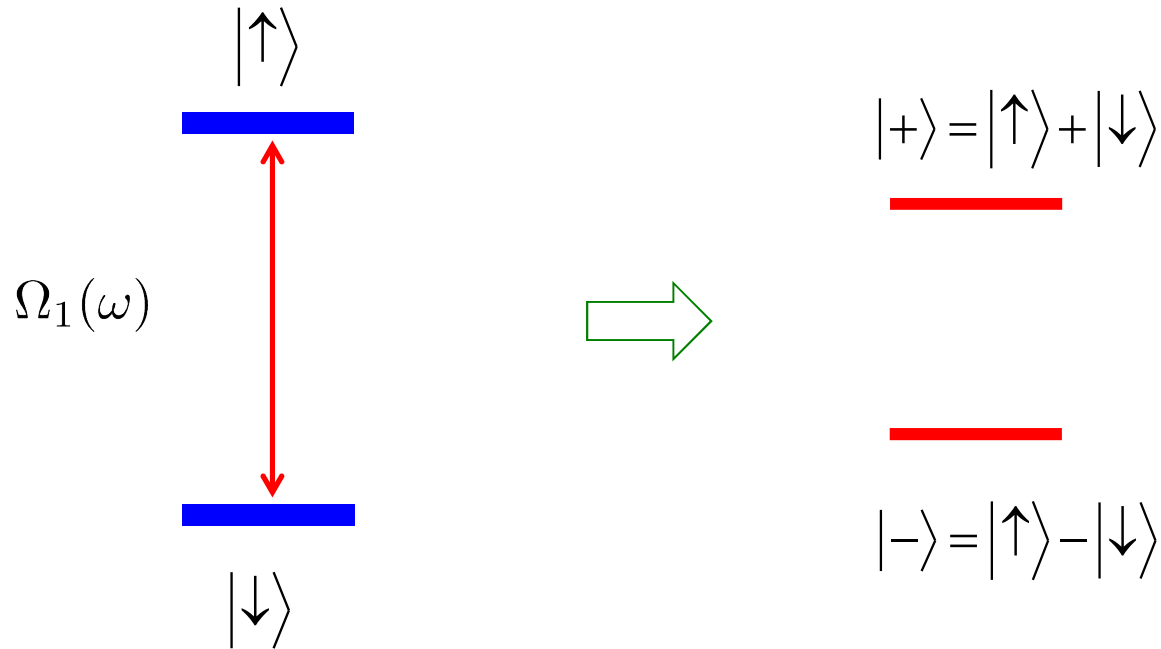
Robustness Against Driving Field Fluctuations



$$H = \hbar\Omega_1 \cos(\omega t)\sigma_x + \frac{\hbar}{2}\omega\sigma_z$$

Concatenated Continuous Dynamical Decoupling

Robustness Against Driving Field Fluctuations

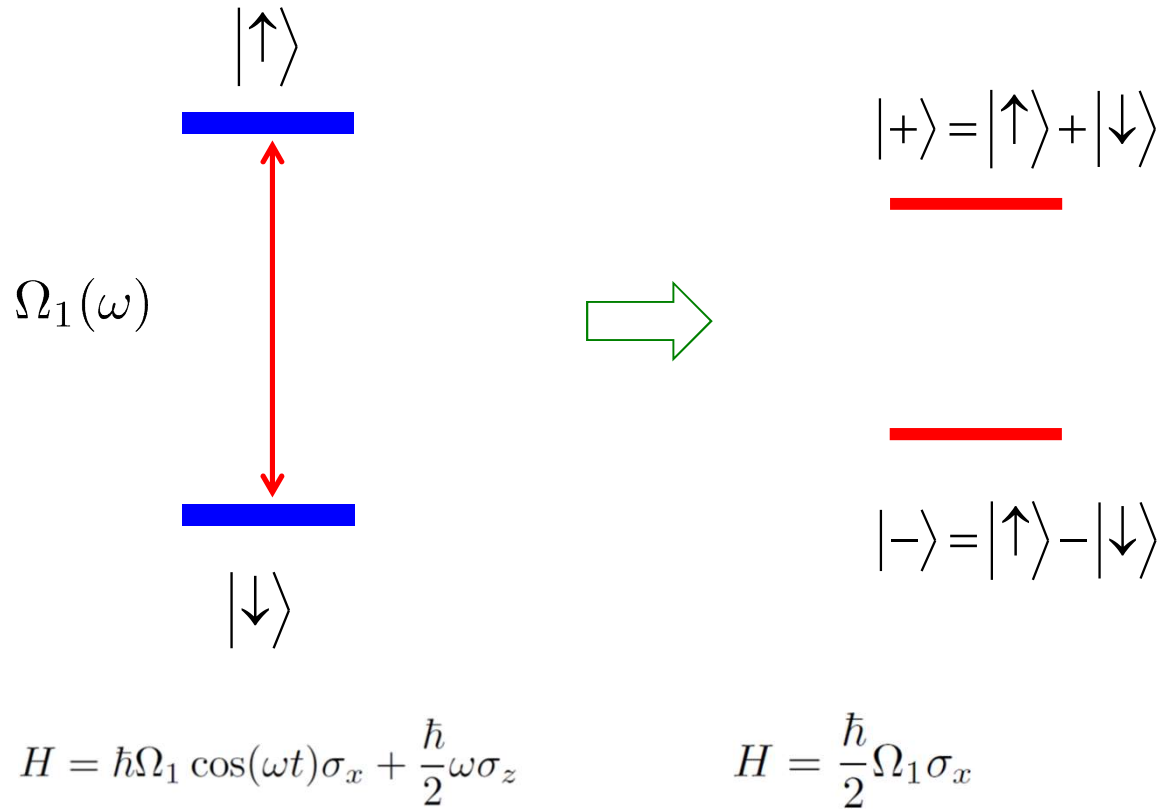


$$H = \hbar\Omega_1 \cos(\omega t)\sigma_x + \frac{\hbar}{2}\omega\sigma_z$$

$$\begin{aligned} H &= \hbar\Omega_1 \cos(\omega t)(\sigma_x \cos(\omega t) + \sigma_y \sin(\omega t)) \\ &\cong \frac{\hbar}{2}\Omega_1\sigma_x \end{aligned}$$

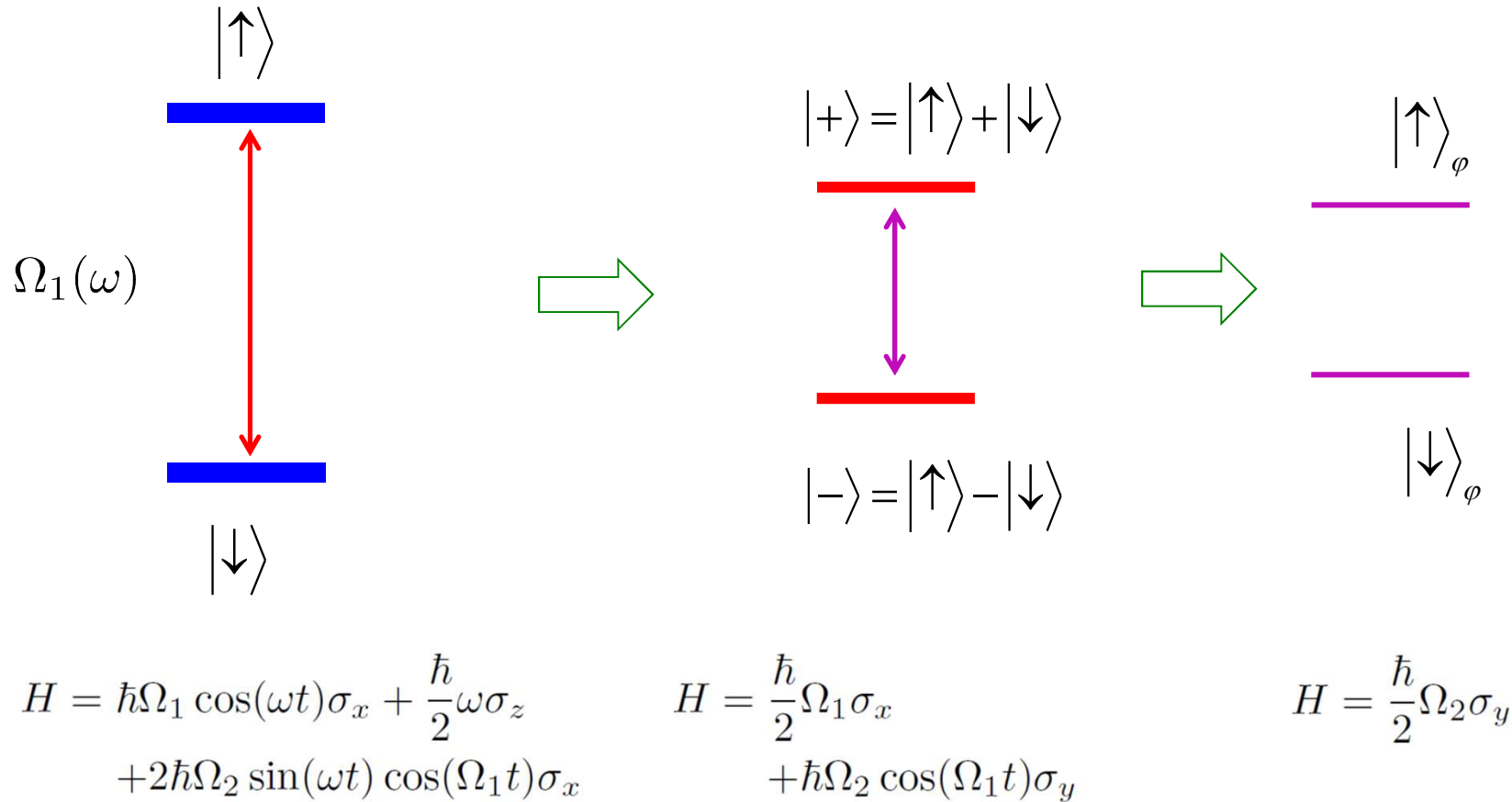
Concatenated Continuous Dynamical Decoupling

