Casimir effect meets the cosmological constant







Ulf Leonhardt, Weizmann Institute of Science, 5 May 2022

Dark energy – cosmological constant



Forces of the Quantum Vacuum presents a number of approaches to Casimir, van der Waals and Casimir-Polder forces that have been fruitfully employed in mainstream research, and reviews the experimental evidence for Casimir forces.

Beginning with basic ideas in quantum mechanics and building its way to a sophisticated form of macroscopic QED, Forces of the Quantum Vacuum provides an inspiring training manual for graduate students that develops the ideas needed for modern research on Casimir forces in a natural progression, with a strong emphasis on physical understanding.

Contributing editors

William Simpson is a Research Fellow in Theoretical Physics at the Weizmann Institute of Science, and a Research Associate in Theology at the University of St Andrews.

Ulf Leonhardt is a Professor of Physics at The Weizmann Institute of Science. His research interests include quantum electrodynamics in media, Hawking radiation, and transformation optics.

"... a refreshingly readable introduction to Casimir physics. The contributing experts have introduced the concepts and techniques needed for students and nonspecialists to learn the essential physics of van der Waals and Casimir forces."

> Peter Milonni, Professor of Physics, University of Rochester

William M.R. Simpson Ulf Leonhardt

FORCES OF THE QUANTUM VACUUM

An introduction to Casimir Physics





Redwood Sequoia sempervirens

The limits to tree height

George W. Koch¹, Stephen C. Sillett², Gregory M. Jennings² & Stephen D. Davis³

 ¹Department of Biological Sciences and the Merriam-Powell Center for Environmental Research, Northern Arizona University, Flagstaff, Arizona 86011, USA
²Department of Biological Sciences, Humboldt State University, Arcata, California 95521, USA
³Natural Science Division, Pepperdine University, Malibu, California 90263-4321, USA

Trees grow tall where resources are abundant, stresses are minor, and competition for light places a premium on height growth^{1,2}. The height to which trees can grow and the biophysical determinants of maximum height are poorly understood. Some models predict heights of up to 120 m in the absence of mechanical damage^{3,4}, but there are historical accounts of taller trees⁵. Current hypotheses of height limitation focus on increasing water transport constraints in taller trees and the resulting reductions in leaf photosynthesis⁶. We studied redwoods (Sequoia sempervirens), including the tallest known tree on Earth (112.7 m), in wet temperate forests of northern California. Our regression analyses of height gradients in leaf functional characteristics estimate a maximum tree height of 122-130 m barring mechanical damage, similar to the tallest recorded trees of the past. As trees grow taller, increasing leaf water stress due to gravity and path length resistance may ultimately limit leaf expansion and photosynthesis for further height growth, even with ample soil moisture.



The limits to tree height

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Casimir force in nature: gecko feet



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FORCES OF THE QUANTUM VACUUM

An introduction to Casimir Physics

Dark energy – cosmological constant





2011

The Cosmological Principle: homogeneity and isotropy



 α (DD mm ss)



The Cosmological Principle: homogeneity and isotropy





Take an arbitrary point in homogeneous space



Pick another point and consider their distance *a*





Acceleration on particle at distance a: Gauss' law





Acceleration on particle at distance a: Gauss' law







Relativistic acceleration on particle at distance *a*



 $\mathcal{E} = \mathcal{OC}^2$ $\frac{t\pi 6}{3\rho^2} \left(\varepsilon + 3p \right)$





Sitzung der physikalisch-mathematischen Klasse vom 8. Februar 1917

Kosmologische Betrachtungen zur allgemeinen Relativitätstheorie.

Von A. EINSTEIN.









Einstein's field equations with cosmological term







 $R_{M}^{\nu} - \frac{R}{2} \frac{\delta V}{M} = \frac{\delta T G}{C4} \left(\frac{T^{\nu} + \epsilon_{A} \delta^{\nu}}{M} \right)$





























Acceleration!