Robustness Against Driving Field Fluctuations



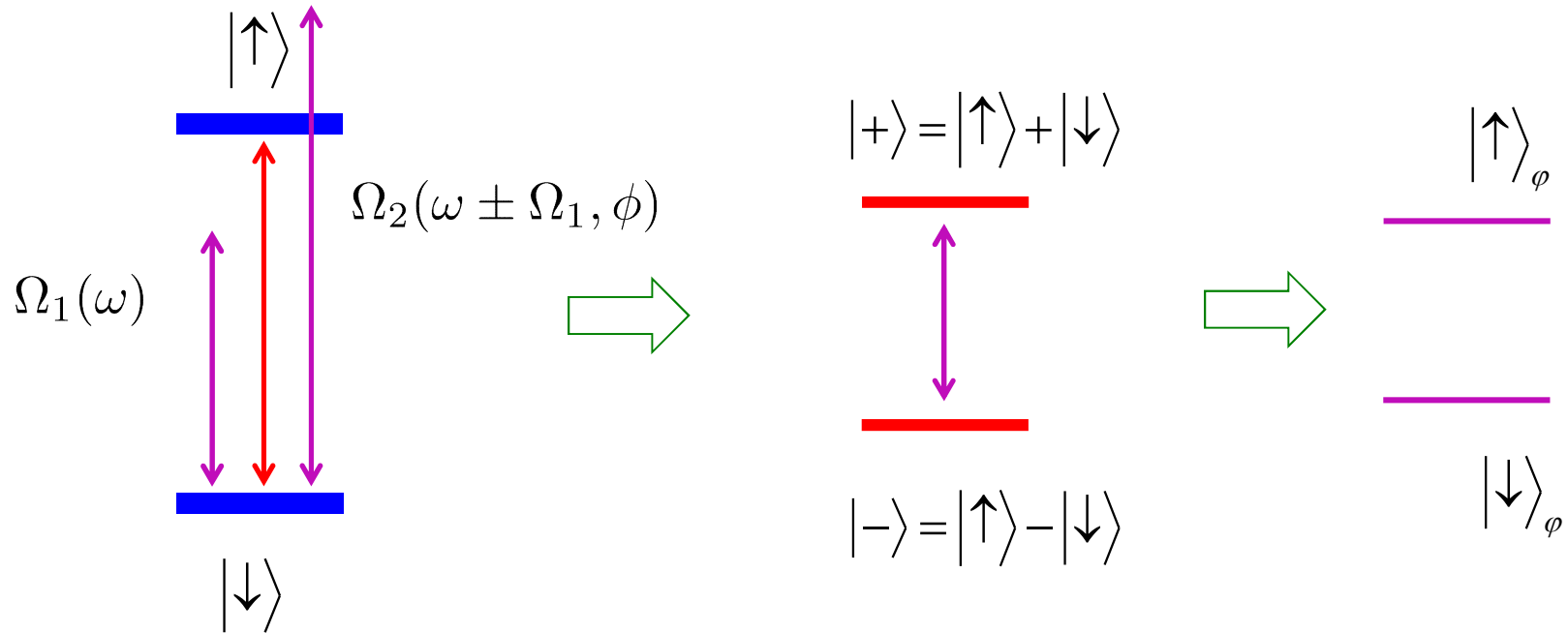
Concatenated Continuous Dynamical Decoupling

Robustness Against Driving Field Fluctuations



Concatenated Continuous Dynamical Decoupling

Robustness Against Driving Field Fluctuations



$$H = \hbar\Omega_1 \cos(\omega t)\sigma_x + \frac{\hbar}{2}\omega\sigma_z + 2\hbar\Omega_2 \sin(\omega t) \cos(\Omega_1 t)\sigma_x$$

$$\cong \hbar\Omega_1 \cos(\omega t + \frac{\Omega_2}{\Omega_1} \cos \Omega_1 t)\sigma_x$$

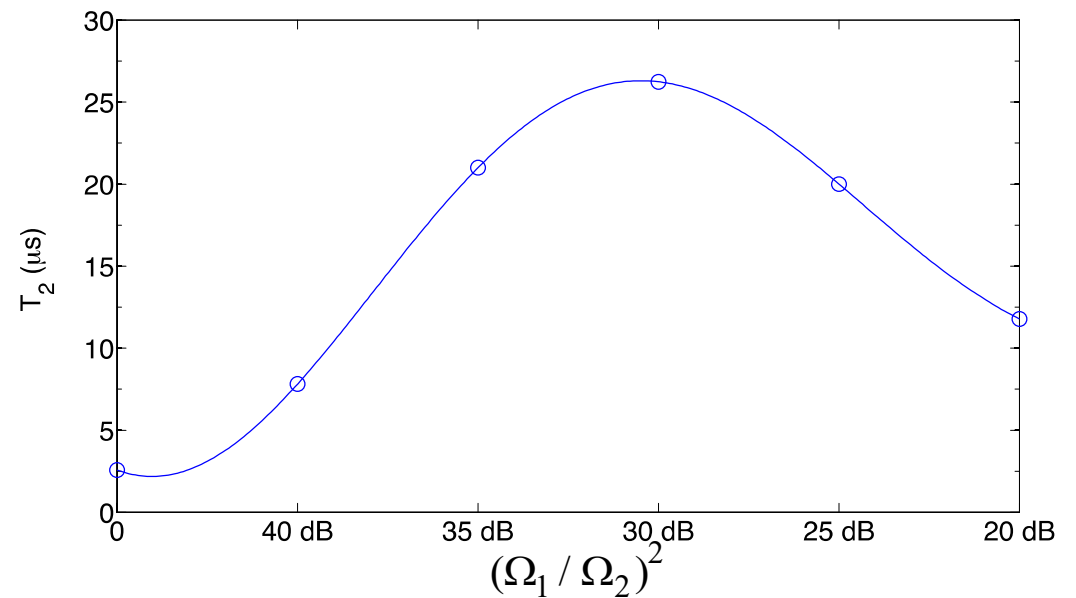
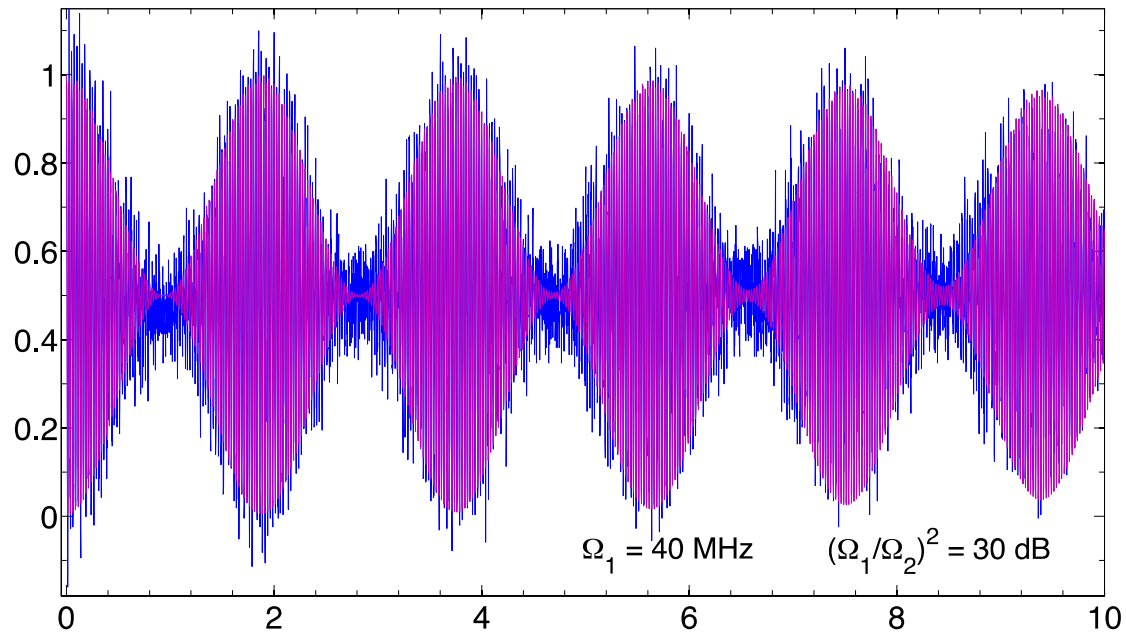
$$H = \frac{\hbar}{2}\Omega_1\sigma_x + \hbar\Omega_2 \cos(\Omega_1 t)\sigma_y$$

$$H = \frac{\hbar}{2}\Omega_2\sigma_y$$

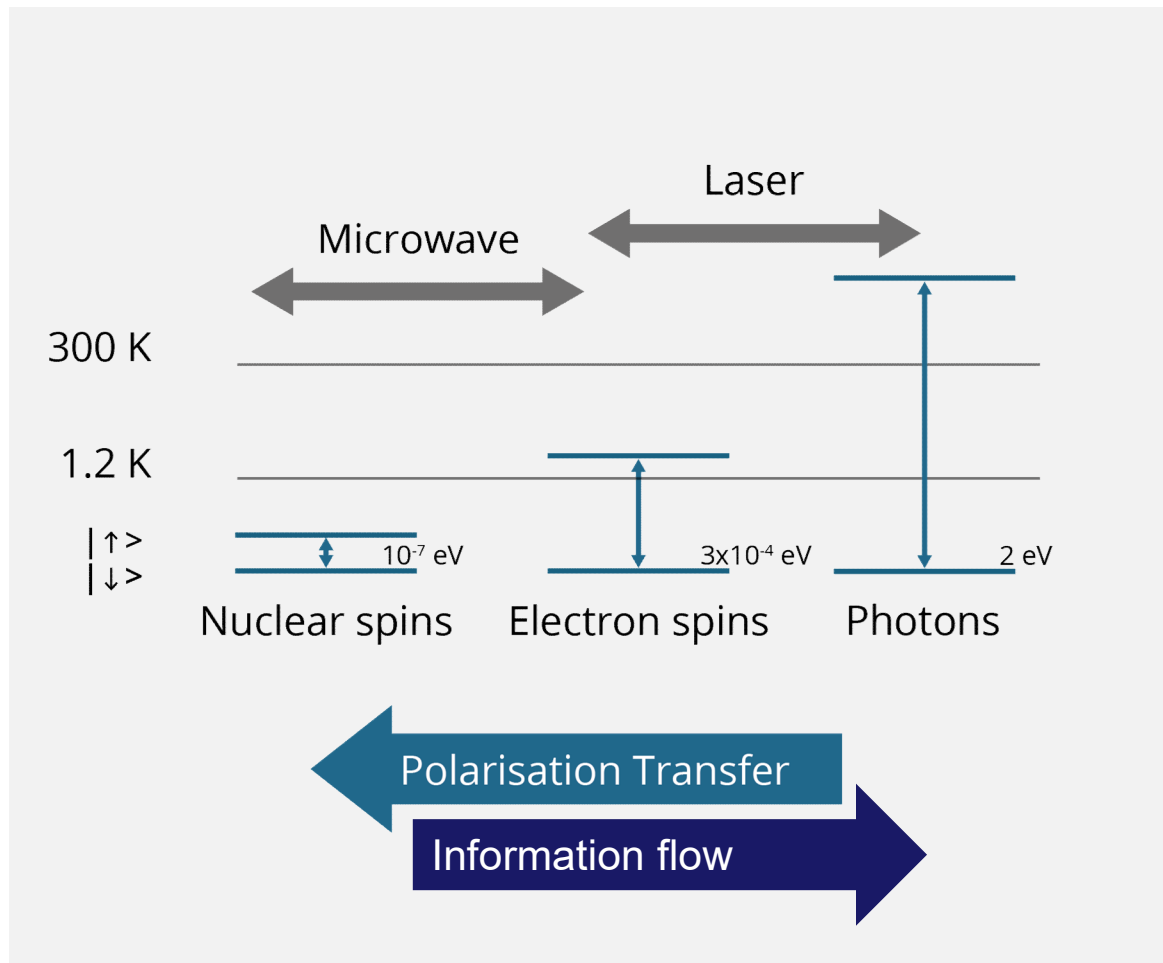


Concatenated Continuous Dynamical Decoupling

Robustness Against Driving Field Fluctuations



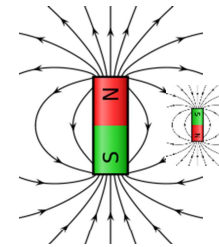
Principles



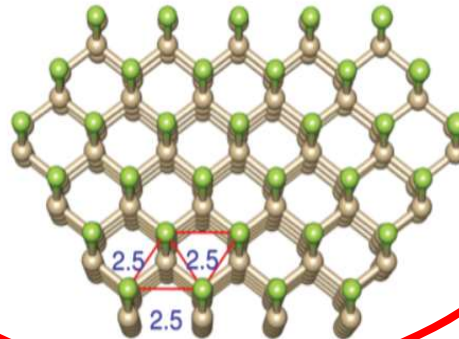
Roadmap

Diamond Quantum Devices for Simulation and Imaging

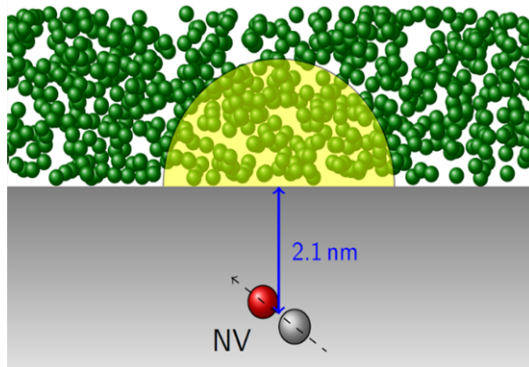
Electrons and Nuclei



Quantum Simulation



Nanoscale NMR



Quantum Simulation for 2-D Systems

Why ?

➤ Offer unusual physics

Anyons, Surface codes, Topological phase transitions, Frustration, ...

➤ Difficult to simulate by classical computers

For 1-D we have (t)-DMRG

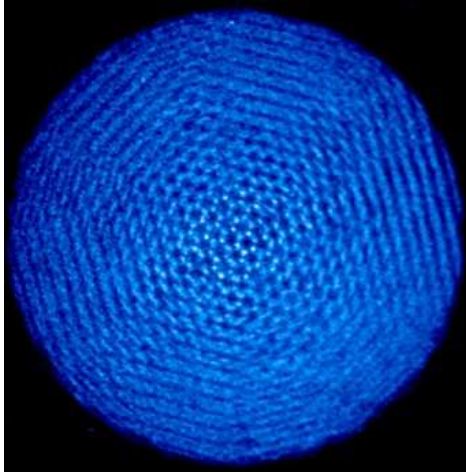
S.R. White, PRL 1992

For 2-D ...

Systems are really hard to simulate !

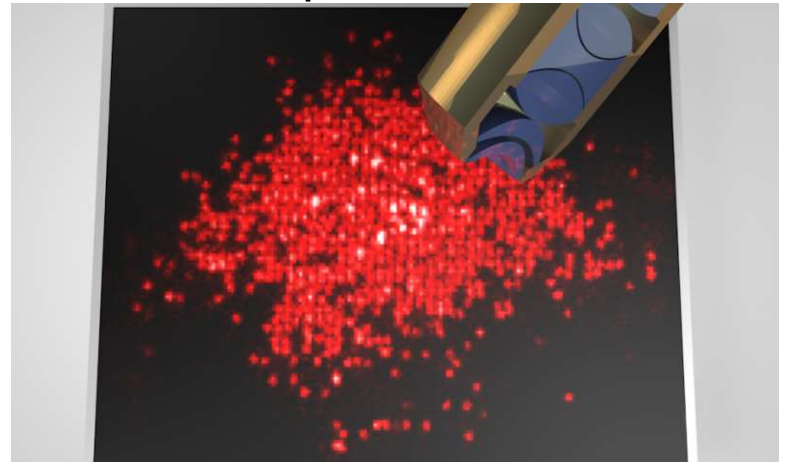
Quantum Simulation for 2-D Systems

2-D Trapped Ion Coulomb
Crystal



John Bollinger @ NIST

2-D Neutral Atom Optical
Lattice

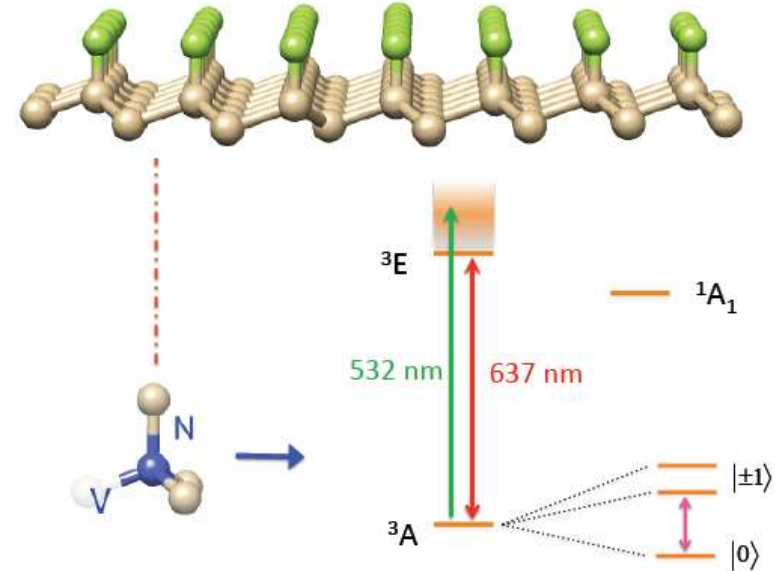
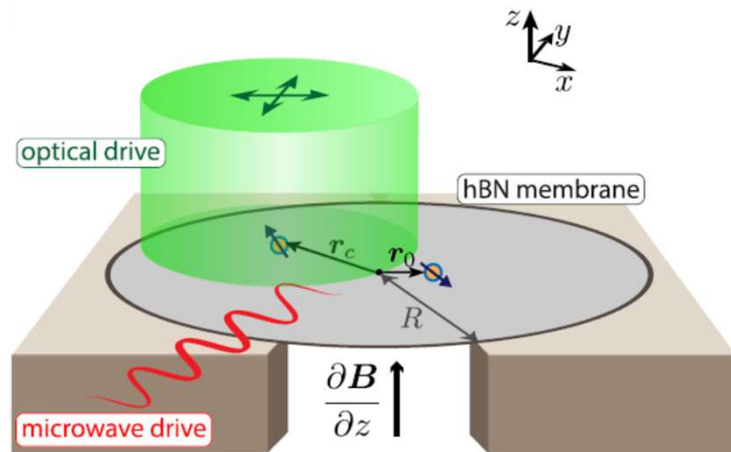


Immanuel Bloch @ MPQ Garching

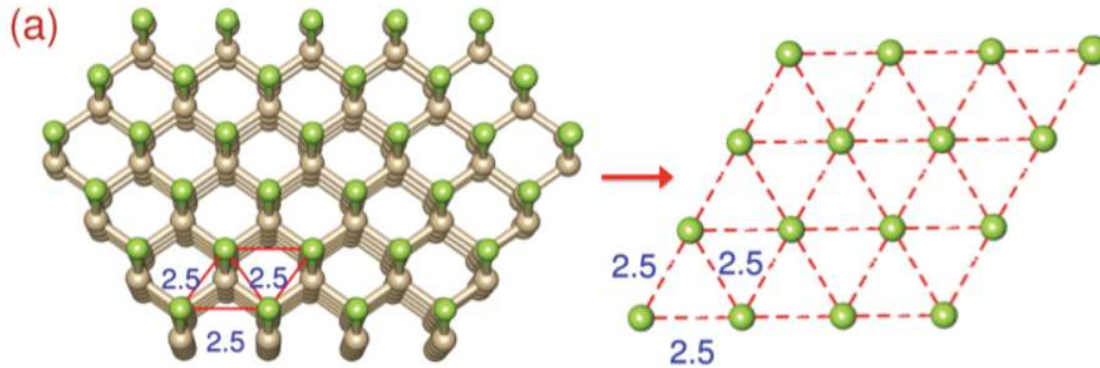
A Diamond Surface Simulator

Address three main challenges

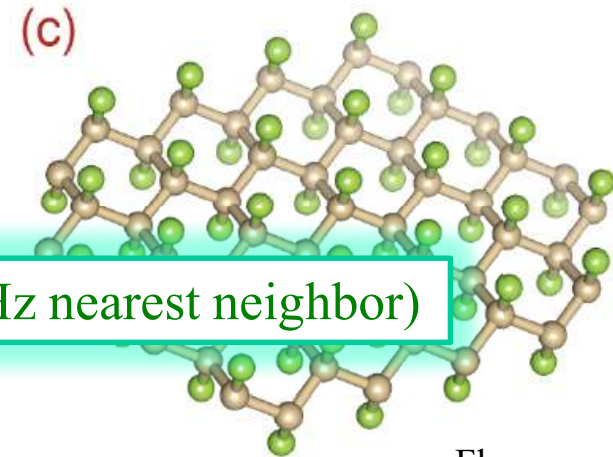
- Initialization of the nuclear spin lattice
- Control of the Hamiltonian of the nuclear spin lattice
- Readout from the nuclear spin lattice



A Diamond Surface Simulator

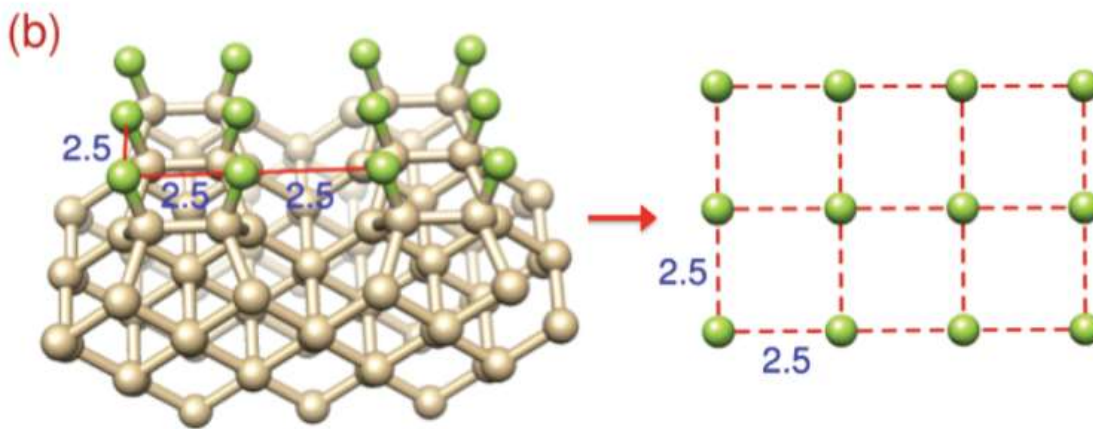


Diamond 111-surface



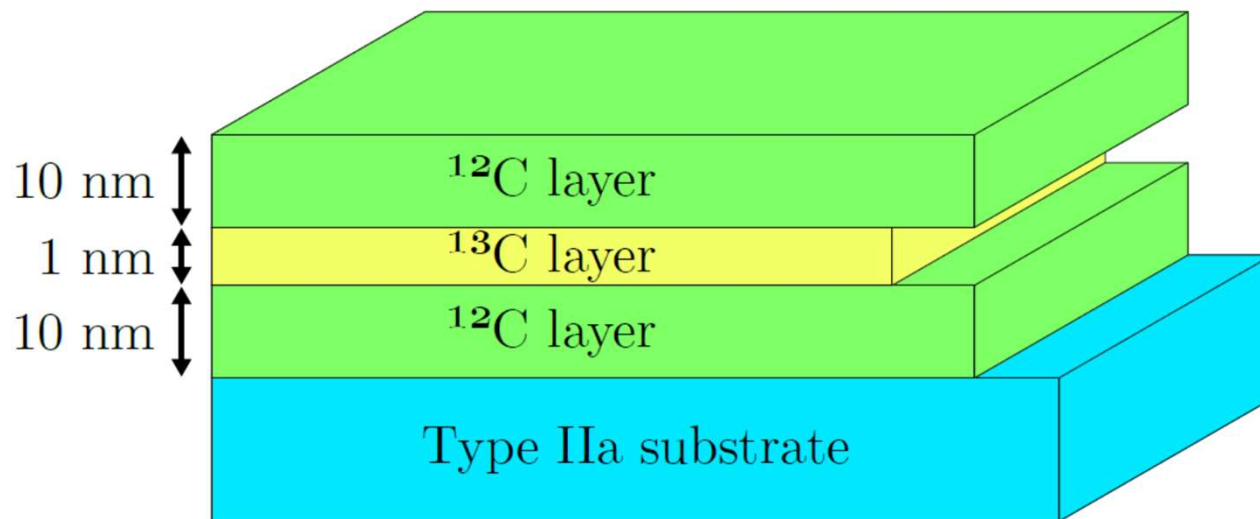
Fluorographene

F-F (long range dipole) interaction (6.8kHz nearest neighbor)