70% of all ε at present time



Dark energy – cosmological constant



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FORCES OF THE QUANTUM VACUUM

An introduction to Casimir Physics







The gravity of vacuum fluctuations

SOVIET PHYSICS USPEKHI

VOLUME 11, NUMBER 3

530.12 : 531.51

Institute of Applied Mathematics, USSR Academy of Sciences

Usp. Fiz. Nauk 95, 209-230 (May, 1968)



NOVEMBER-DECEMBER 1968

THE COSMOLOGICAL CONSTANT AND THE THEORY OF ELEMENTARY PARTICLES

Ya. B. ZEL'DOVICH

The gravity of vacuum fluctuations

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NOVEMBER-DECEMBER 1968

Ya. B. ZEL'DOVICH



Steven Weinberg

Steven Weinberg



Steven Weinberg



 $\left|\frac{\mathrm{tr}G}{\mathrm{c}^3} \approx 1.6 \cdot 10^{-5} \mathrm{cm}\right|$ lp

Steven Weinberg





 $\frac{tG}{c^3} \approx 1.6 \cdot 10^{-5} \text{ cm}$ $\frac{1}{G} \approx 2.2 \cdot 10^{-9} q$ MP

Steven Weinberg







 $\left|\frac{\mathrm{tr}G}{\mathrm{c}^3} \approx 1.6 \cdot 10^{-5} \mathrm{cm}\right|$ $\sqrt{\frac{\hbar c}{G}} \approx 2.2 \cdot 10^{-5} q$ $M_P = \gamma$

=) $log_{10}(g_{Th}/g) \approx 120$

A general argument? : general covariance of the vacuum

 $T_{M}^{\nu} = \varepsilon_{\Lambda} \delta_{M}^{\nu}$
The vacuum

The vacuum state $|0\rangle$

Unruh-Fulling-Davies effect: view of an accelerated observer



nature photonics

The Casimir effect in microstructured geometries

Alejandro W. Rodriguez^{1,2}, Federico Capasso^{1*} and Steven G. Johnson²



FOCUS | REVIEW ARTICLES PUBLISHED ONLINE: 31 MARCH 2011 | DOI: 10.1038/NPHOTON.2011.39

c Casimir effect (macroscopic bodies)



nature photonics

The Casimir effect in microstructured geometries

Alejandro W. Rodriguez^{1,2}, Federico Capasso^{1*} and Steven G. Johnson²



VOLUME 78, NUMBER 1

PHYSICAL REVIEW LETTERS

Demonstration of the Casimir Force in the 0.6 to 6 μ m Range

S.K. Lamoreaux* Physics Department, University of Washington, Box 35160, Seattle, Washington 98195-1560 (Received 28 August 1996)

FOCUS | **REVIEW ARTICLES** PUBLISHED ONLINE: 31 MARCH 2011 | DOI: 10.1038/NPHOTON.2011.39

c Casimir effect (macroscopic bodies)



6 JANUARY 1997

Precision measurements and ma



RESEARCH

PHYSICS

Stable Casimir equilibria and quantum trapping

Rongkuo Zhao¹^{*}, Lin Li¹^{*}, Sui Yang¹^{*}, Wei Bao¹^{*}, Yang Xia¹, Paul Ashby², Yuan Wang¹, Xiang Zhang^{1,3}⁺

Science **364**, 984–987 (2019) 7 June 2019



Optical analogue of expanding, spatially flat universe



ct

n(*t*)

Ulf Leonhardt and Thomas Philbin

GEOMETRY ADD LIGHT The Science of **INVISIBILITY**



Lifshitz theory



SOVIET PHYSICS USPEKHI

SOVIET PHYSICS

USPEKHI

A Translation of Uspekhi Fizicheskikh Nauk

(Russian Vol. 73, Nos. 3-4

SEPTEMBER-OCTOBER 1961

GENERAL THEORY OF VAN DER WAALS' FORCES

I. E. DZYALOSHINSKII, E. M. LIFSHITZ, and L. P. PITAEVSKII

Usp. Fiz. Nauk 73, 381-422 (March, 1961)

b Casimir-Polder (waves/retardation)



c Casimir effect (macroscopic bodies)



Renormalization: bare vacuum energy is infinite



Renormalization: compare vacuum energy at finite distance



with



Renormalization: compare vacuum energy at finite distance





with





Einstein's field equations: all energy is supposed to curve space-time

GEOMETRY OF SPACETIME

All energy should gravitate



No gravity from the bare vacuum.

 $S \approx 10^{-29} \text{ gcm}^{-3}$

No evidence for the bare vacuum.

Neither does it do mechanical work nor gravitate.

 $\beta \approx 10^{-29} \text{ gcm}^{-3}$

Casimir cosmology: turn from space



Casimir cosmology: turn from space to time



Casimir cosmology: continuous n(t)

n(*t*)



Surprises in Casimir physics with three students and a postdoc





William Simpson PhD student 2010-14

Itay Griniasty PhD student 2013-19



Yael Avni Masters 2015-17

Efi Shahmoon postdoc 2014



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Lifshitz theory of the cosmological constant Ulf Leonhardt

Department of Physics of Complex Systems, Weizmann Institute of Science, Rehovot 7610001, Israel

ARTICLE INFO

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Keywords: Casimir force Dielectrics Vacuum fluctuations Dark energy

Astrophysics has given empirical evidence for the cosmological constant that accelerates the expansion of the universe. Atomic, Molecular, and Optical Physics have proven experimentally that the quantum vacuum exerts forces - the van der Waals and Casimir forces - on neutral matter. It has long been conjectured (Zel'dovich, 1968) that the two empirical facts, the cosmological constant and the Casimir force, have a common theoretical explanation, but all attempts of deriving both from a unified theory in quantitative detail have not been successful so far. In AMO Physics, Lifshitz theory has been the standard theoretical tool for describing the measured forces of the quantum vacuum. This paper develops a version of Lifshitz theory that also accounts for the electromagnetic contribution to the cosmological constant. Assuming that the other fields of the Standard Model behave similarly, gives a possible quantum-optical explanation for what has been called dark energy. © 2019 The Author(s). Published by Elsevier Inc. This is an open access article under the CC BY-NC-ND license (http://creativecommons.org/licenses/by-nc-nd/4.0/).

Two years of work in solitude



ANNALS

of PHYSICS

ABSTRACT

Casimir force in cosmology?



What's the difference?



Equivalence principle: space-time is the same for everything

THE ELECTROMAGNETIC SPECTRUM





Equivalence principle: space-time is the same for everything





Horizon



THE ELECTROMAGNETIC SPECTRUM

Planck





The result(s)

D. Berechya & UL, MNRAS 507, 3473 (2021)

Renormalised vacuum energy depends on changes in n



t

The anomaly

PHYSICAL REVIEW D VOLUME

. .

Trace anomaly of a conformally invariant quantum field in curved spacetime

Robert M. Wald

Enrico Fermi Institute, University of Chicago, Chicago, Illinois 60637 (Received 19 August 1977)

VOLUME 17, NUMBER 6

15 MARCH 1978

Energy conservation: a thermodynamic argument

$dE = -pdV = d(\varepsilon V) = Vd\varepsilon + \varepsilon dV$

Energy conservation: a thermodynamic argument

 $dE = -pdV = d(\varepsilon V) = Vd\varepsilon + \varepsilon dV$

 $\frac{dV}{V} = 3\frac{dM}{M} \Rightarrow d\varepsilon = -3(\varepsilon + p)dM$

Energy conservation: a thermodynamic argument

 $dE = -pdV = d(\varepsilon V) = Vd\varepsilon + \varepsilon dV$

 $\frac{dV}{V} = 3\frac{dM}{M} \Rightarrow d\varepsilon = -3(\varepsilon + p)dM$



Friedman

The anomaly: a thermodynamic argument



 $\dot{\varepsilon} = -3H(\varepsilon + p)$

 $\varepsilon = \varepsilon_{vAC} + \varepsilon_{A}, \quad \rho_{A} = -\varepsilon_{A}$