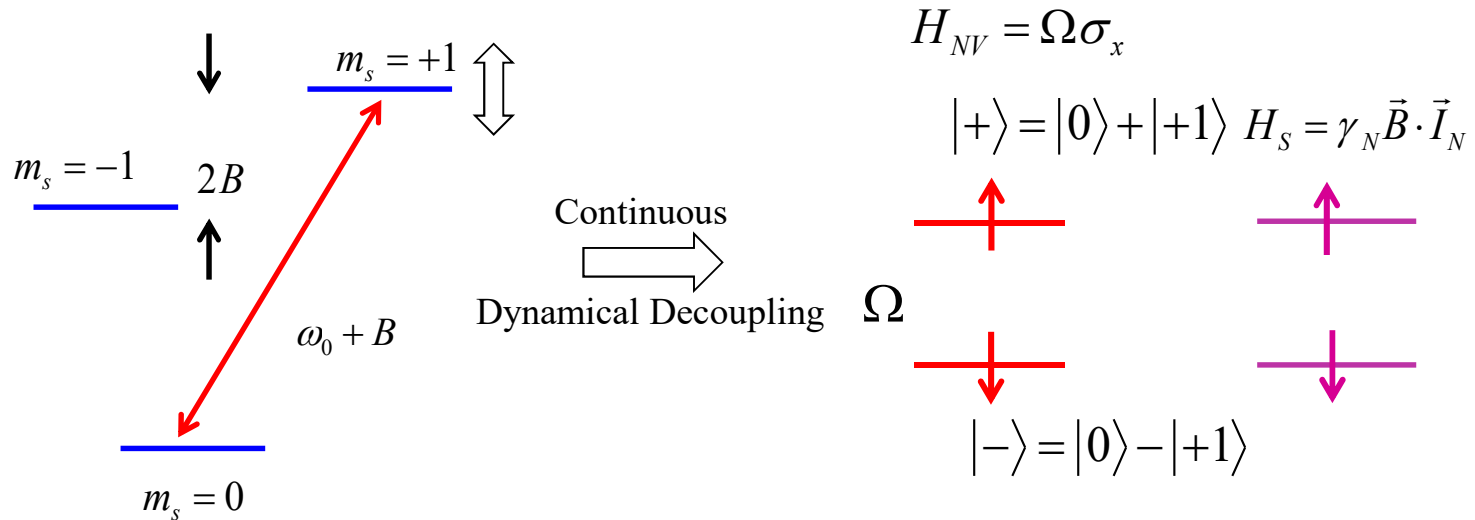
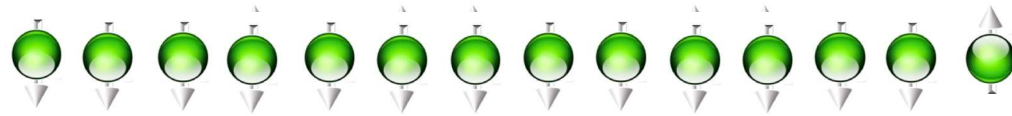
Diamond 100-surface

Quasi-2D Spin Layers



Nitrogen introduced during the growth of the ^{13}C layer, facilitating NV centers in the vicinity of the spin layer.

Initialising a Nuclear Spin Lattice



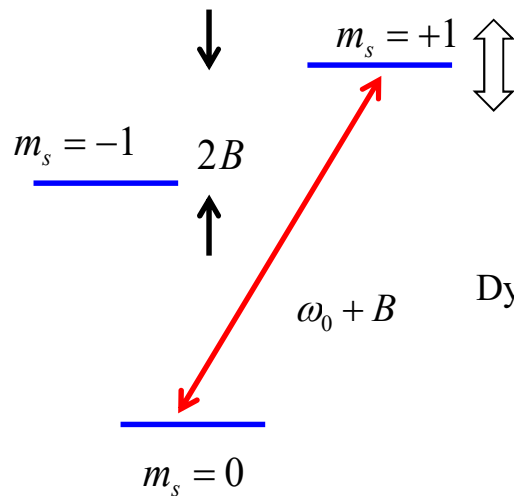
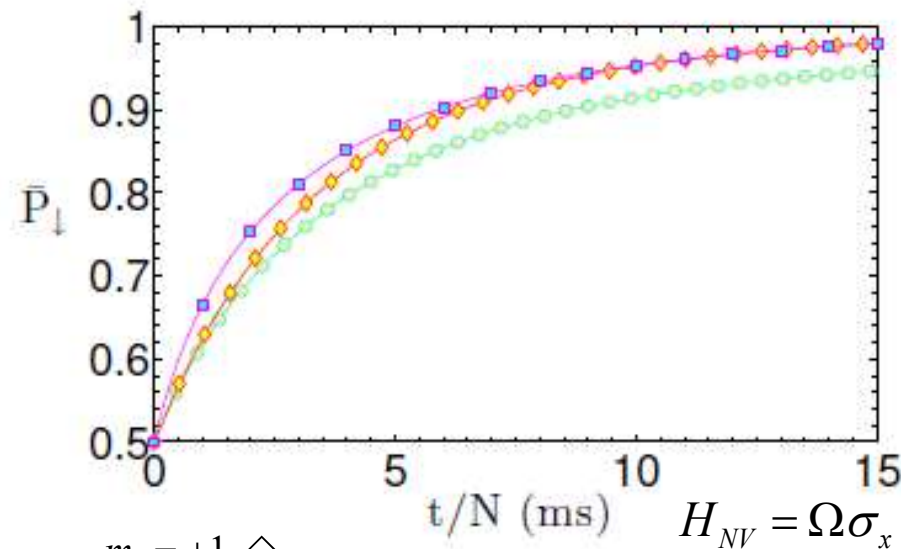
Magnetic field defines two-level system

Hartmann-Hahn condition (1962)

$$\sigma_z \Leftrightarrow \sigma_x$$

Interaction with environment
carries energy penalty

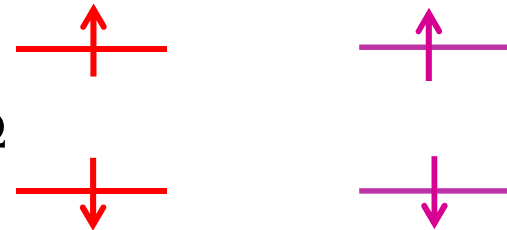
Initialising a Nuclear Spin Lattice



Continuous
Dynamical Decoupling

$$H_{NV} = \Omega \sigma_x$$

$$|+\rangle = |0\rangle + |1\rangle \quad H_S = \gamma_N \vec{B} \cdot \vec{I}_N$$



$$|-\rangle = |0\rangle - |1\rangle$$

$$\sigma_z \Leftrightarrow \sigma_x$$

Magnetic field defines two-level system

Hartmann-Hahn condition (1962)

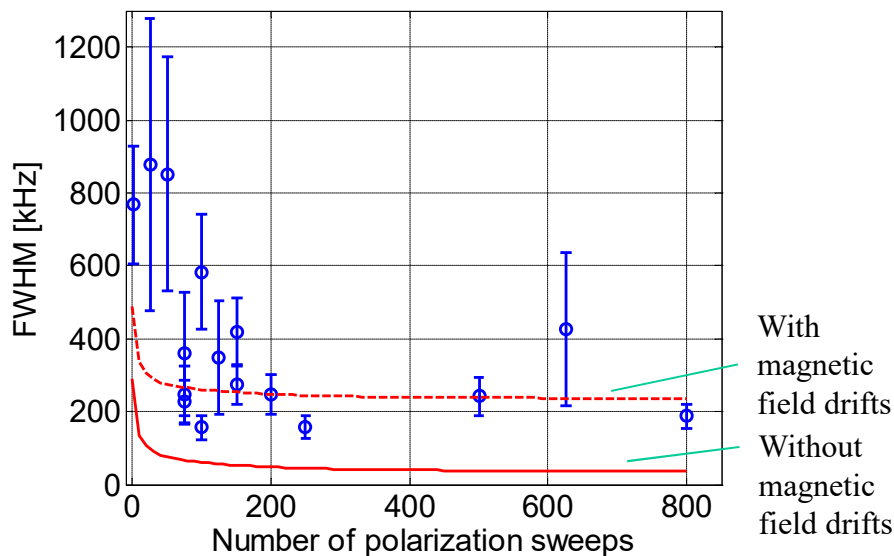
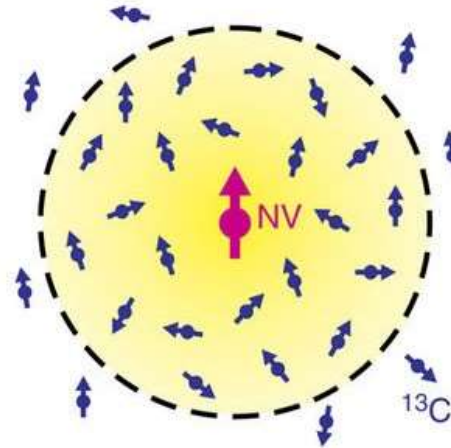
Interaction with environment
carries energy penalty

Spin Ensemble Initialisation

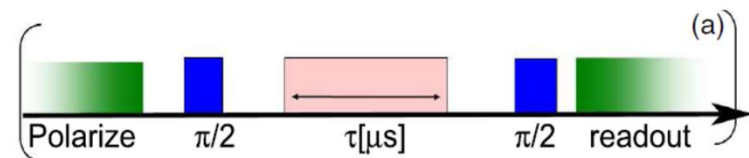
Polarization of nuclear spin bath
reduces linewidth due to T2 time