Casimir cosmology: astrophysics, analogues & more



Dror Berechya Masters 2020 PhD student 2021-





Itai Efrat Masters 2019-21

Nikolay Ebel Masters 2020-



Editors' Suggestion

Van der Waals anomaly: Analog of dark energy with ultracold atoms

Itai Y. Efrat and Ulf Leonhardt Department of Physics of Complex Systems, Weizmann Institute of Science, Rehovot 761001, Israel



Comparison with astronomical data

MNRAS **507**, 3473–3485 (2021) Advance Access publication 2021 August 6

Lifshitz cosmology: quantum vacuum and Hubble tension

Dror Berechya[®] and Ulf Leonhardt^{*}

Weizmann Institute of Science, Rehovot 7610001, Israel

Accepted 2021 August 9. Received 2021 June 15; in original form 2020 November 24

https://doi.org/10.1093/mnras/stab2345



Comparison with Pantheon supernova data



Hubble diagram

Casimir cosmology: continuous n(t), varying Λ

n(*t*)

ct
COSMOLOGY

Tensions between the early and late Universe

A Kavli Institute for Theoretical Physics workshop in July 2019 directed attention to the Hubble constant discrepancy. New results showed that it does not appear to depend on the use of any one method, team or source. Proposed solutions focused on the pre-recombination era.

NATURE ASTRONOMY | VOL 3 | OCTOBER 2019 | 891–895 | www.nature.com/natureastronomy

meeting report

A Comprehensive Measurement of the Local Value of the Hubble Constant with 1 km s⁻¹ Mpc^{-1} Uncertainty from the Hubble Space Telescope and the SH0ES Team

ADAM G. RIESS,^{1,2} WENLONG YUAN,² LUCAS M. MACRI,³ DAN SCOLNIC,⁴ DILLON BROUT,⁵ STEFANO CASERTANO,¹ DAVID O. JONES,⁶ YUKEI MURAKAMI,² GAGANDEEP S. ANAND,¹ LOUISE BREUVAL,² THOMAS G. BRINK,⁷ ALEXEI V. FILIPPENKO,^{7,8} SAMANTHA HOFFMANN,¹ SAURABH W. JHA,⁹ W. D'ARCY KENWORTHY,² JOHN MACKENTY,¹ BENJAMIN E. STAHL,⁷ AND WEIKANG ZHENG⁷



arXiv:2112.04510



Indirect determination of Hubble constant from Cosmic Microwave Background





E. Di Valentino, MNRAS **502**, 2065 (2021)

Correlations in the Cosmic Microwave Background







Correlations in the Cosmic Microwave Background





Correlations in the Cosmic Microwave Background





Observed Hubble constant is consistent with Lifshitz theory



10² theories

OPEN ACCESS

IOP Publishing

Class. Quantum Grav. 38 (2021) 153001 (110pp)

Topical Review

In the realm of the Hubble tension—a review of solutions*

Classical and Quantum Gravity

https://doi.org/10.1088/1361-6382/ac086d

Eleonora Di Valentino^{1,**}, Olga Mena², Supriya Pan³, Luca Visinelli⁴, Weiqiang Yang⁵, Alessandro Melchiorri⁶, David F Mota⁷, Adam G Riess^{8,9} and Joseph Silk^{8,10,11}

10² theories, new fields, new GR, new cosmology

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Classical and Quantum Gravity

https://doi.org/10.1088/1361-6382/ac086d



No new fields.



Why only QED?



Why only QED? Experimental tests?



Why only QED? Experimental tests? Astronomical tensions?



Why on Experim Astrono Renorm

- Why only QED?
- Experimental tests?
- Astronomical tensions?
- Renormalization?



Why on Experim Astrono Renorm

• • •

- Why only QED?
- Experimental tests?
- Astronomical tensions?
- Renormalization?





Let there be light!