Polarization of nuclear spin bath
reduces NV-ESR linewidth



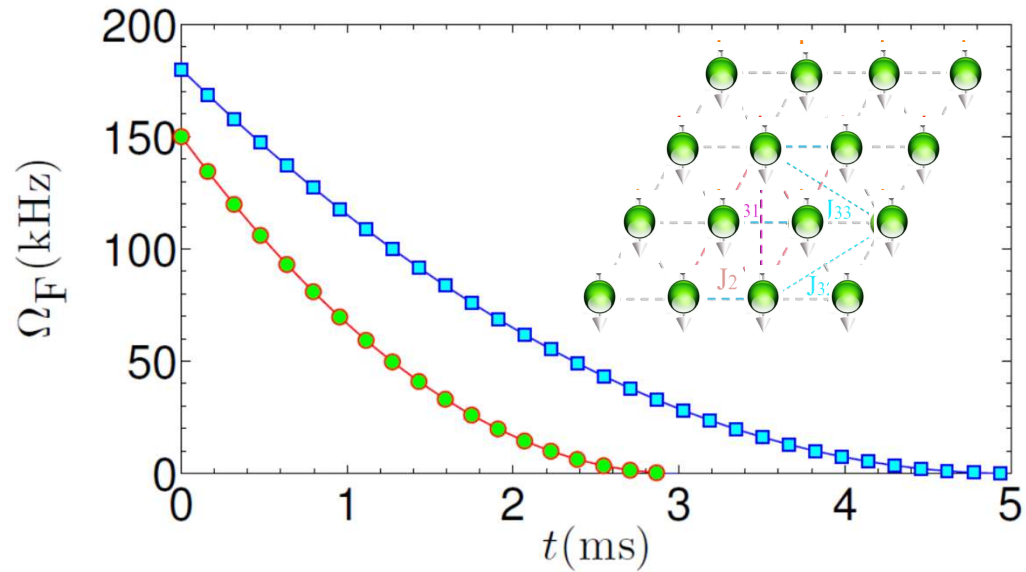
Use continuous microwave drive to establish
Hartmann-Hahn resonance.



Numerical simulation shows >90% polarization
after 500 sweeps of closest 10% of nuclear
spins randomly placed in 4nm radius from NV.

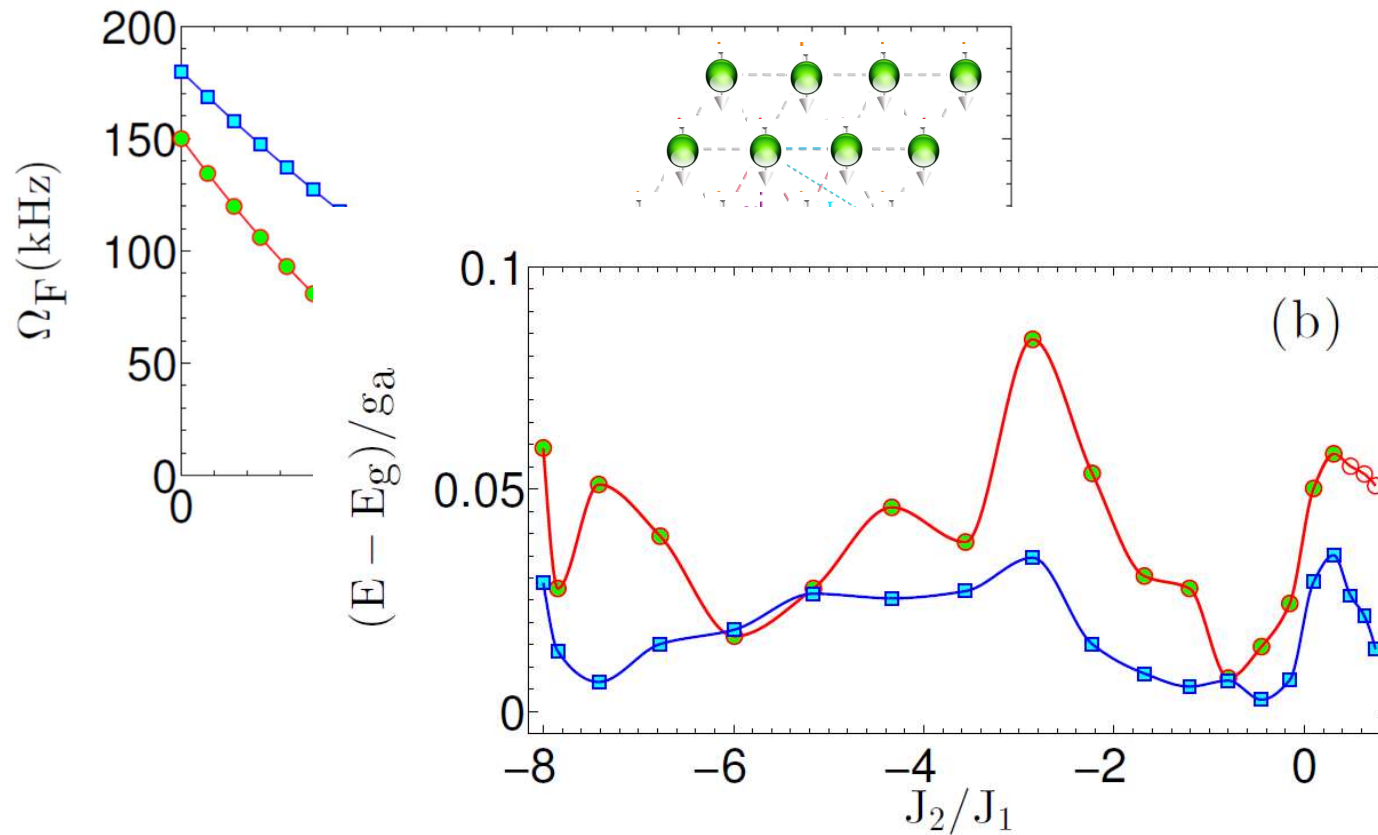
A Diamond Surface Simulator

Ground State Preparation & Detecting Quantum Phases



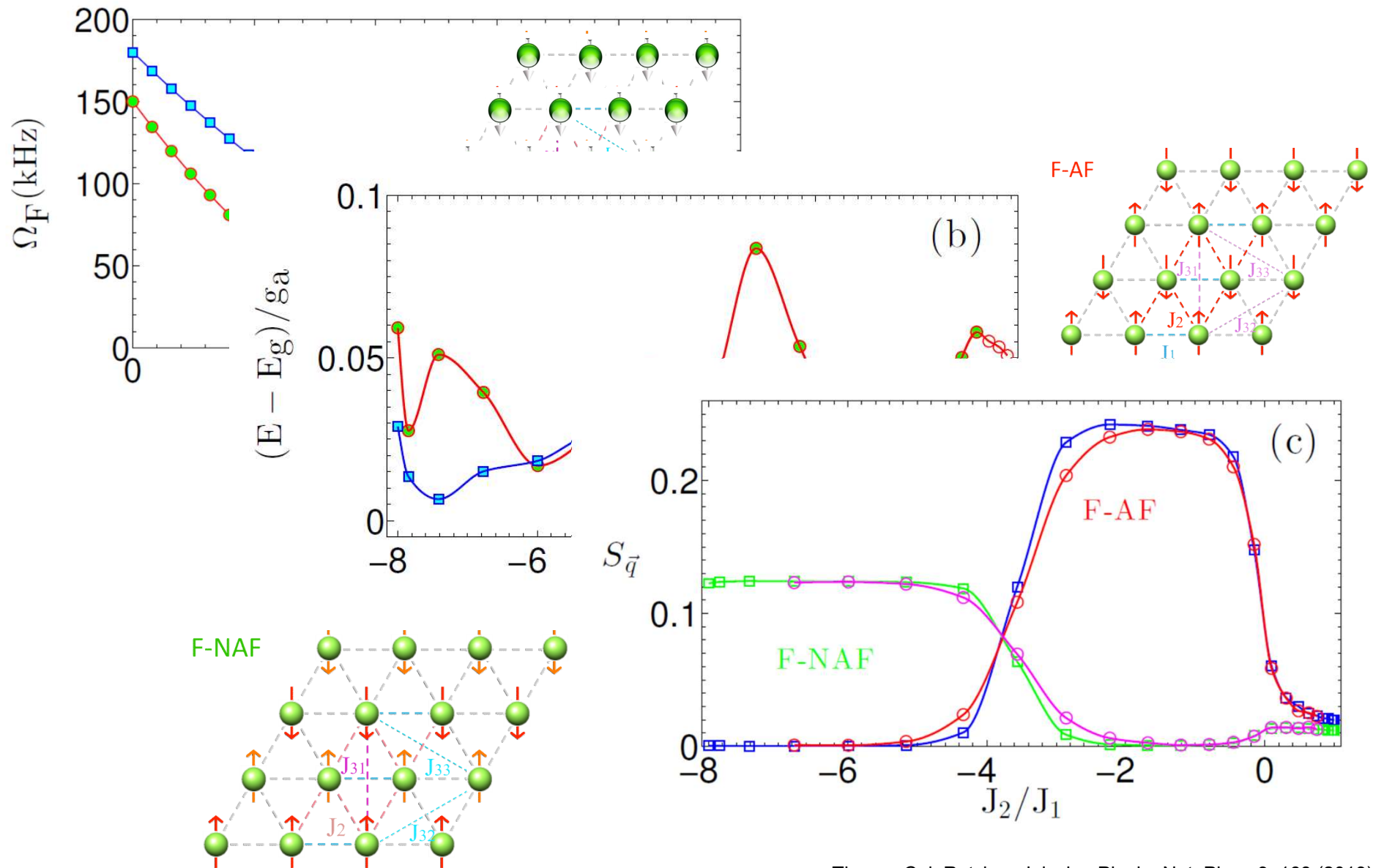
A Diamond Surface Simulator

Ground State Preparation & Detecting Quantum Phases



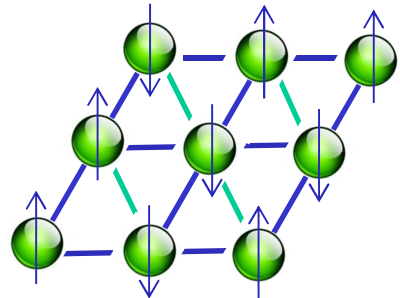
A Diamond Surface Simulator

Ground State Preparation & Detecting Quantum Phases



Readout of Nuclear Spin Lattice

Measurement with NV: $P_{\downarrow}^{\uparrow}(\tau) - P_{\uparrow}^{\downarrow}(\tau) = 2\tau^2 \sum_i g_i^2 I_i^z \longrightarrow$ Spin magnetization $\langle S_z \rangle = \sum_i \langle I_i^z \rangle$



Magnetic gradient: magnetic tip



State-of-art: 7 Gauss per Å

Spin structure factor:

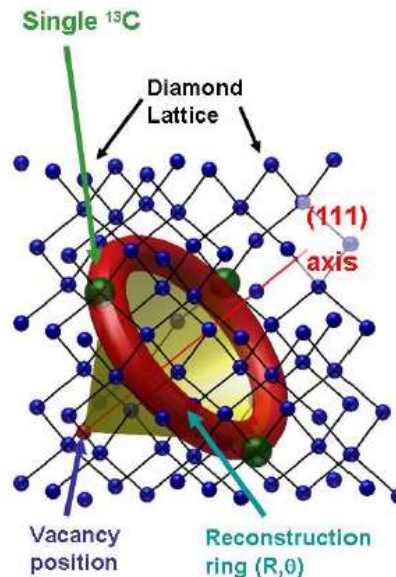
Various tricks

$$S(Q) = \sum_{(i,j)} \left\langle e^{i\vec{Q} \cdot (\vec{r}_i - \vec{r}_j)} I_i^z I_j^z + e^{i\vec{Q} \cdot (\vec{r}_j - \vec{r}_i)} I_j^z I_i^z \right\rangle$$

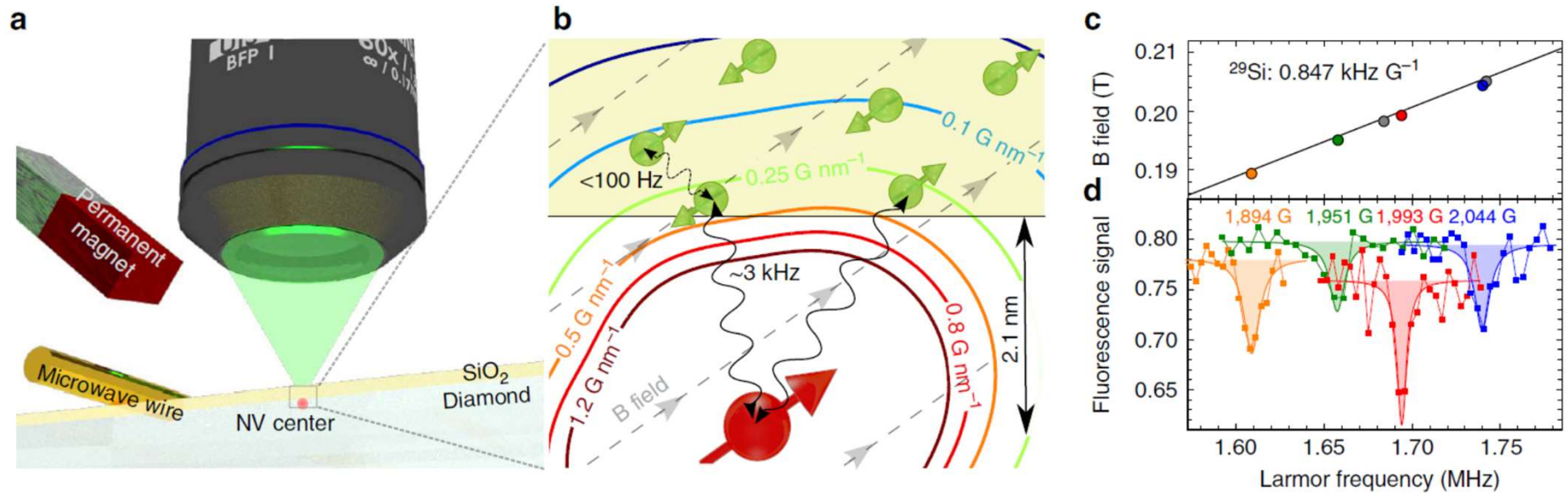
Theory: Cai ... Plenio, Nat. Phys. 9, 168 (2013)

Sufficient to lower bound entanglement:
Cramer, Plenio, Wunderlich, PRL 2013

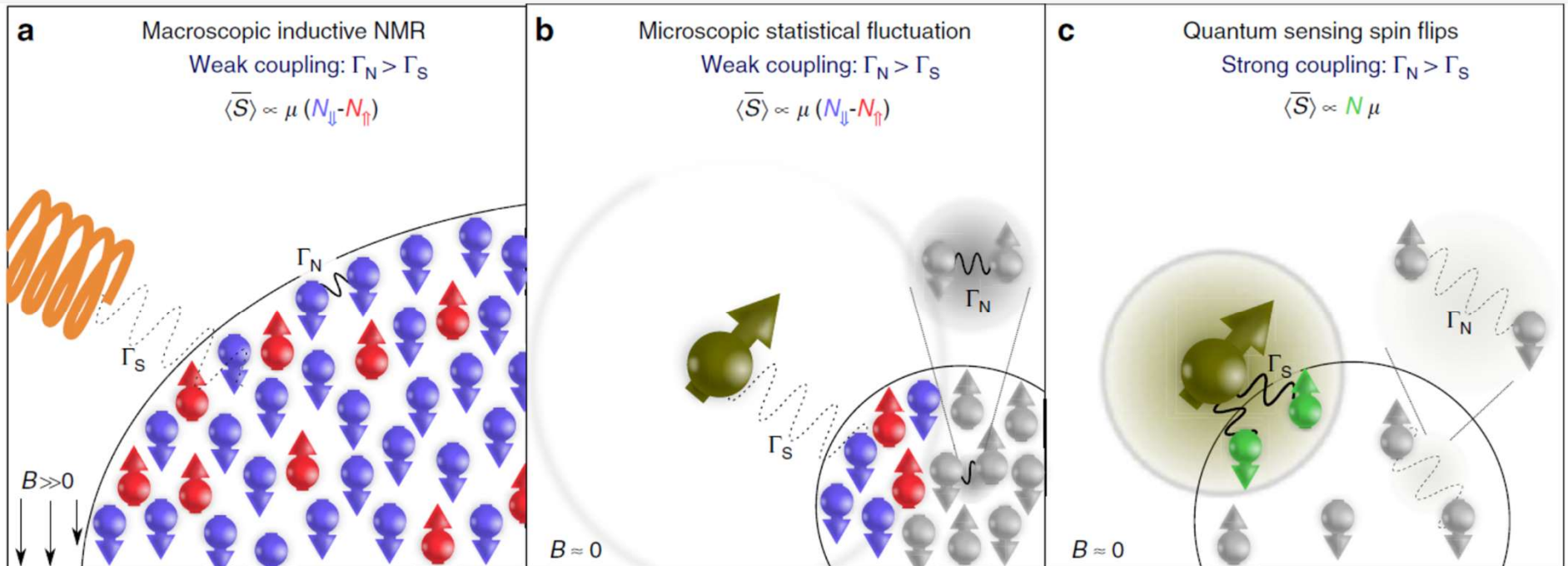
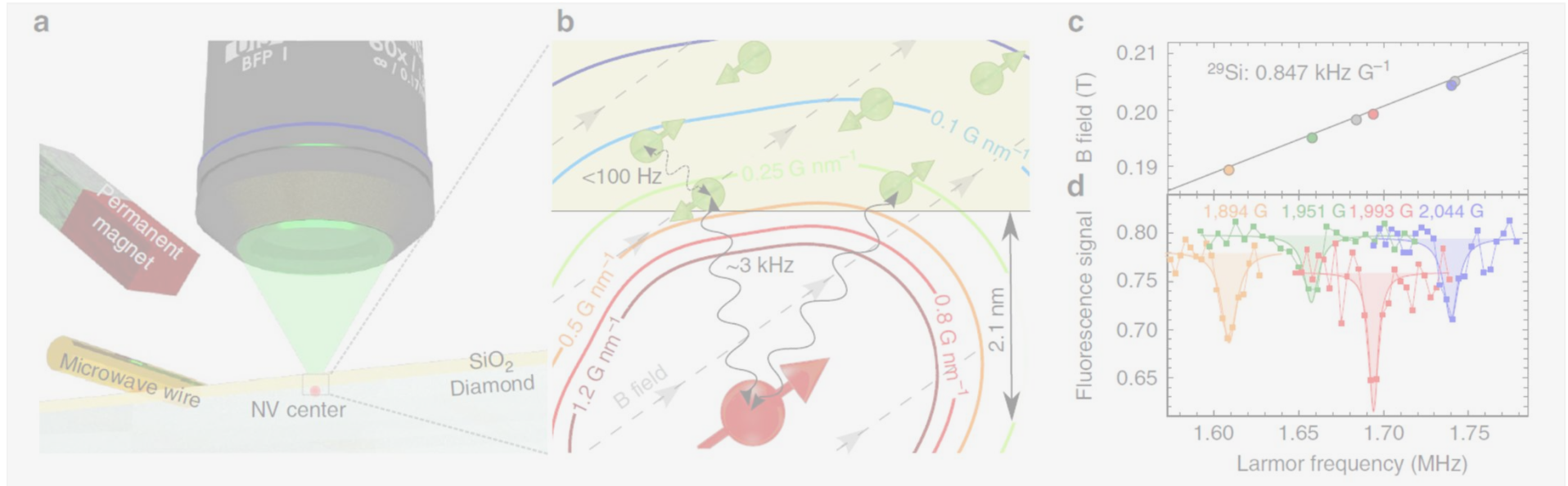
Exploit Hartmann-Hahn condition



Sensing Silicon Nuclear Spins above Diamond Surface



Sensing Silicon Nuclear Spins above Diamond Surface

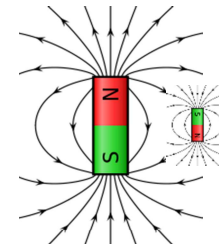


Experiment & Theory: Müller, Kong, Cai, Melentijevic, Stacey, Markham, Isoya, Pezzagna, Meijer, Du, Plenio, Naydenov, McGuinness & Jelezko., Nat. Comm. (2014)

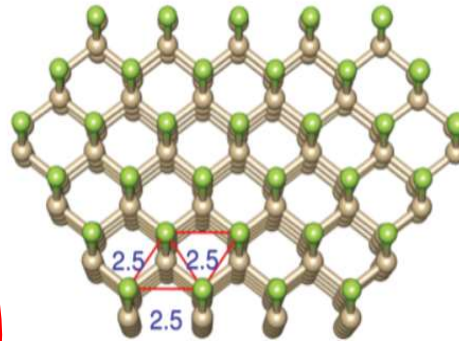
Roadmap

Diamond Quantum Devices for Simulation and Imaging

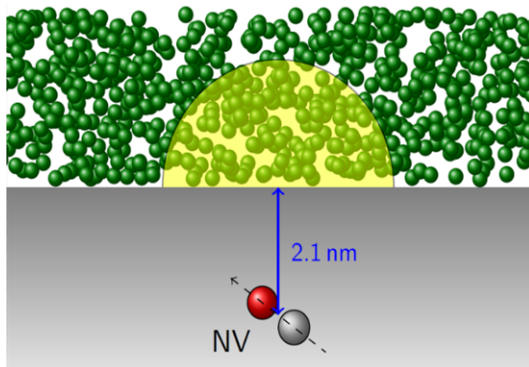
Electrons and Nuclei



Quantum Simulation



Nanoscale NMR

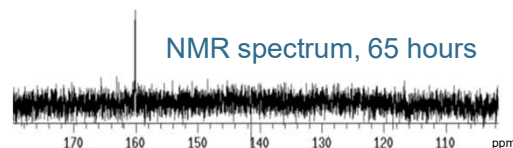
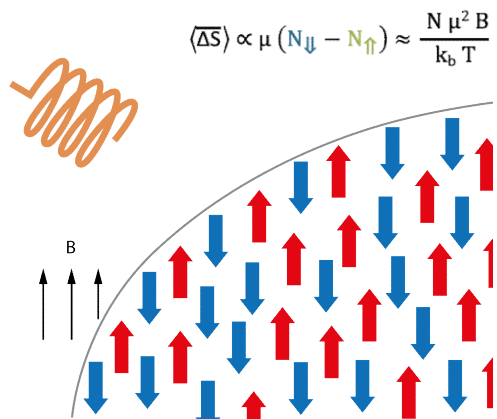


The Sensitivity Challenge of NMR

Classical NMR

- Inductive detector has high electronic noise
- Weak magnetisation – only one spin out of 1,000,000 polarised
- Typical sensitivity – 10^{18} spins (volume ~ millimeter scale)

Macroscopic – Inductive NMR

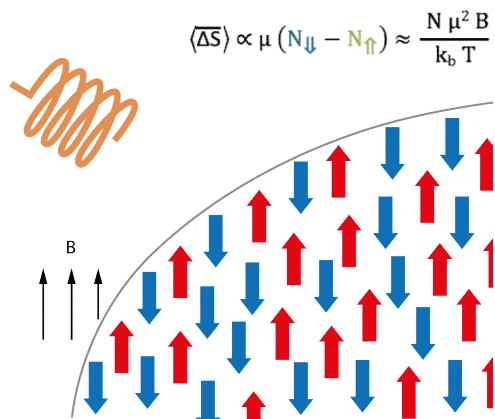


The Sensitivity Challenge of NMR

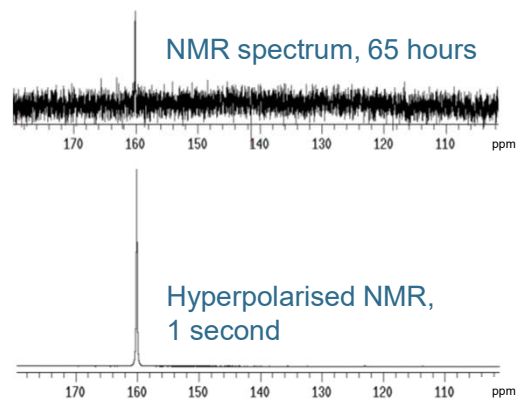
Hyperpolarised Classical NMR

- Inductive detector has high electronic noise
- Hyperpolarisation – one spin out of 10 polarised
- Typical sensitivity – 10^{13} spins (volume ~ 100 micron scale)

Macroscopic – Inductive NMR



Hyperpolarisation

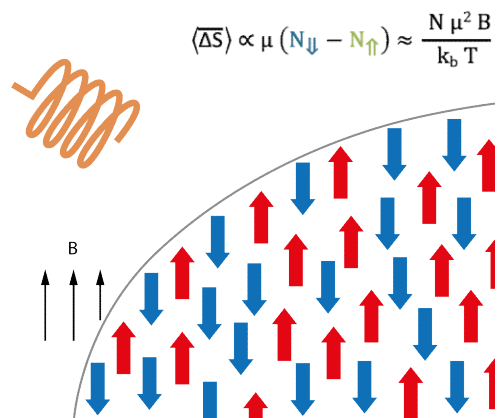


The Sensitivity Challenge of NMR

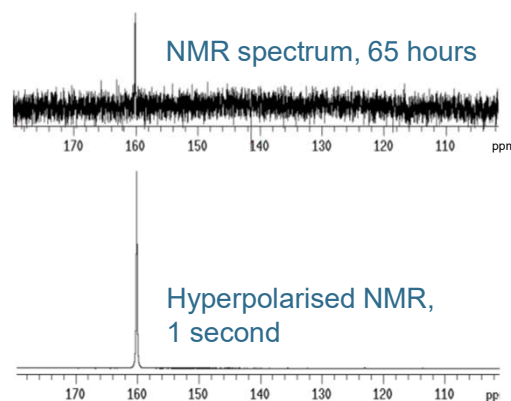
Hyperpolarised Quantum NMR

- Optically detected magnetic resonance
- Hyperpolarisation – one spin out of 10 polarised
- Detection volume – (sub)micron scale

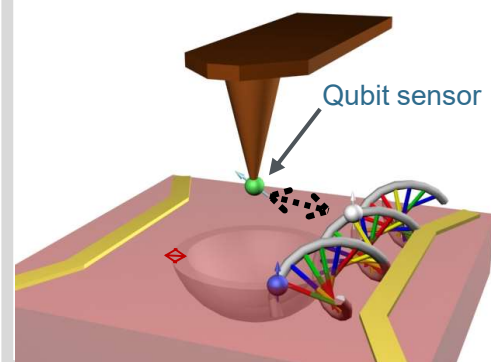
Macroscopic – Inductive NMR



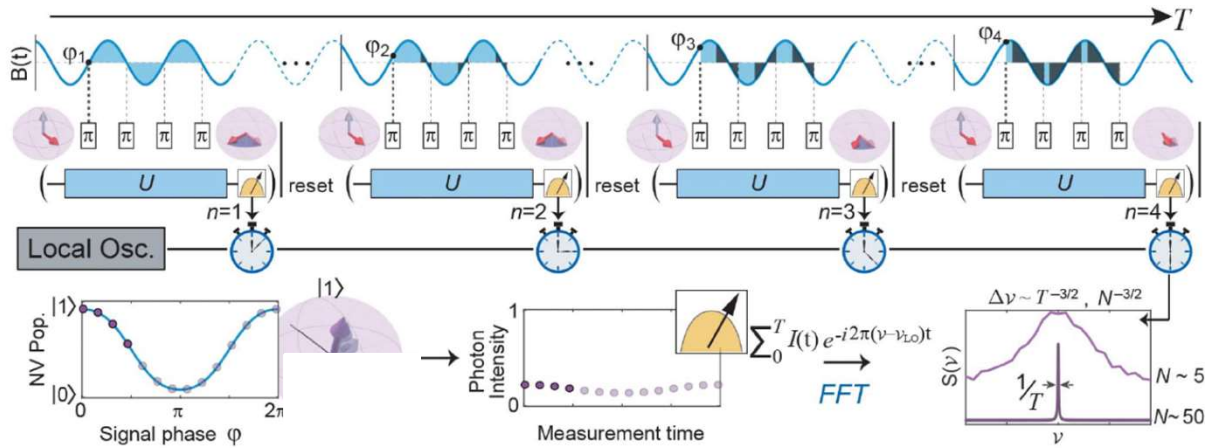
Hyperpolarisation



Diamond quantum sensing



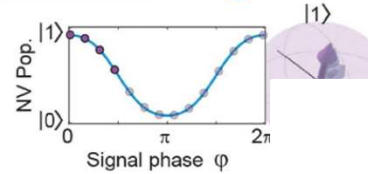
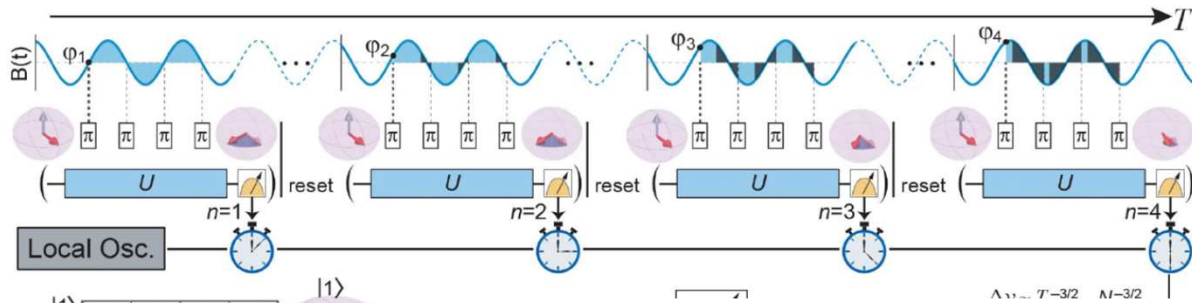
Nanoscale NMR



Qdyne

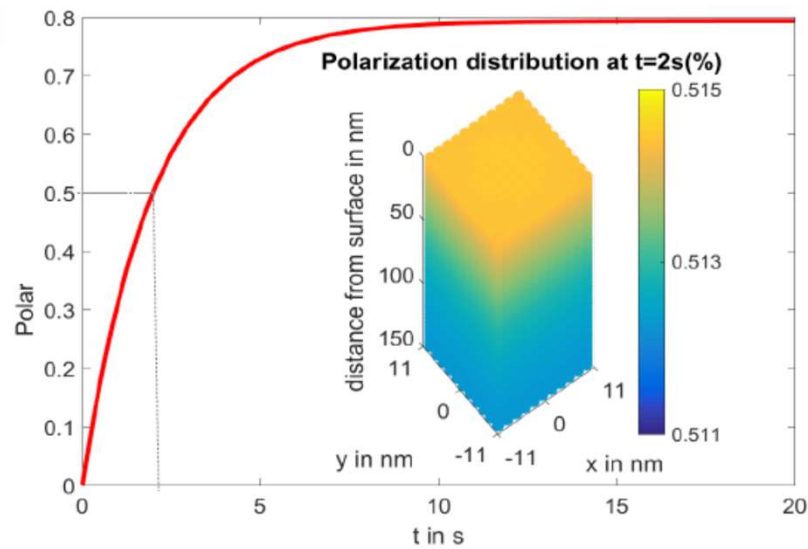
Science 356, 832 (201)

Nanoscale NMR



Qdyne

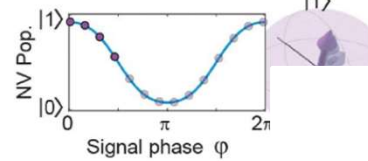
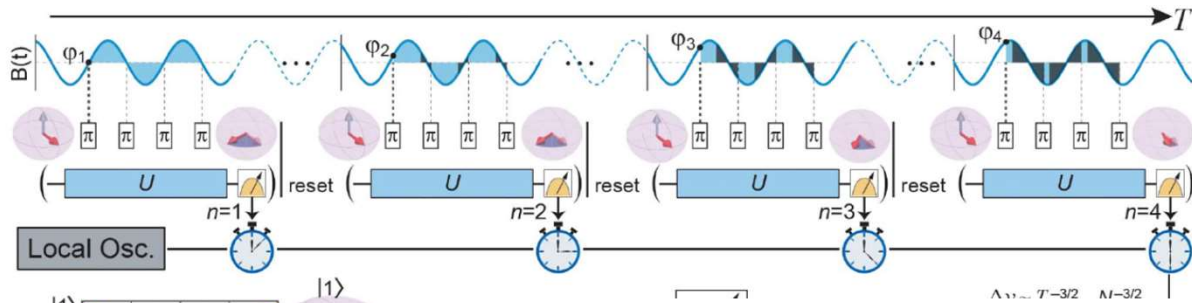
Science 356, 832 (201)



Hyperpolarisation

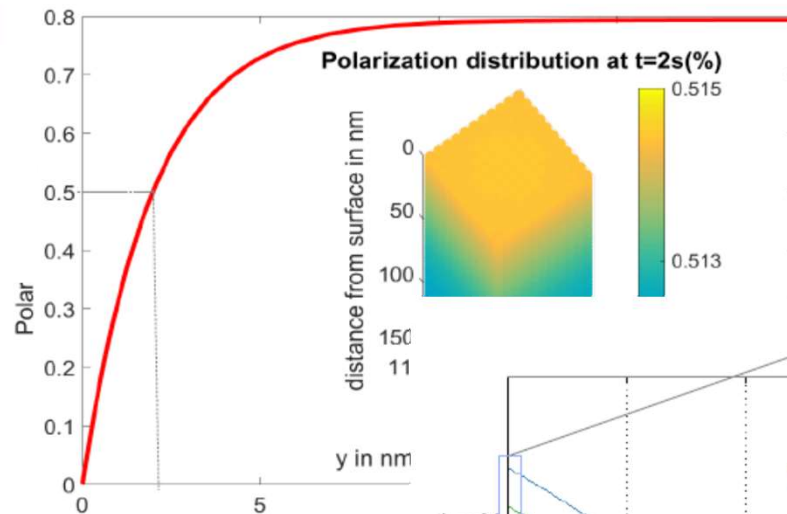
Nat. Phys. 9, 168 (2013)
Phys. Rev. Lett. 111, 067601 (2013)
Sci. Reports 9, 6938 (2019)

Nanoscale NMR



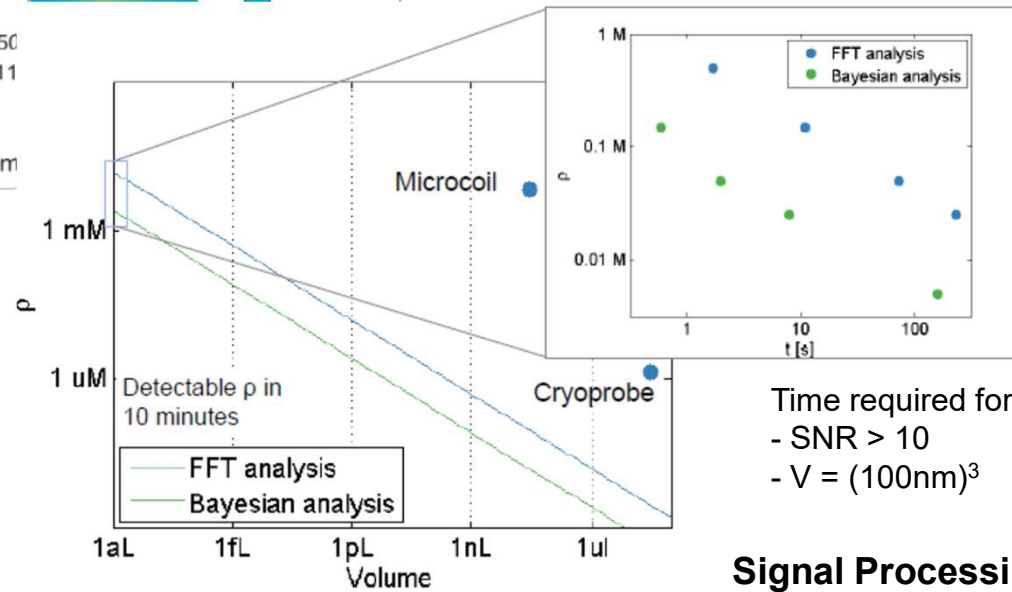
Qdyne

Science 356, 832 (201)



Hyperpolarisation

Nat. Phys. 9, 168 (2013)
Phys. Rev. Lett. 111, 067601 (2013)
Sci. Reports 9, 6938 (2019)

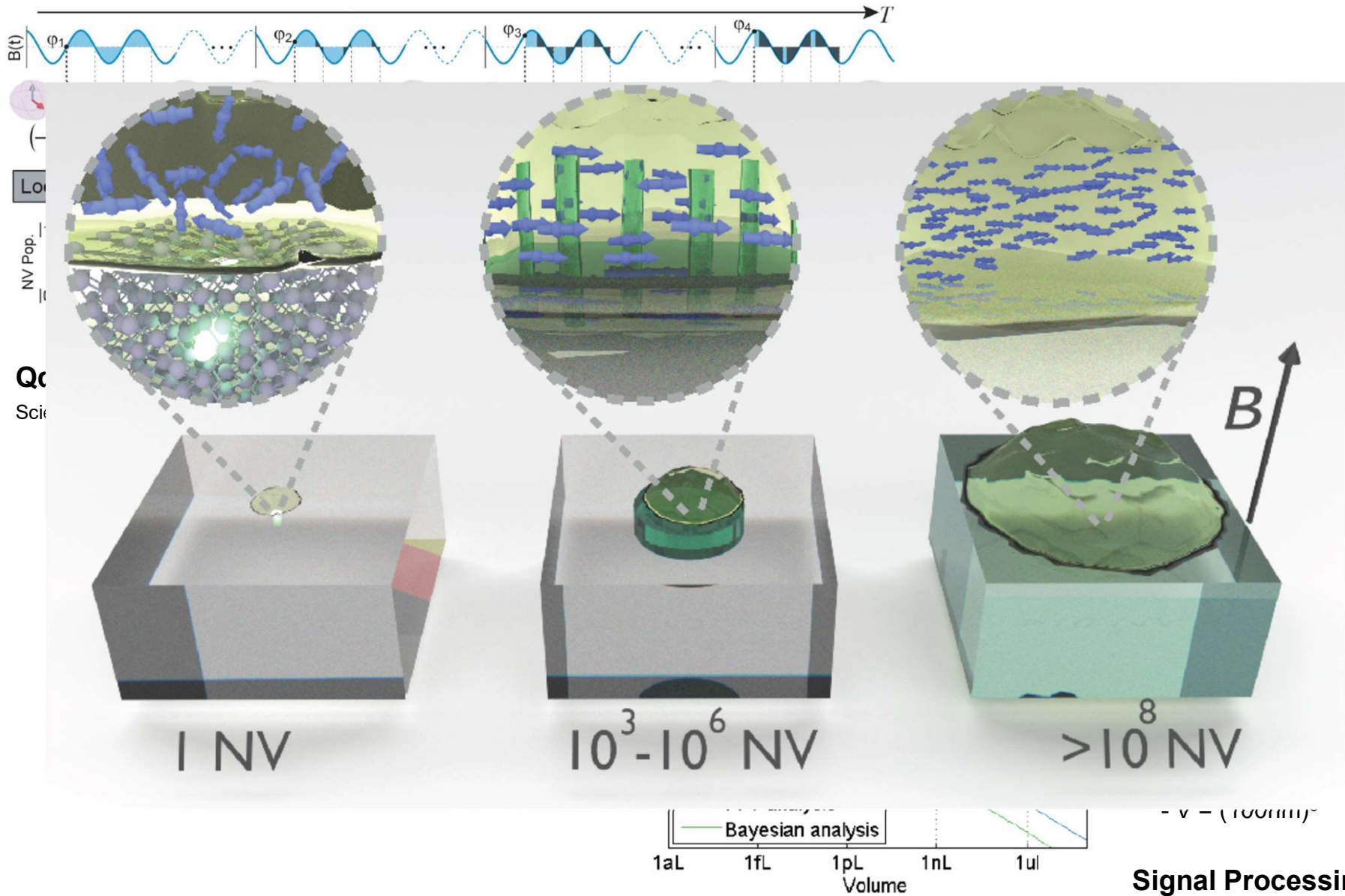


Time required for
- SNR > 10
- $V = (100\text{nm})^3$

Signal Processing

Sci. Reports 9, 6938 (2019)

Nanoscale NMR

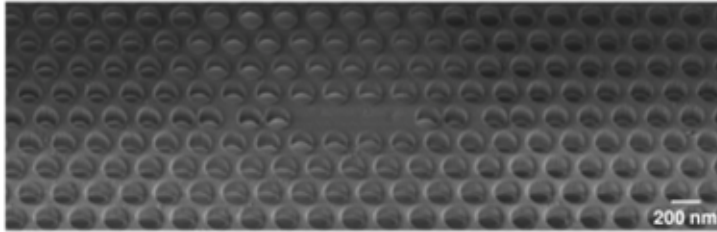


Signal Processing

Sci. Reports 9, 6938 (2019)

Colour Centers for Quantum Technologies

Optical Interface, Repeater, Computer



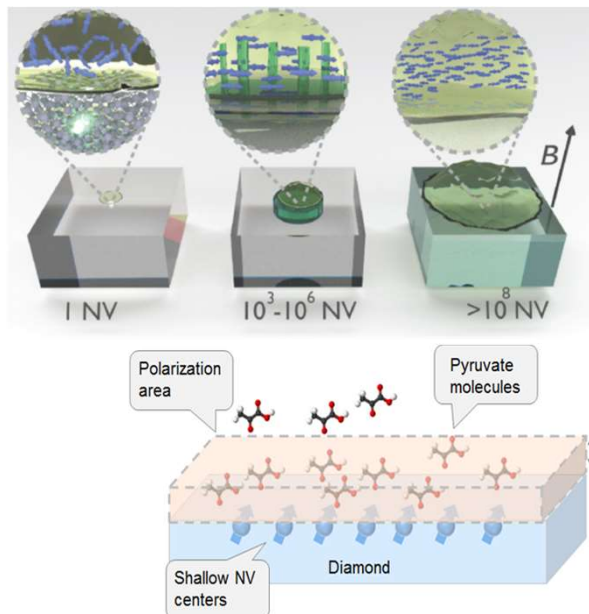
Englund et al, arXiv:1801.01151

Quantum Sensor

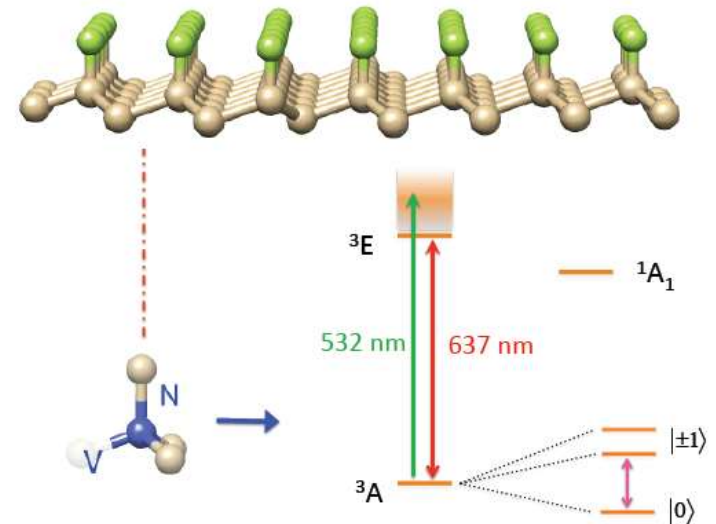


NJP 15, 013020 (2013); Nature Comm. **5**, 4703 (2014); ...

Nanoscale NMR & Hyperpolarisation



Quantum Simulator



Nature Phys. **9**, 168 (2013)

PRL 111, 067601 (2013); Sci. Adv. **4**, eaat8978 (2018); Science **356**, 832 (2017)

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Synergy Grant:
Diamond Quantum
Devices and Biology & Proof of Concept Grant
(BioQ) 2013 -2019



European Research Council
Established by
the European Commission

Synergy Grant: Quantum hyperpolarisation
for ultrasensitive NMR and MRI
(HyperQ) 2020 - 2026



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**SFB TRR-21 & SPP 1601
Reinhart Koselleck Award**